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# Dynamic System Representation of Basic and Non-Linear in Parameters Oscillatory Motion Gestures

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NOTE: At the time of publication, author Daniel Koditschek was affiliated with the University of Michigan. Currently, he is a faculty member in the School of Engineering at the University of Pennsylvania.

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## **Comments**

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# Dynamic System Representation of Basic and Non-Linear in Parameters Oscillatory Motion Gestures

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## ABSTRACT

We present a system for generation and recognition of oscillatory gestures. Inspired by gestures used in two representative human-to-human control areas, we consider a set of oscillatory (circular) motions and refine from them a 24 gestures lexicon. Each gesture is modeled as a dynamic system with added geometric constraints to allow for real time gesture recognition using a small amount of processing time and memory. The gestures are used to control a pan-tilt camera neck. The gesture lexicon is then enhanced to include non-linear in parameter ("come here") gesture representations. An enhancement is suggested which would enable the system to be trained to recognize previously unidentified yet consistent human generated oscillatory motion gestures.

## Developing A Gesture Lexicon

Sociological and biological research on human created gestures suggests that while gestures have standard meanings within a society, no known body motion or gesture has the same meaning in all societies [1]. Even in American Sign Language, few signs are so clearly transparent that a non-signer can guess their meaning without additional clues [6]. Thus we are free to create gestures for device control as we see fit.

### Examples of a Human Gesture Control Environment.

Two areas in which gesture languages have developed to communicate commands are crane and excavator<sup>1</sup> and runway traffic control. A sample set of crane control gestures, shown in Figure 1 [3], is composed of oscillating planar motions, that is, circles or back-and-forth lines made in two dimensions in real world three dimensional space. Certain gestures used to signal aircraft on a runway are also planar oscillators [10].

The use of gestures in these environments shows that oscillatory motions are useful for several reasons. First, oscillatory motions are recognizable by other humans and

<sup>1</sup> Thanks to Prof. Louis Whitcomb for suggesting this application.

used in critical and potentially dangerous areas. Second, humans can easily and consistently make oscillatory motions. Third, some oscillatory gestures have time dependent content which can be created and understood by humans. For example, the "travel ahead" gesture's circular velocity is increased when a faster response is desired.

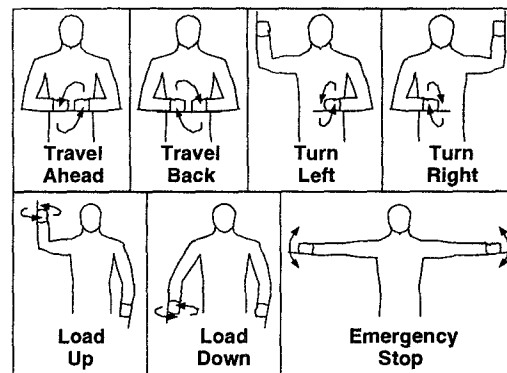


Figure 1: Sample crane control gestures.

### An "Oscillating Motion" Gesture Lexicon.

The oscillating circles and lines used in the crane and runway lexicons form the basis of the gestures used in our system. When the geometric features of size and direction are added, the lexicon is expanded to encompass 24 gestures (Figure 2).

## Identification Method for Gestures Represented as a Dynamic System

A representative planar gesture, used throughout this section to exemplify our method, consists of a family of oscillating motions which form a (roughly) horizontal line segment ("x-line motion"). Humans are incapable of reliably generating a perfect sinusoidal motion, as we suggest by the illustrated x-line motion shown Figure 3. We find it most convenient to represent such motions as they evolve over time in the x-velocity plotted against the x-position "phase plane" space. This figure, in its evident departure from a pure sinusoid, suggests the natural range of variation that we would nevertheless like to

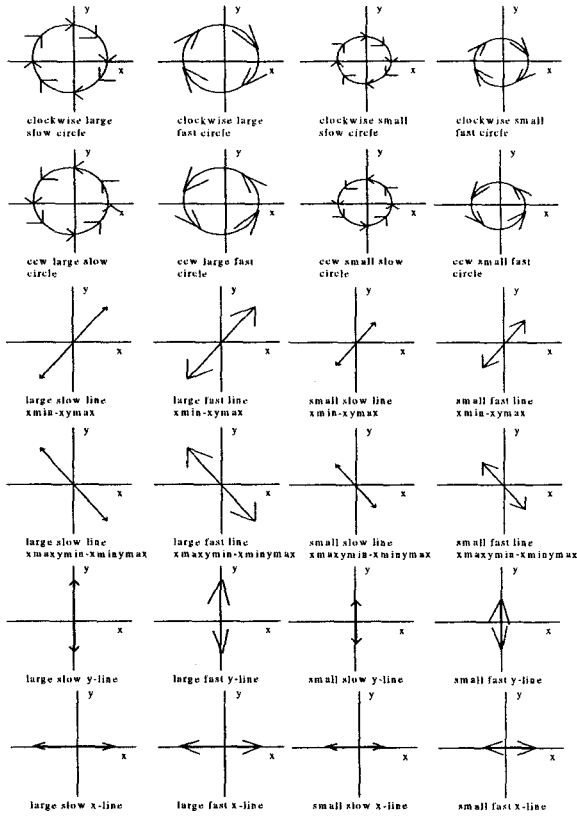


Figure 2: The 24 Gesture Lexicon.

associate with the same gesture. We desire a computationally effective mathematical representation for such gestures.

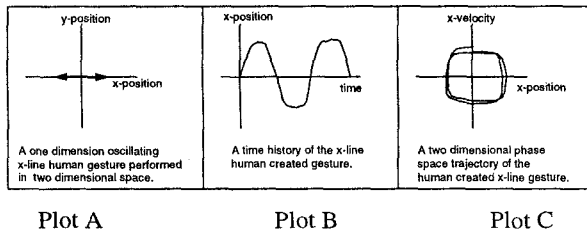


Figure 3: Plots of a Human Create One Dimensional X-Line Oscillating Motion

Out of the enormous variety of possible representations, we choose to rely on the dynamic properties of simple physical motions. A dynamic system is a mathematical model describing the evolution of all possible states in some state space as a function of time [5]. Given an initial state, the evolution over time of subsequent states is called a “trajectory” or “motion”. We use a differential equation representation of a dynamic system. Specifically, a vector field,  $f$ , parameterized by a carefully chosen combination of tunable constants,  $\theta$ , comprises our representation of gestures and the motions associated with them.

### Notation and Terminology.

For ease of exposition, we present in this section the abbreviations and definitions used throughout this paper. Parameterized differential equation models can be divided into two types: non-linear-in-parameters (NLIP) and linear-in-parameters (LIP) (which include linear systems). The two models can be further subdivided into linear-in-state (LIS) and non-linear-in-state (NLIS). Given such a representation, the instantaneous output of our model takes the form of a tangent vector,  $\dot{x}$ , that depends upon the present state (input,  $x$ ) and parameter setting,  $\theta$ .

### Representing Oscillatory Motions.

We “invent” certain differential equations, composed of state variables and parameters, which intuition suggests may represent human gestures. It is advantageous to use a NLIP/NLIS model because it covers a much broader range of systems than an LIP model. However, for reasons to be discussed below, we find it expedient to use a LIP model. We choose to represent planar oscillatory gestures as second order systems with the intuition that a model based on the acceleration (physical dynamics) of a system is sufficient to characterize the gestures in which we are interested.

An LIP representation has the form:

$$\dot{x}(t) = f(x)\theta \quad (1)$$

where  $\theta$  represents tunable parameters. Fixing the parameters yields a unique set of motions, with different initial conditions. With the intuition in mind of capturing the variability of human motion, each such set of motions we take to represent one specific gesture. Choosing different values of  $\theta$  in a given representation results in a family of sets of motions — a “gesture family”.

For example, we might represent an oscillatory circular gesture as combinations of two ( $x$  and  $y$  axis) two-dimensional state space representations:

$$\begin{aligned} \dot{x}_1 &= x_2 & \dot{y}_1 &= y_2 \\ \dot{x}_2 &= \theta_{x_1} x_1 & \dot{y}_2 &= \theta_{y_2} y_2 \end{aligned} \quad (2)$$

where  $x_1$  and  $y_1$  represent the position of the gesture on the  $x$  and  $y$ -axis,  $x_2$  and  $y_2$  are its  $x$  and  $y$ -axis velocity, and  $\theta_{x_1}$  and  $\theta_{y_1}$  are specified parameters. For any constant  $\theta < 0$ , all trajectories (on each axis) satisfy  $-\theta_1 x_1^2 + x_2^2 = const$ , as can be seen by direct differentiation (figure 4). A gesture begun at any point (initial condition) in its trajectory should still be identified as the same oscillating line.

Our family of gestures (the family of sets of trajectories) is a mathematical model which contains a finite number of tunable parameters (although, in the final implementa-

tion, parameters will not be the sole basis of gesture classification). In order to categorize a finite number of gestures in this family and to permit further variability in the exact motions associated with a particular gesture within this family, we partition the parameter space into a finite number of cells — the “lexicon” — and associate all parameter values in the same cell with one gesture. We use off-line simulations to determine the location of these cells.

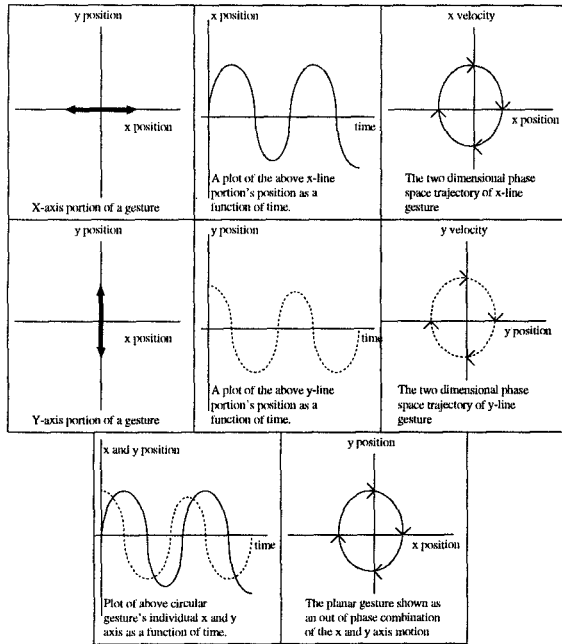


Figure 4: Formation of a Circular Gesture.

#### Tuning Gesture Model Parameters.

Our gesture model and parameter determination scheme arises from the following considerations. First, we abandon off-line “batch” techniques in favor of on-line “sequential” ones because we desire our recognition system to identify gestures as they are generated.

Previously, in an attempt to use only position data, we considered the possible role of an adaptive estimator (which *estimates* unknown states for purely LIP/LIS systems). We abandoned this approach because we found the limitation to LIS models could not adequately handle imperfect human gestures.<sup>2</sup>

A Linear Least Squares method (LLS), which makes use of all the data independent of ordering, is our choice for

<sup>2</sup> We also examined an on-line gradient descent method, but for presently available methods applicable to sequential estimates of NLIP systems, there is no guarantee that the parameters will converge towards their optimal values. In consequence, the parameters computed via this method are data order dependent.

parameter identification. The recursive LLS technique works for LIP, but not NLIP, models.

Given an LIP  $n$ th order system (eq. 1), the identification error due to  $\theta$  for all sampled times from 0 to  $t$  is:

$$\sum_{k=1}^m e_k = \sum_{k=1}^m \|\dot{x}_k - f(x_k)\theta\|^2 \quad (3)$$

Because the system is LIP, we can uniquely (assuming a good data set) determine  $\theta$  based on all input and output data by a formula which minimizes the above error function. However, an equivalent sequential version of this batch approach can be derived by considering each successive error,  $e_k$  as the data arrives. Taking the gradient of  $e_k$  and using appropriate algebra yields the sequential update law [7]:

$$\begin{aligned} \theta_{k+1} &= \theta_k + R_{k+1}^{-1} f_{k+1}^T (\dot{x}_{k+1} - f_{k+1} \theta_k) \\ R_{k+1}^{-1} &= R_k^{-1} - R_k^{-1} f_k^T (f_k R_k^{-1} f_k^T + 1)^{-1} f_k R_k^{-1} \end{aligned} \quad (4)$$

where  $\theta$  denotes the present parameter estimate, and  $R_k$  denotes the local expression of the batch LLS pseudo-inverse.

#### Various Gesture Models

The following five LIP models are candidates for circle and line gesture representations. Each model represents only one dimension of motion. An oscillating circle or line is formed when two of these decoupled models are present, one for each planar motion dimension. The position and velocity states are denoted  $x_1$  and  $x_2$  respectfully. They are of the form  $\dot{x}_1 = x_2$ , and for

- Linear with offset:  $\dot{x}_2 = \theta_1 x_1 + \theta_2$
- Van der Pol:  $\dot{x}_2 = \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_2 x_1^2$
- Van der Pol with offset:  $\dot{x}_2 = \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_2 x_1^2 + \theta_4$
- Higher Order Terms:  $\dot{x}_2 = \theta_1 x_1 + \theta_2 x_1^2 + \theta_3 x_1^3 + \theta_4 x_2 + \theta_5 x_2 x_1^2 + \theta_6$
- Velocity Damping:  $\dot{x}_2 = \theta_1 x_1 + \theta_2 x_1^2 + \theta_3 x_1^3 + \theta_4 x_2 + \theta_5 x_2 x_1^2 + \theta_6 x_2^3 + \theta_7 x_1^2 x_2^3 + \theta_8$

To use the models described here on a digital computer, a fourth-order Runge-Kutta integration method is used. Simulations showed that a sampling rate of 60 Hz is sufficiently small to allow the use of this method.

#### Choosing a Gesture Model via Residual Calculation.

A predictor bin, composed of a model with parameters tuned to represent a specific gesture, determines a gesture's future position and velocity based on its current

state. To measure the accuracy of the bin's prediction, we compute an instantaneous residual error, which is the normalized difference between the bin's prediction and the next gesture state (normalized version of  $e_k$  in equation 3). The total residual error is an exponentially decayed summation of the residual error. A bin that predicts the future state of a gesture it truly represents should have a smaller residual error than a bin tuned to other gestures.

For the residual error calculations, we used position and velocity data from slow, medium and fast circular gestures. In simulations, the total residual error was calculated by subjecting each predictor bin to each gesture type. For example, Table 1 lists the residual errors for one of the proposed models.

A measure of a model's usefulness is determined by examining the ratio of the lowest residual error to the next lowest residual error in each column. The worst "residual error ratio" is the smallest ratio from all the columns because it is easier to classify a gesture when the ratio is large. A comparison of the worst "residual error ratio" of each model we consider is summarized in Figure 5, and suggests that the velocity damping model is the best choice for our application. However, for our on-line gesture recognition experiments, we will use the model with the clearest physical meaning, Linear with Offset Component, so we can both most intuitively assess our results and determine if gesture discrimination is possible when the residual ratio is that large.

	gesture input		
	slow	medium	fast
slow bin	<b>1.31</b>	1.20	1.37
medium bin	14.1	<b>0.24</b>	1.01
fast bin	424	23.1	<b>0.23</b>

**Table 1: Residual Errors of Linear with Offset Component Model**

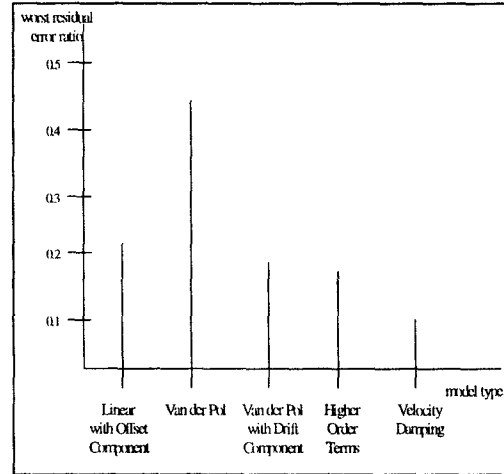
### A Dynamic Gesture Recognition and Control System

In this section we detail the specific components of the dynamic gesture recognition system. Figure 6 illustrates the signal flow from gesture creation, sensing, identification, and transformation into an executed robot response. The gesture recognition system is implemented on a INMOS based distributed transputer control system built by Rizzi *et. al.* [9], that also inspired this architecture.

#### System Modules.

In module G, the Gesture Creator, a human moving a flashlight against a black background creates a gesture. Our gesture lexicon, the set of gestures our system can recognize, consists of 24 planar oscillators. The user sig-

nals the start and stop of a gesture by turning the flashlight on and off, thus enabling isolation of gestures, one from another. The sensor module detects the light from the flashlight.



**Figure 5: Model residual ratios: the Velocity Damping model discriminates most effectively, and the Van der Pol model discriminates least effectively, for the data considered**

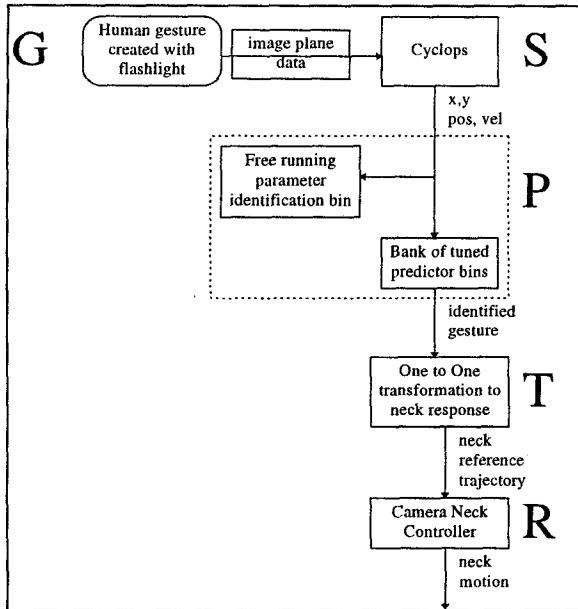
The Sensor Module, S, using the Cyclops vision system [9], detects the gesture by transforming the light from a flashlight bulb into x and y position and velocity coordinates, sending them to the Predictor Module at a rate of 60 Hz.

The Predictor Module, P, contains a bank of predictor bins (inspired by Narendra and Balakrishnan's work [8]). Each predictor bin contains a dynamic system model with parameters preset to a specific gesture. We assume that the motions of human circular gestures are decoupled in x and y. Therefore, there are separate predictor bins for the x and y axes. Since there are three basic gestures, a total of six predictor bins is required.

Each bin's model is used to predict the future position and velocity of the motion by feeding the current state of the motion into the gesture model and computing a residual error. The bin, for each axis, with the least residual error is the best gesture match. If this lowest value is not below a predefined threshold, then the result is ignored; no gesture is identified. Otherwise, geometric information is used to constrain the gesture further. A single gesture identification number, which represents the combination of the best x bin, the best y bin, and the geometric information, is outputted to the transformation module upon the initiation of the gesture, and is continually updated until the flashlight turns off.

The predictor module also contains two bins, one for each axis, for identifying the actual parameters of human generated motions using the linear least squares tech-

nique. During our research, these “gesture parameter identification bins” were used to recompute the parameters seeded in each predictor bin and to allow users to confirm that they presented the gestures they intended. The states of the identification bins are reset at the beginning of each new gesture.



**Figure 6: Gesture Recognition System Architecture**

The Transformation module, T, uses the gesture classification to determine an appropriate response for the controlled robot. The response in this system is a reference trajectory which, when followed by a camera neck, will “mimic” the observed gesture. This allows the person creating the gesture to know immediately if the recognition system properly identified the gesture.

The actuated mechanism, module R, tracks the reference trajectory using an inverse dynamics controller.

### Experiments and Results

Two types of experiments were performed. The first experiment, trial “A”, was designed to test the gesture recognition system’s ability to recognize gestures despite the fact that humans vary the way they make the same gesture. In this experiment, the subject repeated each gesture in the lexicon twenty times. In the second experiment type, trials “B”, “C”, and “D”, we tested how well the system can recognize gestures when presented with different gestures in a random order by having subjects perform gestures from a randomly ordered list: “B” contained “large gestures”, “C” contained “circular gestures”, and “D” contained all types.

The experimental results are summarized in Table 2, showing that the system achieves a greater than 85% correct classification rate. Note that two subjects performed

all experiments, while two others performed only “B” and “C”.

Subject	A	B	C	D
0	87%	92%	94%	90%
1	91%	86%	86%	86%
2	n/a	86%	90%	n/a
3	n/a	90%	90%	n/a

**Table 2: Recognition Experiment Results.**

### System Features.

As a natural byproduct of the gesture’s dynamic systems representation, our system requires a small amount of memory because it stores a representation of the gesture “generator” (Equation 1), rather than of the spatial array of data (Figure 3). Specifically, the memory required increases linearly with the size of the gesture lexicon and with the number of model parameters.

The use of a predictor results in small computational requirements for gesture recognition. These computations can be performed at camera field rate (60 Hz) (other experiments have shown that the prediction module still functions at field rate at least up to a ten parameter model). Additional small memory parallel processors could be added to allow for an increased lexicon, with the calculations farmed out to the added processors.

### Non-Linear Gestures

Human gestures consist of more than basic circles and lines. The “come here” or “go there” motions represent a useful class of gestures that our system should be able to identify. A person creates a “come here” motion by sweeping one hand repeatedly, first quickly toward their body then slowly away. A non-linear-in-state model is required to represent these types of gestures due to the dynamics of their motions. Therefore, we define these motions as non-linear gestures.

### Model Determination

In addition to using the previously defined linear-in-parameter models to represent circle, line, and skew gestures, we created extra linear-in-parameter models based on the Velocity Damping Terms model. Using the same analysis procedure for determining a non-linear gesture model as was used for determining a linear gesture model, we determined that the following model (termed Velocity Damping B) worked best (out of an additional four possible models A through D):

$$\dot{x}_2 = \theta_1 x_1 + \theta_2 x_1^2 + \theta_3 x_1^3 + \theta_4 x_2 + \theta_5 x_2 x_1^2 + \theta_6 x_2^3 + \theta_7 x_1^2 x_2^3 + \theta_8 x_1^4 x_2 + \theta_9 x_1^5 + \theta_{10}$$

For the residual measurement experiment, three circular and four skew gestures were used. The three circular gestures were slow, medium, and fast. The four skew gestures were back left (hand sweeps towards the left side of the body), back right (hand sweeps towards the right side of the body), front left (hand sweeps away from the left side of the body), and front right (hand sweeps away from the right side of the body).

Specific details of the experiments can be found in [2]. The simulation experiments are summarized in Figure 7. Our analysis indicates that adding more non-linear terms to the linear-in-parameters model enables the predictor bin to better discriminate between skew gestures. However, the time needed to identify gestures increases with parameter size. We limit our model to ten parameters, because we want to be certain our system identifies gestures at field rate.

#### Automatic Adding of New Gestures to the Lexicon

When the predictor bins fail to recognize a gesture, then either the human was making random motions, or the human made a gesture unknown to the predictor bins. If the latter is the case, then we can use the x and y identification bins to determine the gesture's parameters. New predictor bins, seeded with these parameters, would be able to recognize the gesture in the future.

We now present a method for using the identification bins to automatically add new gestures to the lexicon. While a gesture is being created, the parameters from the x and y identification bins are used to seed two x and y predictor bins. A residual error measurement is computed from these bins. When the gesture is completed then the system determines if a gesture was recognized. If none of the prediction bins that were tuned to the gestures in the lexicon produce a lower residual error measurement than the pre-defined threshold, then no gesture was recognized. If no gesture was recognized, and the system determines that the residual error measurement from the new parameter bins is lower than the threshold, then a new gesture was identified.

When a new gesture is identified, a new permanent predictor bin for each axis, seeded with the computed parameters, is added to the predictor bins which represent the gesture lexicon. An arbitrary classification number is assigned to this combination of x and y motion and is sent to the transformation module whenever this gesture is recognized in the future.

#### Acknowledgments.

We thank Dr. Al Rizzi for his advice concerning various technical and theoretical aspects of this work, and Laura Sosnowski for her help with the figures.

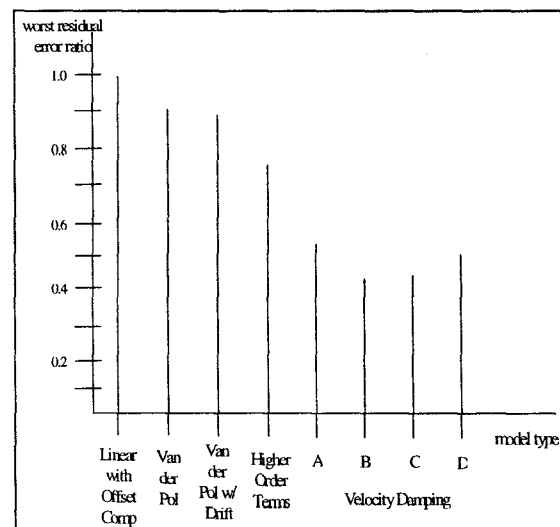


Figure 7: The worst case residual ratios for each gesture model. The lower the ratio, the better the model.

#### Bibliography

- [1] R. L. Birdwhistell. *Kinesics and Context; essays on body motion communication*. Phila., PA, 1970.
- [2] C. Cohen. Dynamical system representation, generation, and recognition of basic oscillatory motion gestures and applications for the control of actuated mechanisms. Ph.D. Dissertation, U. of Mich., 1996.
- [3] Link-Belt Construction Equipment Company. *Operating safety: Cranes and excavators*, 1987.
- [4] L. Conway. System and method for teleinteraction. U.S. Patent 5,444,476, August 1995.
- [5] M. Hirsch and S. Smale. *Differential Equations, Dynamical Systems, and Linear Algebra*. Academic Press, Inc., Orlando, Florida, 1974.
- [6] E. Klima and U. Bellugi. Language in another mode. *Language and brain: Developmental aspects, Neurosciences research prog. bulletin.*, 12(4):539-550, 1974.
- [7] P. Kumar and P. Varaiya. *Stochastic Systems: Estimation, Identification, and Adaptive Control*. Prentice-Hall, Inc., Englewood Cliffs, NJ, 1986.
- [8] K. Narendra and J. Balakrishnan. Improving transient response of adaptive control systems using multiple modls and switching. *IEEE Trans. On Auto. Control*, 39:1861-1866, Sept 1994.
- [9] A. Rizzi, L. Whitcomb, and D. Koditschek. Distributed real-time control of a spatial robot juggler. *IEEE Computer*, 25(5), May 1992.
- [10] FAA U.S. Dept. of Transportation. *Aeronautical information manual: official guide to basic flight information and ATC procedures*, 1995.