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Fluctuations and Rheology in Active Bacterial Suspensions

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Abstract

We probe nonequilibrium properties of an active bacterial bath through measurements of correlations of passive tracer particles and the response function of a driven, optically trapped tracer. These measurements demonstrate violation of the fluctuation-dissipation theorem and enable us to extract the power spectrum of the active stress fluctuations. In some cases, we observe $1/\sqrt{\omega}$ scaling in the noise spectrum which we show can be derived from a theoretical model incorporating coupled stress, orientation, and concentration fluctuations of the bacteria.

Disciplines

Physical Sciences and Mathematics | Physics

Comments

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Fluctuations and Rheology in Active Bacterial Suspensions

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We probe nonequilibrium properties of an active bacterial bath through measurements of correlations of passive tracer particles and the response function of a driven, optically trapped tracer. These measurements demonstrate violation of the fluctuation-dissipation theorem and enable us to extract the power spectrum of the active stress fluctuations. In some cases, we observe $1/\sqrt{\omega}$ scaling in the noise spectrum which we show can be derived from a theoretical model incorporating coupled stress, orientation, and concentration fluctuations of the bacteria.

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Active complex fluid systems such as living cells [1,2], assemblies of motors and filaments [3], flocks of birds [4], and vibrated granular media [5] differ from conventional equilibrium media in that some of their components consume and dissipate energy, thereby creating a state that is far from equilibrium. An understanding of model active systems, even at a phenomenological level, provides insight about fundamental nonequilibrium statistical physics and, potentially, about the inner workings of biological systems. Bacterial baths [6–10] are attractive model active systems because energy input is homogeneous, because individual bacteria can be directly observed, and because critical parameters such as density, activity, and swimming behavior [6] can be brought under experimental control. Indeed, recent experiments have reported on a rich variety of nonequilibrium phenomena in this system class including anomalous diffusion [7] and pattern formation [9,11], while recent theories of self-propelled organisms predict ordered phases such as “flocks” [4], their instabilities [12], novel rheological effects [13], and giant density fluctuations [14].

In this Letter, we describe measurements of the fluctuations and mechanical responses of an active bacterial suspension. In contrast to previous work [7–9], we concurrently measure the one- and two-point correlation functions of embedded passive tracer particles to assess material fluctuations over a wide range of length scales [15], and we independently measure the macroscopic response function of the “active” medium by displacing a particle through it with an optical trap [16]. Even at a low volume fraction ($\phi \sim 10^{-3}$) of bacteria, fluctuations in the medium are substantially greater than they are in the absence of bacteria while rheological response is unchanged, implying a strong violation of the fluctuation-dissipation theorem (FDT). The mean-square displacements (MSDs) of tracer particles as a function of time Δt depend on swimming behavior. For wild-type bacteria, the MSD extracted from two-point correlations scale superdiffusively as $\Delta t^{3/2}$ for the time scale of our experiments, and the stress power spectrum [2] as a function of fre-

quency ω scales as $\phi/\sqrt{\omega}$. Existing theories of active media [12] predict long-time tails and anomalous corrections to diffusion but not superdiffusion. We propose a theoretical model, following Ref. [13], that accounts for our experimental observations.

We used two strains of *E. coli*, a rod-shaped bacterium with dimensions $3 \times 1 \mu\text{m}$, in these studies: RP437, the “wild type”, which runs and tumbles [17] and RP1616, the “tumbler”, which predominantly tumbles [18]. Overnight cultures were diluted 1/300 in Luria Broth (Difco) and grown at 25 °C for 6 h. Subsequently, they were centrifuged for 10 minutes at 5000 rpm and resuspended to the desired concentration in a buffer comprised of 10 mM K_2HPO_4 , 0.1 mM EDTA, and 0.2 wt% glucose ($\text{pH} = 8.2$), which was added to maintain bacterial motility. We added a small amount ($\phi_s = 10^{-4}$) of fluorescently labeled polystyrene spheres (Duke Scientific) of radius a to the bacterial suspension, and to density match them, we added 15 wt% sucrose to the solution. To prevent bacterial adhesion, we prepared the chambers from bovine serum albumin coated glass slides and cover slips. We used parafilm spacers to bring the thickness of the chambers to $\sim 240 \mu\text{m}$, and we recorded quasi-2D image slices from the middle of the 3D chamber. Samples were loaded into the chamber and sealed with optical glue just prior to each run.

We quantified the fluctuations in the bacterial bath by computing MSDs from the motions of embedded micron-sized tracers [15]. The one-point displacement (MSD1) is defined by $\langle \Delta \mathbf{r}^2(\Delta t) \rangle_1 = \sum_i \langle \Delta r_i(t, \Delta t) \Delta r_i(t, \Delta t) \rangle$, where $\Delta r_i(t, \Delta t) = r_i(t + \Delta t) - r_i(t)$ is the particle displacement in the $i = (x, y, z)$ direction in time Δt , and the brackets denote time and ensemble averaging. The two-point displacement (MSD2) is defined as $\langle \Delta \mathbf{r}^2(\Delta t) \rangle_2 = (2R/a)D_{rr}(R, \Delta t)$, where $D_{rr}(R, \Delta t)$ is the longitudinal component $D_{rr}(R, \Delta t) = D_{ij}R_iR_j/R^2$ of the two-point tensor $D_{ij}(R, \Delta t) = \langle \Delta r_i^{(1)}(t, \Delta t) \Delta r_j^{(2)}(t, \Delta t) \rangle$, which measures correlations of two distinct particles (1, 2) with an initial separation $\mathbf{R}$. Over the time scale of our experiments, $\mathbf{R}$ lies in the focus plane of our microscope and its magnitude

$R \equiv |\mathbf{R}|$ is greater than that of individual particles' displacements. The main advantage of two-point microrheology is that it provides a more reliable measure of length-scale dependent fluctuations in media where the length scale of heterogeneities and tracer boundary conditions are not *a priori* known [2,15]. Indeed, since $D_{ij}(R, \Delta t)$ is ensemble averaged over tracer pairs with $R \gg a$, it reflects the dynamics of the medium on larger length scales than the tracer size, permitting quantitative measurements even in the presence of heterogeneities. In general, MSD2 will equal MSD1 if heterogeneities in the medium have length scales smaller than the tracer size, otherwise they will differ in both magnitude and functional form.

Typical MSD data are presented in Fig. 1, which shows that the one-point MSD in both bacterial strains displays a crossover from superdiffusive behavior at short lag times ($\langle \Delta r^2 \rangle_1 \sim \Delta t^\alpha$, $1 < \alpha < 1.5$) to diffusive behavior ($\alpha = 1$) at long lag times. This observation is similar to that of Ref. [7]. However, our two-point data for the wild type, by contrast, exhibit a nearly power-law superdiffusion ($\langle \Delta r^2 \rangle_2 \sim \Delta t^{1.5}$) over 2.5 decades of observation time. We also verified that $D_{rr}(R, \Delta t) \sim 1/R$ (see inset of Fig. 1), indicating that the bacterial bath, though an active medium, can be treated on the separation scale R as a coarse-grained continuum whose properties can be probed with two-point microrheology [2,15]. That MSDs exhibit superdiffusion is suggestive of but not a proof of violation of FDT, which requires an independent measurement of the rheological response function.

Response measurements were performed using an oscillating optical tweezer setup similar to that of Ref. [16]. Briefly, an optical trap with typical trap stiffness of $\sim 1 \times 10^{-3}$ pN/nm was formed by focusing an ~ 100 mW laser beam ($\lambda = 1054$ nm) through a 1.3 numerical aperture oil immersion objective (Zeiss). The trapping beam position

FIG. 1. 1-pt (open symbols) and 2-pt (closed symbols) mean-square displacements divided by the lag time, Δt , for $2a = 2 \mu\text{m}$ particles in bath of wild-type RP437 (triangles) and tumbling RP1616 (circles) bacteria at $\phi = 0.003$. Inset: $RD_{rr}(R, \Delta t = 0.067 \text{ sec})$ demonstrating $D_{rr} \sim 1/R$ for $R \geq 10 \mu\text{m}$, and implying correlation length $\xi_U \leq 10 \mu\text{m}$.

was sinusoidally scanned using a galvo mirror at frequencies from 0.5 to 500 Hz. A $4.0 \mu\text{m}$ polystyrene sphere was trapped $\sim 6 \mu\text{m}$ from the cover slip. The position of the tracer was detected using forward scattered light from a colinearly aligned HeNe laser beam focused onto a split photodiode (Hamamatsu S4204). The photodiode signal was fed into a lock-in amplifier (Stanford Research Systems 530) along with the reference from the driving function generator signal. The displacement and phase of the trapped particle output by the lock-in amplifier were logged into a PC running LABVIEW (National Instruments).

The equation of motion for a particle of radius a trapped in an oscillating harmonic potential may be written as: $6\pi\eta a \dot{x} = -k[x - A \cos(\omega t)]$, where η is the viscosity of the medium, k is the stiffness of the trap, and A is the driving amplitude. Its steady state solution yields the normalized displacement of the sphere in the trap: $d(\omega) = \{1 + [6\pi a \eta(\omega) \omega / k]^2\}^{-1/2}$.

The inset of Fig. 2 shows the raw normalized displacement data for a particle in water and in active bacterial baths of tumblers and wild types. The solid line is a fit to $d(\omega)$ with $\eta = 0.001$ Pa.s, trap stiffness $k = 8 \times 10^{-4}$ pN/nm, and radius $a = 2.0 \mu\text{m}$. The experimental data agree with each other and with the theoretical curve. From them, we extract the viscosity $\eta(\omega)$ shown in the main graph of Fig. 2. Clearly, the presence of actively swimming bacteria at volume fraction 10^{-3} does not modify the viscosity of the medium from that of water, $\eta(\omega) = \eta_0 = 0.001$ Pa.s. We measured the same $\eta(\omega)$ using a capillary viscometer.

FIG. 2 (color online). Frequency dependent viscosity derived from oscillating trap measurements for $4.0 \mu\text{m}$ sphere in water ($\blacksquare$), the tumbler ($\bullet$), and the wild type ($\blacktriangle$) at $\phi = 0.003$. Viscosities $\eta_2(\omega)$ derived from the averaged two-point measurements using the generalized Stokes-Einstein relation are plotted for the tumbler ($\circ$), the wild type ($\triangle$), and a bead in water ($\square$). Inset: normalized displacement of a $4.0 \mu\text{m}$ sphere in the optical trap as a function of driving frequency for wild type (triangles), tumbler (circles), and water (squares). Line is a fit to $d(\omega)$ (see text).

While recent theories of active systems predict novel enhancement in the viscosity [13], our experiments are well below the concentration at which these effects are observable. Instead, our results are consistent with the Einstein result for hard spheres: $\eta = \eta_0(1 + \frac{5}{2}\phi)$, namely, a negligible modification in the viscosity for $\phi \sim 10^{-3}$. Moreover, assuming for the moment the generalized Stokes-Einstein relation, we can extract the (FDT consistent) response from the collapsed two-point displacement (MSD2) [15]: $\eta_2(\omega) = k_B T / 3\pi\omega^2 a \langle \Delta r^2(\omega) \rangle_2$, as shown in Fig. 2. The difference between $\eta(\omega)$ and $\eta_2(\omega)$ explicitly indicates a strong violation of FDT.

Next, to access the heterogeneity of the bacterial bath, we explored the length-scale dependence of fluctuations by systematically varying the size of the tracers at a fixed bacterial concentration. The inset of Fig. 3(a) shows MSDs obtained for spheres in the tumbler bath. All samples and all tracer sizes exhibit a crossover from superdiffusion to diffusion on similar time scales, with an enhanced diffusion coefficient $D = \gamma D_T$, where $\gamma = 4.3$ and $D_T = k_B T / (6\pi\eta_0 a)$ is the equilibrium coefficient. Moreover, MSD1 and MSD2 are nearly equal in magnitude and functional form. Rescaling time by the crossover time τ and the MSDs by $2D_T\Delta t$ collapses all the data onto a master curve: $[\langle \Delta r_x^2(\Delta t) \rangle_1, \langle \Delta r^2(\Delta t) \rangle_2] / (2D_T\Delta t) = \gamma + (1 - \gamma)(1 - e^{-x})/x$, where $x = \Delta t/\tau$. Figure 3(a) shows the collapsed MSD data along with the master curve with $\tau = 0.1$ s.

The MSDs for the wild type are strikingly different: the MSD1 exhibits a crossover dependent on tracer size, while all of the MSD2 exhibit superdiffusion with nearly the same exponent of 1.5 over 2.5 decades of time, independent of the tracer size. The trivial rescaling $a\langle \Delta r^2(\Delta t) \rangle_2$ collapsed the respective MSD2 data [Fig. 3(b)]. Under this rescaling, however (and other simple scaling functional forms as well) the wild-type MSD1 failed to collapse [inset of Fig. 3(b)], signaling the presence of heterogeneity on the tracer length scale. The superdiffusive exponent of the MSD1 approaches that of the two-point data ($\alpha \sim 1.5$) as a increases. This suggests that one-point measurements are intrinsically ambiguous: the activity inferred depends on the tracer size and boundary conditions [2,19]. Two-point measurements, in contrast, provide a more robust characterization of the long-wavelength fluctuations of the medium than one-point measurements.

We employ a recently developed phenomenological theoretical framework for an active medium to interpret the experimental MSD data [2]. The bacterial activity gives rise to nonthermal stress fluctuations whose power spectrum $\Delta(\omega)$ can unambiguously be extracted from *two-point* microrheology data via

$$D_{rr}(R, \omega) = \frac{\Delta(\omega)}{6\pi\omega^2 R |\eta(\omega)|^2}. \quad (1)$$

The results are exhibited in Fig. 4(a). For water, the power spectrum is flat. For the tumblers, it is nearly Lorentzian,

FIG. 3 (color online). (a) Collapsed 1-pt (open symbols) and radius collapsed averaged 2-pt (closed symbols) MSDs for the tumblers at $\phi = 0.003$. The solid line is the master curve: $\gamma + (1 - \gamma)(1 - e^{-x})/x$. Circles, triangles, and squares are for particle diameters $2a = 2.0, 5.0$, and 10.0 μm , respectively. Inset: raw 1-pt (open symbols) and 2-pt (closed symbols) MSDs for tumblers. (b) Radius rescaled 2-pt (closed symbols) MSDs for the wild types at $\phi = 0.003$. Circles, triangles, and squares are for particle diameters $2a = 2.0, 5.0$, and 10.0 μm , respectively. Inset: radius rescaled 1-pt MSD (open symbols) for the same ϕ and particle size data.

flat at low frequencies with a knee at higher frequencies. For wild types, it exhibits power-law behavior, $\Delta(\omega) \sim \omega^{-0.5}$, over 2.5 decades. In both cases, $\Delta(\omega)$ is substantially greater than in a thermal system. For the wild type, the prefactor Δ_0 of $\Delta(\omega)$ rises linearly with the bacterial concentration, as shown in Fig. 4(b).

We propose a simple model to account for the observed spectra of the tumblers and the wild types within the theoretical framework of Ref. [13]. In the process of tumbling or swimming, each bacterium contributes an additional active stress to the medium. It has the form: $\sigma_{ij}^A \propto c(\mathbf{x}, t) S_{ij}(\mathbf{x}, t)$, where $c(\mathbf{x}, t)$ is the concentration of the bacteria and S_{ij} is a force-dipole density generated by the active bacteria. In wild types and tumblers, forces are directed, respectively, along and perpendicular to the long-bacterial axes. Thus, in wild types, S_{ij} is equal to the uniaxial nematic order parameter Q_{ij}^U whereas in tumblers, it is equal to a biaxial order parameter Q_{ij}^B . Active pro-

FIG. 4. (a) The spectrum $\Delta(\omega)$ of active stress fluctuations obtained from two-point microrheology and active response measurements. The triangles are the wild types, circles are the tumblers (both $\phi = 0.003$), squares are water ($\phi = 0$). (b) Linear dependence of the prefactor Δ_0 in $\Delta(\omega)$ on the volume fraction ϕ of the wild-type bacteria; $\Delta_T \equiv 2\eta k_B T$.

cesses enhance stress fluctuations, and assuming long-range isotropy, the active stress fluctuations can be expressed as $\langle \sigma_{ij}^A(\mathbf{q}, \omega) \sigma_{kl}^A(-\mathbf{q}, -\omega) \rangle = \Delta_\sigma(q, \omega) \times [\delta_{ik}\delta_{jl} + \delta_{il}\delta_{jk} - \frac{2}{3}\delta_{ij}\delta_{kl}]$ for both tumblers and wild types. The power spectrum in Eq. (1) is related to $\Delta_\sigma(q, \omega)$ by $\Delta(\omega) = \Delta_\sigma(\mathbf{q} = 0, \omega)$.

The linearized equation for Q_{ij}^A ($A = U, B$) is $\partial_t Q_{ij}^A = -\tau_A^{-1}(1 - \xi_A^2 \nabla^2) Q_{ij}^A + s_{ij}$, where τ_A is the relaxation time, ξ_A the correlation length of Q_{ij}^A , and s_{ij} is a spatial-temporal white noise with zero mean. Interactions among bacteria favor long-range order in Q_{ij}^U but not in Q_{ij}^B , implying that $\tau_B \ll \tau_U$ and $\xi_B \ll \xi_U$. In both cases, the concentration of bacteria obeys the continuity equation: $\partial_t \delta c = -\nabla \cdot \mathbf{J}$ with $J_i = -D\partial_i \delta c - \alpha_2 c_0 \partial_j Q_{ij}^A + \delta J_i$, where c_0 is the average concentration, D is the diffusion constant, δJ_i is a random current, and the second term stems from the nonequilibrium driving of mass flow [4]. These equations lead after Gaussian decoupling to $\Delta_\sigma(\mathbf{q}, \omega) = \Delta_\sigma(q\xi_{\sigma A}, \omega)$ with $\xi_{\sigma A} \approx \xi_A$. In tumblers ξ_B is very small, and $\Delta_\sigma(\omega)$ can be replaced by a Lorentzian $\Delta(\omega)$ with characteristic time $\tau_B \sim 0.1$ s (Fig. 4) [20] in both MSD1 and MSD2, implying agreement between $\langle \Delta \mathbf{r}^2(\Delta t) \rangle_1$ and $\langle \Delta \mathbf{r}^2(\Delta t) \rangle_2$. In wild types, $\Delta_\sigma(q\xi_U, \omega)$ can be replaced by $\Delta(\omega)$ in MSD2 when $R > \xi_U$ [with $\xi_U \leq 10 \mu\text{m}$ (see inset of Fig. 1)], but not in MSD1 when it probes lengths shorter than ξ_U , implying different values for $\langle \Delta \mathbf{r}^2(\Delta t) \rangle_1$ and $\langle \Delta \mathbf{r}^2(\Delta t) \rangle_2$ [Fig. 1]. Our calculations yield $\Delta(\omega) \sim c_0/\sqrt{\omega}$ for $\omega\tau_U > 1$ to lowest order in c_0 , in

agreement with our experiments [20]. This result arises essentially from the concentration fluctuations in the active stress, which were ignored in previous theories. Note also that one might expect that swimming bacteria have a tendency to develop long-range *polar* rather than the nematic order of our model, but we find that incipient polar order yields $\Delta(\omega) \sim c_0^2 \omega^{-3/2}$ in clear disagreement with our measurements [20].

In conclusion, using a combination of passive 2-pt microrheology and active response measurements, we have demonstrated that the macroscopic stress fluctuations depend sensitively on microscopic swimming behavior of the bacteria. When contrasted with other active systems such as living cells, our results suggest that departures from equilibrium proceed via nonuniversal mechanisms.

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