Patterns of Cost for Patients Dying in the Intensive Care Unit and Implications for Cost Savings of Palliative Care Interventions.

Nita Khandelwal

David Benkeser

Norma B Coe

University of Pennsylvania, nbcoe@pennmedicine.upenn.edu

Ruth A Engelberg

Joan M Teno

See next page for additional authors

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OBJECTIVE: To characterize patterns of daily costs of ICU care at the end of life and, based on these patterns, examine the role for palliative care interventions in enhancing value.

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SETTING/PATIENTS: 572 patients who died in the ICU between 2003 and 2005 at a Level-1 trauma center.

METHODS: Data were linked with hospital financial records. Costs were categorized into direct fixed, direct variable, and indirect costs. Patterns of daily costs were explored using generalized estimating equations stratified by length of stay, cause of death, ICU type, and insurance status. Estimates from the literature of effects of palliative care interventions on ICU utilization were used to simulate potential cost savings under different time horizons and reimbursement models.

MAIN RESULTS: Mean cost for a terminal ICU stay was 39.3K ± 45.1K. Direct fixed costs represented 45% of total hospital costs, direct variable costs 20%, and indirect costs 34%. Day of admission was most expensive (mean 9.6K ± 7.6K); average cost for subsequent days was 4.8K ± 3.4K and stable over time and patient characteristics.

CONCLUSIONS: Terminal ICU stays display consistent cost patterns across patient characteristics. Savings can be realized with interventions that align care with patient preferences, helping to prevent unwanted ICU utilization at end of life. Cost modeling suggests that implications vary depending on time horizon and reimbursement models.

Keywords
Cost Savings, Hospital Costs, Intensive Care Units, Length of Stay, Palliative Care

Disciplines
Medicine and Health Sciences

Author(s)
Nita Khandelwal, David Benkeser, Norma B Coe, Ruth A Engelberg, Joan M Teno, and J Randall Curtis

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Nita Khandelwal, MD, MSc,1 David Benkeser, PhD2 Norma B. Coe, PhD3 Ruth A. Engelberg, PhD4,5 Joan M. Teno, MD, MS,5,6 and J. Randall Curtis, MD, MPH4,5

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Conclusions: Terminal ICU stays display consistent cost patterns across patient characteristics. Savings can be realized with interventions that align care with patient preferences, helping to prevent unwanted ICU utilization at end of life. Cost modeling suggests that implications vary depending on time horizon and reimbursement models.

Introduction

In the United States, ~20% of patients die during a hospitalization with an intensive care unit (ICU) stay.1 Critical care costs are estimated to exceed $82 billion annually, accounting for 13% of inpatient hospital costs.2,3 It is not surprising that strategies that target reducing costs in the ICU are of great interest. One area of focus for this cost reduction is the costs of end-of-life care in the ICU. Despite the relatively high proportion of patients who die in the ICU, most patients would prefer to die at home if diagnosed with a life-limiting illness.4,5 This raises the potential for simultaneously improving quality of care through palliative care services or advance care planning (ACP) by matching patient’s preferences with care received, and reducing intensity and costs of care at the end of life.

However, the potential ICU cost savings associated with improving palliative care and the incentive to realize these savings may vary depending on the perspective (hospital, payer, society), the reimbursement models (fee-for-service, bundled payment, value-based purchasing, capitated system), and the time horizon (short term with a range from days to months vs. long-term range of years). As our reimbursement models incorporate more value-based purchasing, capitated

1Department of Anesthesiology and Pain Medicine, Harborview Medical Center, University of Washington, Seattle, Washington.
2Department of Biostatistics, University of California Berkeley, Berkeley, California.
3Department of Health Services, University of Washington, Seattle, Washington.
4Division of Pulmonary and Critical Care Medicine, Harborview Medical Center, University of Washington, Seattle, Washington.
5Department of Medicine, University of Washington, Seattle, Washington.
6Division of Geriatric Medicine, Harborview Medical Center, University of Washington, Seattle, Washington.

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Interventions such as ACP and palliative care consultation that seek to improve decision-making among clinicians, patients, and families may have different economic implications for terminal ICU stays in different reimbursement models. Modeling potential cost savings from these types of interventions requires an understanding of the patterns and distribution of costs for patients who die in the ICU. For example, shortening length of stay (LOS) is often advocated as a target for cost-saving interventions. However, whether or not significant cost savings can be achieved by shortening LOS in the ICU has been debated. The impact of reducing ICU LOS will vary depending on the proportion of costs that are fixed and the reimbursement model.

The objective of this study was to describe the patterns and breakdown of daily ICU costs in a cohort of patients who died in the ICU to better understand expenditures related to terminal ICU stays and the potential influence of palliative care services or ACP. We describe the variation in total daily costs by ICU day and report the proportion of total costs that were direct variable, direct fixed, and indirect costs. Direct variable costs include supply and drug costs and are responsive to patient characteristics and volume. Direct fixed costs, such as labor (nursing, medical assistants, etc.), are fixed in the short term. Indirect costs are not directly linked to patient care (i.e., information technology and environmental services).

We further explore the pattern of costs by LOS, cause of death, clinical service, type of ICU, and insurance status. In particular, we test two hypotheses for each of these groups: (1) on average, costs are greater the first ICU day than the second day; and (2) on average, costs are stable after the second day. In addition, we examine whether the patterns of costs are similar across different diseases, different types of ICUs, and across different physician disciplines. We demonstrate how these results can be used to simulate what cost savings could look like on both short and long time horizons if interventions that reduce or shorten unwanted ICU utilization were implemented. Our goal is to provide insights for clinicians, healthcare systems, and policy makers on the implications of cost savings regarding end-of-life care in the ICU.

**Methods**

**Design overview**

Data were collected as part of an interdisciplinary multifaceted intervention to improve the quality of end-of-life care for critically ill patients and their families. Eligible patients were adults who had died in an ICU between 2003 and 2005 after a minimum stay of 6 hours. The study setting was a university-affiliated 413-bed Level-1 trauma center. There were 88 ICU beds distributed among five ICUs (medical/cardiac, trauma/surgical, neurology/neurosurgical, burn, and pediatric). The institutional review board approved this study (UW HSC#23503).

**Data collection**

Trained chart abstractors using a standardized chart abstraction protocol reviewed eligible patients’ medical records to obtain demographic (age, gender, type of insurance) and clinical information (diagnoses, ICU, and hospital LOS, code status, life-sustaining treatments). Patient race, education, and cause of death were determined from death certificates. AbSTRACTED data were linked to hospital financial records to obtain detailed cost information.

**Predictors/strata**

The pattern of costs was stratified by cause of death, clinical service, type of ICU, and insurance status. Cause of death was divided into trauma, cancer, cardiac, respiratory, neurological, and other. Clinical service was grouped into general surgery, medicine, neurology, neurosurgery, and other. Type of ICU included neurology, medicine, pediatric, coronary, burn, trauma, and surgical. Insurance was grouped into private, Medicare, other government funded, and other/none/unknown.

**Outcomes**

Costs were used instead of charges since charges bear little resemblance to economic cost, and use of charges as a proxy for economic cost may lead to unwarranted conclusions about economic efficiency. These costs were abstracted by hospital financial analysts directly from patient accounts and represent the total costs for all services provided on each hospital day, including overhead costs, labor costs, and supply costs. In the accounting system, cost components are grouped into 3 categories: direct variable, direct fixed, and indirect. These categories allowed us to capture which costs could change in the short term or the long term. Direct costs represent costs that are traceable to a specific cost center providing direct patient care, such as pharmacy, radiology, respiratory care, laboratory, and microbiology. Direct variable costs include supply and drug costs and are the most responsive to individual patient characteristics such as severity of illness and reason for admission. Direct fixed costs include labor, clinical department administration, and overhead fees. These costs are fixed in the short term, but responsive to patient volume in the long term. For example, wages and contracts are set for the year, but if bed occupancy decreases over time, new contracts with fewer staff or hours could be written. Indirect costs, which are included in the patient bill, represent services provided by cost centers not directly linked to patient care, such as information technology and environmental services. These types of costs are the least amenable to change based on patient characteristics or bed occupancy.

This institution uses the McKesson Explorer platform for hospital accounting; physician fees are generated from a separate organization and were not included in this analysis because they were not available at the ICU-day level. All costs were adjusted for inflation and compared at the 2013 US dollar value.

**Statistical analysis**

**Patterns of ICU costs.** To describe the patterns of total cost over an ICU stay, we examined the average total cost and breakdown by day of stay. The daily pattern and breakdown of costs were then stratified by LOS, cause of death, clinical service, type of ICU, and insurance status. We used generalized estimating equations with independent working correlation matrices to test whether costs were higher on day 1 than day 2 and whether costs were stable thereafter. The
The remaining categories stayed relatively constant. The proportion of costs attributable to supplies decreased from 21% to 12%.

Over the length of the ICU stay, the proportion of total ICU costs compared with 11.8% in the lower tertile.

ICU LOS of only one day had a higher percentage of supply costs (23.2%) and lower percentage of labor costs (33.3%) than patients with longer ICU stays (15.7% and 39.8% for supply and labor, respectively). High total ICU costs were associated with patients defined by covariate levels to see if the trend was constant across patient groups. Details on the regression model and testing procedures are in Appendix A. All analyses were conducted using R 3.1.0 (https://cran.r-project.org/).

**Potential cost savings.** To estimate cost savings that might be associated with the use of ACP and palliative care consultation, we conducted simulations using the patterns and distribution of costs identified in this sample and current estimates of reductions in ICU utilization associated with ACP (37% fewer ICU admissions) and palliative care consultation (26% shorter LOS). We estimate savings based on short and long time horizons.

**Results**

Five hundred and seventy-two patients were included in our sample. The average age was 61 ± 18 years. About 90% of patients were intubated in the last week of life, with 19% dying without any withdrawal of life support. The median ICU LOS was 3 days (interquartile range [IQR]: 1–8). Additional patient characteristics are displayed in Table 1.

**Patterns of cost distributions**

The average total ICU cost per patient was 39.3K ± 45.1K (median 24.1K; IQR 10.4–51.9). Direct fixed costs represented 45% of total hospital costs; direct variable costs were 20%; and indirect costs were 34% of hospital costs. The detailed breakdown of subcategories is displayed in Figure 1. Patients with an ICU LOS of only one day had a higher percentage of supply costs (23.2%) and lower percentage of labor costs (33.3%) than patients with longer ICU stays (15.7% and 39.8% for supply and labor, respectively). High total ICU costs were associated with a higher percentage of costs represented by supplies (correlation = 0.09, p = 0.02) with 17.3% in the upper tertile of total ICU costs compared with 11.8% in the lower tertile.

Over the length of the ICU stay, the proportion of total costs that were represented by labor increased slightly from 35% to 43% by week 2 and were offset by a decrease in proportion of costs attributable to supplies from 21% to 12%. The remaining categories stayed relatively constant.

The average cost of an ICU day over the entire LOS was 7.7K ± 6.1K (median 6.1K; IQR 4.9–8.4). Day of admission was the most expensive (mean 9.6K ± 7.6K; median 6.9K [IQR 5.2–11.0]). The average cost per day after admission was 4.8K ± 3.4K (median 4.3K; IQR 3.5–5.5) (Table 2). Mean daily costs beginning with day of admission, broken down by category of cost, are displayed in Figure 2. The day before death was similar in expense to all other days, excluding admission day.

This pattern of admission day being the most expensive and subsequent days having stable costs was consistent across patients and differed by clinical service, type of ICU, and insurance status (Fig. 3). This pattern was consistent across causes of death. It was also consistent across ICU LOS, provided LOS was ≥7 days. For patients with LOS <7 days, admission day was still the most expensive; however, there was a slight trend of decreasing costs from days 2 through 7.

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**Table 1. Characteristics of Cohort**

<table>
<thead>
<tr>
<th>Characteristic</th>
<th>All Subjects (n=572)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Age at time of death</td>
<td>61.5 ± 17.7</td>
</tr>
<tr>
<td>Females, n (%)</td>
<td>193 (33.7%)</td>
</tr>
<tr>
<td>Race/ethnicity</td>
<td>White 437 (80.5%), Black 34 (6.3%), Asian 39 (7.2%), Hispanic 21 (3.9%), Other 12 (2.2%)</td>
</tr>
<tr>
<td>Level of education</td>
<td>&lt;8th grade 49 (9.1%), Some high school 67 (12.4%), HS/GED 209 (38.6%), Some college 119 (22.0%), Four-year college 70 (12.9%), Graduate level 27 (5.0%)</td>
</tr>
<tr>
<td>ICU length of stay, median (IQR)</td>
<td>3.00 (1.00–8.00)</td>
</tr>
<tr>
<td>Hospital length of stay, median (IQR)</td>
<td>4.00 (1.00–11.00)</td>
</tr>
<tr>
<td>Diagnosis</td>
<td>Heart disease 31 (5.4%), HIV/infection 55 (9.6%), Respiratory 33 (5.8%), GI/liver 26 (4.5%), Stroke/neuro 150 (26.2%), Trauma 63 (11.0%), Cancer 5 (0.9%), Unknown/other 210 (36.6%)</td>
</tr>
<tr>
<td>Cause of death</td>
<td>Trauma 164 (28.7%), Cancer 20 (3.5%), Cardiovascular/cardiac 76 (13.3%), Respiratory 39 (6.8%), Neurological 123 (21.5%), Other 149 (26.0%)</td>
</tr>
<tr>
<td>Intubated in last week of life</td>
<td>521 (87.7%)</td>
</tr>
<tr>
<td>DNR in place at time of death</td>
<td>501 (87.7%)</td>
</tr>
<tr>
<td>Died in setting of full support</td>
<td>406 (75.6%)</td>
</tr>
<tr>
<td>Invasive mechanical ventilation or BiPAP discontinued before death</td>
<td>406 (75.6%)</td>
</tr>
<tr>
<td>CPR in last 24 hours of life</td>
<td>67 (11.7%)</td>
</tr>
<tr>
<td>Documentation of a living will before admit</td>
<td>117 (21.5%)</td>
</tr>
<tr>
<td>Type of insurance</td>
<td>Private 106 (18.5%), Medicare 282 (49.3%), Other Government 109 (19.1%), Other/none/unknown 75 (13.1%)</td>
</tr>
<tr>
<td>Postintervention</td>
<td>324 (56.5%)</td>
</tr>
</tbody>
</table>

Data presented as mean ± SD or n (%), unless otherwise indicated.

- Determined by first ICD-9 code listed; this reflects most reimbursable, not necessarily primary, diagnosis.
- As reported on death certificate using ICD-10 coding.
- Proportion of patients with medical record documentation of a living will (n = 367).
- Patients who died after implementation of the intervention to improve palliative care in the ICU (10–12).

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representative patient in our cohort who died from complications of chronic obstructive pulmonary disease (COPD) who would have preferred to die at home. Preventing the 6.5-day ICU admission with ACP would immediately save the hospital $6,200 in direct variable costs. Over time, if ICU bed occupancy decreased as a result of ACP and the alignment of patient preferences at the end of life with care received, the direct fixed costs could also be saved, adding on average, an additional $18,400 in savings to the hospital per patient (Table 3).

If this representative patient was admitted to the ICU and received ICU-based palliative care intervention of average effectiveness, the LOS could be reduced by an estimated 26%, or 1.7 days. In the short term, this would have led to $1,300 per patient in immediate direct variable cost savings for the hospital. If the palliative care intervention was widespread, in the long term, ceteris paribus, as bed occupancy rates decline, another $2,800 per patient in direct fixed costs may be saved (Table 3). It is important to note that these figures are ICU costs avoided and do not take into account the costs incurred through the alternative care received, whether at home or in the hospital. Thus, these figures represent the upper bound of potential cost saving.

The degree of savings is thus determined by the time horizon—short versus long term. The incentive, however, for hospitals to realize these savings varies depending on the reimbursement model with increasing incentive as we move from fee-for-service toward capitated payment models.

**Discussion**

Our findings demonstrated that (1) the first ICU day was the most expensive with the days in between admission and death having relatively stable costs; (2) this pattern was consistent across patients regardless of clinical service, insurance status, type of ICU, or cause of death; (3) direct variable costs accounted for ~20% of ICU costs; this percentage decreased over time; (4) direct fixed and indirect costs constituted ~45% and 35% of ICU costs, respectively, these percentages increased slightly over time; and (5) high total ICU costs were associated with a higher percentage of direct variable costs (represented primarily by supplies). To our knowledge, this is the first study evaluating the pattern and breakdown of ICU costs by day of stay for patients who died in the ICU, and our findings demonstrate the stability of the pattern across a diverse group of decedents.

Our finding that the first ICU day is the most expensive is consistent with most previous studies.\(^6,17,18\) The stability of costs in days between admission and death/discharge is similar to that observed in patients receiving mechanical ventilation in the ICU for >48 hours who survived to ICU discharge.\(^6\) Our study demonstrated that this pattern was consistent and applicable to a broad group of ICU decedents, across different ICUs and different clinical services. By contrast, a recent study did not see higher day 1 costs in patients admitted to medical/nonsurgical ICUs.\(^19\) This difference in findings may be due to severity of illness; ICU mortality was not reported in this study, making it difficult to determine if our cohorts are comparable.

One important implication of the stability of these cost patterns is that the aging population (and accompanying increase in Medicare coverage), and the concomitant increases in chronic comorbidities, will increase ICU costs, but they are
FIG. 2. Upper panel: ICU costs broken down by day of stay; Lower panel: Spine plot by day of stay, indicating relative fraction of cost categories ($n=572$).

FIG. 3. Results of regression analyses stratified by length of stay, underlying cause of death, insurance type, type of ICU, and clinical service. (A) Tests if, on average, costs are greater on admission day versus day 2; (B) tests if, on average, costs are stable after the second day.
Reducing ICU LOS is likely to decrease both direct variable and direct fixed costs. In the long term, when the majority of costs are fixed, prevention of unwanted ICU stays is a quality measure, hospital administration may be incentivized to integrate ACP and palliative care interventions to decrease ICU LOS, prevent unwanted ICU stays, and match care with patient wishes. In fact, ICU LOS has been proposed as a quality measure by the Joint Commission, strengthening the incentive for adoption within quality-based payment systems. Capitated payment systems and fixed global budgets, as recently passed in Maryland, provide a fixed budget per patient regardless of care required, providing even more financial incentives for hospitals to reduce overall costs with hospitals bearing more of the financial burden for costly patients.

Several prior studies have demonstrated reductions in overall hospital costs associated with inpatient palliative care services. One study also found that palliative care consultation was associated with reduced ICU costs; however, the peak of savings was achieved when the ICU admission was prevented altogether, leading to significant financial incentives for hospital administrators.

In our study, labor costs represented nearly 40% of total ICU costs and nearly the entire portion of direct fixed costs. As care providers are only responsible for costs when they work, this may provide a greater sense of urgency to reduce unwanted ICU admissions and LOS, especially in the short term when the majority of costs are fixed. However, our changing reimbursement systems provide stronger financial incentives for both administrators and physicians to decrease ICU usage since both bear some financial risk for costly episodes. However, both the size of the budget and the sharing of financial risk between physicians and hospitals will depend on contract negotiations. Under value-based performance, reimbursement is linked to improving quality and reducing costs. Thus, even in the short term when most ICU costs are fixed, but prevention of unwanted ICU stays is a quality measure, hospital administrators may be incentivized to integrate ACP and palliative care interventions to decrease ICU LOS, prevent unwanted ICU stays, and match care with patient wishes. In fact, ICU LOS has been proposed as a quality measure by the Joint Commission, strengthening the incentive for adoption within quality-based payment systems. Capitated payment systems and fixed global budgets, as recently passed in Maryland, provide a fixed budget per patient regardless of care required, providing even more financial incentives for hospitals to reduce overall costs with hospitals bearing more of the financial burden for costly patients.

Several prior studies have demonstrated reductions in overall hospital costs associated with inpatient palliative care services. One study also found that palliative care consultation was associated with reduced ICU costs; however, to our knowledge, no study to date has looked at the effect of palliative care and ACP on ICU costs in the short term and long term using direct variable, direct fixed, and indirect ICU costs. This study provides insight into what patterns of ICU cost look like for ICU decedents and potential savings that may be realized in the short and long term.

Our study has several limitations. First, we acknowledge that there is considerable variation in defining direct (variable and fixed) and indirect costs. In addition, this study was performed on a single institution and may not be generalizable to other healthcare settings. Future research is needed to confirm the findings and explore the potential for implementing similar interventions in other settings.
conducted in a single hospital and different hospitals may have a different fee structure for direct and indirect costs as well as different patterns of care. Additionally, this hospital was the site of a system-level intervention to improve palliative care in the ICU and thus estimates of cost reductions may be conservative. Second, our analyses do not include physician fees as these are generated from a separate organization and are unable to be broken down by day in the ICU; thus, our cost estimates are conservative. However, this study provides insights into the costs of terminal ICU care that can help guide future studies. Third, our study describes costs for diverse patients dying in the ICU and is not focused only on patients for whom palliative care interventions are appropriate. Nonetheless, these cost findings provide guidance for assessing the economic impact of implementing palliative care interventions on ICU costs. Fourth, we recognize that these findings do not provide information for conducting analyses from the societal perspective. Furthermore, the concept of cost shifting has not been factored in and thus these figures represent the maximum potential cost saving. Finally, data from this study were collected between 2003 and 2005 and should be replicated with more recent data. We did not see changes in quality of palliative care in the ICU between 2003 and 2008, but additional research should be conducted to ascertain if patterns of costs are changing. These findings have important implications for palliative and ICU care in the United States as we reduce volume-based fee-for-service reimbursement and shift toward accountable care organizations and value-based purchasing. Value in healthcare is key to controlling costs and improving quality. Most importantly, these estimates provide insight into the range of cost savings that may be realized with interventions such as ACP and palliative care that help to align care with outcomes desired by patients, such as dying outside of the hospital. Future research, identifying cost patterns and implications using additional institutions and more recent data, is needed to inform clinicians as well as healthcare administrators and policy makers. All the authors attest that they do not have any potential or actual personal or financial involvement with any company or organization with financial interest in the subject matter.

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Author Disclosure Statement

No competing financial interests exist.

References

Regression models:
In each group, we used the following regression model:

\[ E\{\log(\text{daily ICU cost}) | \text{day}, \text{death}\} = \beta_0 + \beta_1(\text{day} = 1) + \beta_2(\text{day} > 2) + \beta_3(\text{day} > 2 \text{ and death} = 1) + \beta_4(\text{day} > 2 \times \text{day}). \]

This model parameterizes an overall mean of log ICU costs on day 1 \((\beta_0 + \beta_1)\) and day 2 \((\beta_0)\) regardless of whether a subject died on that day. The model also uses a straight line with slope \(\beta_4\) to describe the trend in average log-costs after day two. Death days are cheaper on average, simply due to the fact that a full day is not spent in the ICU on that day. To account for this, we allow a separate intercept for death days by including \(\beta_3\).

To test whether costs on the first day are more expensive than the second, we test the null hypothesis \(H_0 : \exp(\beta_1) = 1\), noting \(\exp(\beta_1)\) may be interpreted as the ratio of geometric mean costs comparing day one to day two, with values greater than one indicating greater average costs on day one. The geometric mean is simply the exponentiated mean of the log-transformed data. The geometric mean is less sensitive to extreme cost values than the usual arithmetic mean and thus may be a better representation of the central tendency of costs.

In order to determine an appropriate test for determining whether costs are stable after the second day in the ICU, first note that \(\exp(\beta_4)\) can be interpreted as the per-day multiplicative change in average daily ICU costs. Thus, if costs were completely stable after day two on average, \(\exp(\beta_4)\) would equal one. Standard hypothesis tests would assess evidence against the null hypothesis \(H_0 : \exp(\beta_4) = 1\); however, a lack of evidence against this null hypothesis is not necessarily evidence in favor of it. A more appropriate procedure is an equivalence test that examines evidence against two one-sided null hypotheses, \(H_{01} : \exp(\beta_4) < l\) and \(H_{02} : \exp(\beta_4) > u\). Here, \(l \leq 1\) and \(u > 1\) are user-specified lower and upper bounds that together define a range of values for which costs may be claimed to be clinically equivalent. Rejecting these null hypotheses thus provides the desired statistical evidence that \(l \leq \exp(\beta_4) < u\). We set these to be 0.960 and 1.032, which would imply a 25% change in costs over a one-week time period; this can be seen by noting \(0.960^7 = 0.75\) and \(1.032^7 = 1.25\). That is, if, based on the slope of the line fit to average costs after day two, daily costs are predicted to have changed by less than 25% over a week’s time, we declare those costs to be clinically equivalent.