A Search for the Higgs Boson Produced in Association With Top Quarks in Multilepton Final States at Atlas

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A Search for the Higgs Boson Produced in Association With Top Quarks in Multilepton Final States at Atlas

Abstract
This thesis presents preliminary results of a search for Higgs boson production in association with top quarks in multilepton final states. The search was conducted in the 2012 dataset of proton-proton collisions delivered by the CERN Large Hadron Collider at a center-of-mass energy of 8 TeV and collected by the ATLAS experiment. The dataset corresponds to an integrated luminosity of 20.3 inverse femtobarns. The analysis is conducted by measuring event counts in signal regions distinguished by the number of leptons (2 same-sign, 3, and 4), jets and b-tagged jets present in the reconstructed events. The observed events in the signal regions constitute an excess over the expected number of background events. The results are evaluated using a frequentist statistical model. The observed exclusion upper limit at the 95% confidence level is 5.50 times the predicted Standard Model production cross section for Higgs production in association with top quarks. The fitted value of the ratio of the observed production rate to the expected Standard Model production rate is 2.83 $\pm$ 1.58 $\pm$ 1.35.

Degree Type
Dissertation

Degree Name
Doctor of Philosophy (PhD)

Graduate Group
Physics & Astronomy

First Advisor
Ira J. Kroll

Keywords
Associated Production, ATLAS, Higgs, LHC, Top Quarks

This dissertation is available at ScholarlyCommons: http://repository.upenn.edu/edissertations/1083
A Search for the Higgs boson produced in association with top quarks in multilepton final states at ATLAS

Chris Lester

A dissertation
in
Physics and Astronomy

Presented to the Faculties of The University of Pennsylvania
in Partial Fulfillment of the Requirements for the Degree of Doctor of Philosophy
2015

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A Search for the Higgs boson produced in association with top quarks in multilepton final states at ATLAS

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Acknowledgements

Thanks to Joe, for his friendship and his insight. Thanks to the Penn graduate students and postdocs, for the treasured memories. Thanks to my mother-in-law, for her support and enthusiasm. Thanks to Zoë, for everything.

This thesis is dedicated to my parents, who have always been there and constantly encouraged and expected the best from of me. They are behind all of my accomplishments.
ABSTRACT

A SEARCH FOR THE HIGGS BOSON PRODUCED IN ASSOCIATION WITH TOP QUARKS IN MULTILEPTON FINAL STATES AT ATLAS

Chris Lester

Joseph Kroll

This thesis presents preliminary results of a search for Higgs boson production in association with top quarks in multilepton final states. The search was conducted in the 2012 dataset of $\sqrt{s} = 8$ TeV proton-proton collisions delivered by the CERN Large Hadron Collider and collected by the ATLAS experiment. The dataset corresponds to an integrated luminosity of 20.3 fb$^{-1}$. The analysis is conducted by measuring event counts in signal regions distinguished by the number of leptons (2 same-sign, 3, and 4), jets and b-tagged jets present in the reconstructed events. The observed events in the signal regions constitute a small excess over the expected number of background events. The results are evaluated using a frequentist statistical model. The observed exclusion upper limit at the 95% confidence level is 5.50 times the predicted Standard Model $t\bar{t}H$ production cross section. The fitted value of the ratio of the observed production rate to the expected Standard Model $t\bar{t}H$ production rate is $2.83^{+1.58}_{-1.35}$. 

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Preface

This analysis represents only the last year of work of my graduate career and was accomplished as part of a ~ 10 person team. I was involved in some way at every level of the analysis, but for some parts I had a more important role. I led the team that managed the datasets and analysis coding infrastructure, developed the techniques for estimating the fake and vector-boson backgrounds and optimized the selection for the 3 lepton signal region. I also directly supervised the work of multiple students, each of which performed a critical task for the analysis: measurement of the isolation selection efficiency for leptons, assessment of the impact of the experimental systematic uncertainties on the analysis and development of the 4 lepton signal region.

Earlier in my graduate career, I focused primarily on performance work for the ATLAS experiment. In 2010 I helped create an in-situ mapping of the inner detector material using photon conversions. As a part of small Penn-led team, I developed the electron identification algorithms that formed the basis of the primary electron trigger for the 2011 and 2012 runs and are used by many ATLAS analyses. Electrons are critical pieces of analyses at hadron colliders but also are challenging to understand due to large and diverse backgrounds. Our team oversaw the development of electron identification from very basic cut-based roots to the extremely robust and high performing multi-variate algorithms used in this thesis. We managed this at a time when the running conditions were changed rapidly. Later, I pushed
for the proper measurement of electron identification efficiency at lower energies that were important for finding Higgs signals in a number of channels.

Before the $t\bar{t}H$ analysis, I worked on two additional analysis projects. The first was a search for the Higgs in the $W^+W^-$ decay channel. For this analysis I played a small role as the coordinator for non-$W^+W^-$ di-boson background measurements. The second was a search I explored for the Higgs in the $W^\pm H$ production mode with same-sign dileptons. As many things in science, this ended up being a dead-end: a difficult analysis without compelling sensitivity.

I had the privilege and luck of being part of some truly amazing research at a very important time in the field. While experimental particle physics is a collaborative effort, I can look at my small set of accomplishments with pride in the fact that they helped contribute to the overall success of the experiment and to push our fundamental understanding of the universe the tiniest bit forward.

Chris Lester
CERN, Fall 2014
Chapter 1

Introduction

The discovery of the Higgs boson at the Large Hadron Collider (LHC) experiments has opened up a new paradigm of research into the Standard Model of particle physics. This thesis primarily documents a search for the production of Higgs boson in association with top quarks \((t\bar{t}H)\) in multi-lepton final states. Searching for this production mode of the Higgs is an important step toward a precise measurement of the top Yukawa coupling, because it accesses this coupling via diagrams that do not contain loops. Comparison of this coupling with the already well-measured top quark mass provides a direct test of a fundamental provision of the Higgs mechanism: that it gives mass to the fermions.

The analysis uses the 2012 ATLAS experiment’s dataset of proton-proton collisions at a center-of-mass energy of 8 TeV provided by the LHC. The statistics available do not allow for an observation of the \(t\bar{t}H\) process at the Standard Model production cross-section, and the results of the search are interpreted as a 95% exclusion on the production rate. The results will provide some of strictest constraints on the rate to date and establish a program for future analyses on larger datasets that will eventually observe this production mode.

Chapter 2 provides theoretical background and motivation for the study of this particular Higgs production mode and Chapter 3 provides a basic review of the experimental apparatus, the LHC and ATLAS. Chapter 4 is a brief diversion from the main text to elaborate on the
1. **Introduction**

Techniques used to identify electrons and measure their identification efficiency.

Chapters 5-10 are the main text, which discuss the full analysis procedure for the search and the final measurement. The results of the analysis have been approved by the ATLAS collaboration and eventually will be documented for publication. They will eventually be combined with other Higgs searches to set limits on Higgs couplings to other SM particles, particularly the top quark.
CHAPTER 2

Theoretical Background

The Standard Model of particle physics (SM) is an extraordinarily successful description of the fundamental constituents of matter and their interactions. Many experiments have verified the extremely precise prediction of the SM. This success has culminated most recently in the discovery of the Higgs Boson. This chapter provides a brief introduction to the structure of the SM and how scientists are able to test it using hadron colliders. It focuses primarily on the physics of the Higgs boson and its decay to top quarks. I stress the importance of a measurement of the rate at which Higgs Bosons are produced in association of top quarks, as a new, rigorous test of the SM. The experimental search for this production mode in multi-lepton final states is the general subject of this thesis.

2.1 The Standard Model

2.1.1 The Standard Model Structure

The Standard Model (SM) [1, 2, 3, 4] is an example of a quantum field theory that describes the interactions of all of the known fundamental particles. Particles are understood to be excitations of the more fundamental object of the theory, the field. The dynamics and interactions of the fields are derived from the Standard Model Lagrangian, which is constructed
2. Theoretical Background

to be symmetric under transformations of the group $SU(3) \times SU(2)_L \times U(1)$. $SU(3)$ is the group for the color, $SU(2)_L$ is the group for weak iso spin, and $U(1)$ is the group for weak hyper-charge.

Demanding these symmetries be local, gauge symmetries allows the theory to be renormalizable [5], meaning that unwanted infinities can be absorbed into observables from theory in a way that allows the theory to be able to predict physics at multiple energy scales. Gauging the symmetries results in the introduction of 8 massless gluons, or the boson\(^1\) carriers of the strong force [6] from the 8 generators of the $SU(3)$ symmetry, and the 4 massless bosons, carriers for the weak and electromagnetic forces from the 3 generators of the $SU(2)$ and 1 generator of the $U(1)$ group. The weak and the electromagnetic forces are considered part of a larger single unified electroweak group $SU(2) \times U(1)$ and the associated generators mix.

Matter particles are half-integer spin fermions and are representations of the symmetry groups. Singlets of the $SU(3)$ are called leptons, do not have a color charge, and, therefore, do not interact with the strong force. Quarks, as triplets of the $SU(3)$ group, do interact with the strong force. The SM is a chiral theory: the weak force violates parity, as it only couples to right-chiral particles or left-chiral anti-particles. This means that right-chiral and left-chiral fermions arise from different fields, which are different representations of the $SU(2)_L$ group.

The discovery of particles and new interactions in various experiments is intertwined with the development of the theory that spans many decades and is not discussed in detail here. But these experiments have proven the above model and symmetries to be an overwhelming success. So far, 3 separate generations of both quarks and leptons have been discovered, differing only by mass. The reason for this 3-fold replication is not known. The gluons and

\(^{1}\text{bosons are full integer spin particles that obey Bose-Einstein statistics, while fermions are half-integer spin particles that obey Fermi-Dirac statistics}\)
the 4 electroweak bosons have also been discovered ($W^+$, $W^-$, $Z^0$, and $\gamma$). Figure 2.1 shows a table of the known SM particle content.

2.1.2 Electroweak Symmetry Breaking and the Higgs

Despite the simple structure of theory, the discovery of massive fundamental particles creates two sets of problems both related to $SU(2)_L \times U(1)$ symmetry. First, the force-carrying bosons must enter the theory without mass or the symmetries will be explicitly broken in the Lagrangian. Second, adding fermion masses to theory in an ad-hoc way allows the right-chiral and left-chiral fermions to mix. Since they possess different quantum numbers, as different representations of the weak-isospin group, this too breaks gauge invariance.

To solve these problems, spontaneous electro-weak symmetry breaking (EWSB) is intro-
2. Theoretical Background

duced via the Brout-Englert-Higgs mechanism [7, 8, 9]. A massive scalar field in an electro-
weak doublet is added to the theory with 4 new degrees of freedom and a potential which
includes a quartic self-interaction term. Each fermion field interacts with the scalar field via
a different Yukawa coupling, which unites the left and right chiral fields of a single particle
type. This field explicitly preserves all of the symmetries, but the minimum of the potential
does not occur when the expectation of the field is zero. The field eventually falls to a state,
where it acquires a non-zero vacuum-expectation value. A non-vanishing field must point in
a particular direction of weak-isospin space, breaking the symmetry.

The consequences of this spontaneous symmetry breaking are tremendous. The universe
is filled with a field that has a non-zero expectation value. The theory can be expanded
around this new value and 3 of the degrees of freedom can be interpreted as the longitudinal
polarizations of the now massive $W^+$, $W^−$, and $Z^0$, while the 4th remains a scalar field,
called the Higgs field with an associated particle called the Higgs particle or ‘Higgs’. The
weak bosons acquire a mass via their longitudinal polarizations and the Yukawa couplings of
the scalar field to the fermions now behave like a mass term at this new minimum.

2.1.3 The Standard Model Parameters

Confronting the SM with experiment requires the measurement of $17^2$ free parameters, which
are unconstrained from the theory. These free parameters include the fermion masses from the
Yukawa couplings, the force coupling constants, the angles and phase of the mixing between
quarks, and constants from the Higgs and electroweak sector$^3$.

$^2$There are additional parameters from neutrino mass terms and mixing but it is unclear how to include
these into the Standard Model, since it does not predict right-chiral neutrinos that would not interact via any
force

$^3$ The electroweak sector includes parameters like mass of the $W^±$ and $Z^0$ bosons, the weak mixing
angle,$\sin^2\theta_w$, the fermi constant $G_F$, and Higgs Mass and vacuum expectation value. These parameters
however are not wholly independent. As discussed above, it is only necessary theoretically to specify the two
parameters relevant to the Higgs potential and the two coupling associated with the gauge groups
2. **Theoretical Background**

Experiments have provided a number of measurements of the parameters of the SM\[10\]. With the discovery of the Higgs boson and the measurement of the Higgs mass, all of the parameters of the SM can be estimated and statistical procedures can assess the relative agreement of overlapping measurements to test the self-consistency of the SM. The GFitter collaboration assembles all relevant electroweak observable measurements into a statistical model and then allows certain measurements to float within their uncertainty to allow for a fit among multiple correlated measurements\[11\]. These correlations arise for two reasons. First, measurements are made that often depend on multiple SM parameters. Second, radiative corrections often cause parameters to depend on each other. For instance, the Higgs mass is sensitive to both the $W$ mass and top mass, through loop level corrections.

Figure 2.2 shows the fitted constraints on 4 key SM parameters ($M_H$, $M_W$, $M_t$, $\sin^2\theta_W$) with actual measurements overlaid. The plots show both the removal and inclusion in the fit of key measurements to assess their overall impact. The addition to the fit of the measured Higgs mass from the ATLAS and CMS collaborations creates a small tension, as the other observables prefer the mass to be much lower ($\sim 80$ GeV). This tension in the combined electroweak fit as a result is not statistically significant with a $p$-value of 0.07. The SM seems to be self-consistent.

### 2.2 Collider Physics and the Higgs

To test the theory, physicists accelerate particles to extremely high energies and force them to interact through collisions. Typically, the particles accelerated are electrons or protons, since they are stable. Electron-positron collider machines have a rich history of discovery and measurement in particle physics. The advantage of electron accelerators is that the colliding element is itself a fundamental particle. However, due to synchrotron radiation, the curvature
of the beam line becomes problematic for high energy beams. On the other hand, proton-proton and proton-anti-proton colliders can be accelerated in rings without large losses due to synchrotron radiation, but the actual colliding objects at high energies are the constituent quarks and gluons. This complicates analysis because the initial state of the hard-scattering system is not known on a per-collision basis and the momentum of hard-scattering system is unknown along the beam direction.

For hadron colliders, physicists must rely on form-factor descriptions of the colliding hadrons that describe the fraction of momentum carried by the hadrons constituent ‘partons’. These are called parton distribution functions (PDF), seen in Figure 2.3, and are factorized and integrated through the theoretical calculations of various collision processes [12].
2. Theoretical Background

At the Large Hadron Collider (LHC) protons are collided. The types of initial hard-scattering states at the LHC are quark-quark, quark-gluon, and gluon-gluon. Gluon collisions dominate overall, due to the large number of gluons inside the proton, though the relative importance of different initial states changes with the energy scale of the collision and the type of final state selected.

A prime motivation for the construction of the Large Hadron Collider was the discovery or exclusion of the Higgs boson\(^\text{[13]}\). LEP and the Tevatron excluded large swaths of possible Higgs boson masses, especially below 114 GeV. The Higgs mass was also known to have a theoretically motivated upper bound. The unitarity of diagrams including the WWWWWW vertex required the Higgs mass to be below about 1 TeV. The LHC was designed to be able to eventually find or exclude a Higgs particle in this range \(^\text{[10]}\).

Reaching this discovery or exclusion required an enormous dataset with collisions at high energies. Despite the fact that the Higgs couples to nearly every particle, Higgs boson pro-

Figure 2.3: Proton Parton Distribution Functions (PDFs) from the MSTW Collaboration at \(Q^2 = 10\) GeV\(^2\) and \(Q^2 = 10^4\) GeV\(^2\).
2. Theoretical Background

Production at the LHC is a low rate process. Because it couples to fermions proportional to mass and because the colliding particles must be stable and therefore light, production of the Higgs must occur through virtual states.

The Higgs boson can be produced through collision at the LHC via 4 mechanisms: gluon-fusion (ggF), vector-boson fusion (VBF), Higgsstrahlung (VH), and production in association with top quarks ($t\bar{t}H$). The diagrams are shown in Figure 2.4 and the production cross-sections as a function of Higgs mass for the 8 TeV LHC proton-proton running are shown in Figure 2.5 [14]. The largest production cross-section is via the gluon fusion channel at 20 pb, which proceeds through a fermion loop that is dominated by the top quark, because of its large Yukawa coupling to the Higgs. Because the Higgs couples to every massive particle, it has a rich set of decays also seen in Figure 2.5, especially for $m_H = 125$ GeV. Studies of Higgs properties at hadron colliders offers many tests of the Standard Model and ample room for new physics searches. These tests specifically can verify the link between Yukawa coupling and the particles mass and further constrain details of EWSB by examining Higgs coupling.

![Figure 2.4: Dominant Higgs production modes at the LHC](image-url)
2. Theoretical Background

Figure 2.5: 8 TeV LHC Higgs production cross-sections (left) and decay branching fractions.

to the weak bosons.

2.2.1 Higgs Discovery at the LHC

In 2012 both ATLAS and CMS announced the discovery of a new boson consistent with the Higgs by examining the results of Higgs searches in a number of decay channels ($H \rightarrow W^+W^-$, $H \rightarrow Z^0Z^0$, and $H \rightarrow \gamma\gamma$) in the 2011 dataset at $\sqrt{s}=$ 7 TeV and part of the 2012 dataset at $\sqrt{s}=$ 8 TeV. By 2013 and 2014, both experiments have updated and/or finalized their results for the full 2011 and 2012 datasets [15, 16]. I will focus on the ATLAS results that measured both the Higgs mass[17] and spin[18] and provided initial constraints of the Higgs couplings to different particles.

Figure 2.6 show the results of the searches in all of the measurement channels as well as constraints on the SM Higgs coupling parameters in an example fit, where the couplings to the top-quark, bottom-quark, W,Z, and $\tau$ are allowed to fluctuate independently. These rely on measurements binned in different production and decay channels. They are dominated by higher statistics results in the gluon-fusion production modes, but measurements in the VH
2. Theoretical Background

![ATLAS Preliminary Figure 2.6](image)

Figure 2.6: ATLAS Higgs combination results for all SM measurement channels as ratios of the measured to SM production cross-sections (left) and extracted Higgs coupling constraint scale-factors for a combined fit to the measurement channels, where the W, Z, top-quark, b-quark, and τ couplings are allowed to float. The p-value of this particular model is 0.13 and in agreement with SM expectations

and VBF modes are close to SM sensitivity.

The combined results show basic agreement with the SM with much room for improvement with the addition of new production and decay modes and higher statistics. The coupling constraints are particularly strong for the W and Z, which are the most sensitive decay channels, and top quark due to the dominance of the top Yukawa in the ggF loop.

2.2.2 The Importance $t\bar{t}H$ Production

Notably absent thus far in the SM are searches for the Higgs in the $t\bar{t}H$ production channel, due to the low production rate and lack of statistics. Searches are underway and initial results are close to SM sensitivity for ATLAS and CMS.

Measuring the $t\bar{t}H$ production rate is important, because $t\bar{t}H$ production depends on the
2. Theoretical Background

The top Yukawa coupling at tree level. Comparing the predicted Yukawa coupling from top mass measurements to the coupling from the wholly independent Higgs production measurements is a very direct test of the Higgs’ involvement in providing mass for the fermions in the SM.

The top Yukawa coupling is already constrained from current measurements of the ggF production process, since the ggF loop is dominated by top quarks. However, new, colored particles could be present in the loop. Comparison of the gluon-fusion and the $t\bar{t}H$ modes would allow for disentangling the effects of these possible new particles\cite{19}. The simplest of new physics models, allowing for the modification of the ggF loop, introduce a new generation of quarks. However, fourth generation quarks, which obtain mass from a Higgs Yukawa coupling, are already largely excluded due to their enormous effects on the Higgs production cross-section\cite{20}. Other exotic scenarios allow for new colored particles, which are not entirely constrained by present measurements\cite{21, 22, 23}. These include, for instance, supersymmetric models involving the stop quark.

With the level of statistics available in Run I dataset, very strict constraints on the top Yukawa coupling are simply not possible and the measurement presented in this thesis is a first step. Future, high-statistics datasets will have the ability to provide better measurements and $t\bar{t}H$ production will become very important. Despite similar uncertainties on the overall production cross-sections for $t\bar{t}H$ and the ggF, $t\bar{t}H$ has the advantage that most of these uncertainties would cancel for $t\bar{t}H$ if normalized to the topologically similar $t\bar{t}Z$. Finally, the uniqueness of the experimental signature means that searches for $t\bar{t}H$ signatures can be performed for a variety of Higgs decays ($\gamma\gamma$, $b\bar{b}$, $WW, ZZ$, and $\tau\tau$) with roughly similar degrees of sensitivity (within a factor of 10)\cite{19}.

It is important to note the importance of the top Yukawa coupling due to its enormous size compared to other couplings. For instance, given the measured top and bottom masses, the top Yukawa coupling is roughly 30 times the bottom Yukawa coupling, the next largest.
2. Theoretical Background

Figure 2.7: RGE for the running of the SM parameter, $\lambda$ for the Higgs self-coupling term with present values and uncertainty bands for $M_H$ and $M_t$ (left). The two-dimensional plot colored (right) shows regions for which the SM is stable, unstable and metastable based on this RGE.

The top Yukawa coupling, along with the Higgs mass, is one of the most important pieces of the renormalization group equations (RGE) responsible for the running of the parameter that determines the Higgs self-coupling $\lambda$. If this parameter runs negative, then the potential responsible for the entire mechanism of EWSB no longer has a minimum and becomes unbounded, resulting in instability in the universe [24]. Metastability occurs when the shape of the potential allows for a false local minimum. Figure 2.7 shows the running of this parameter, the regions for which the universe is stable, unstable and metastable. Current measurements suggest that universe lies in a metastable island\(^4\). This is a sort of fanciful aside, intended only to highlight the importance of the top Yukawa coupling and to suggest that new discoveries in the top-Higgs sector have far reaching consequences.

\(^4\)The RGE assumed that there is no new physics at all energy scales
2. Theoretical Background

2.3 Conclusion

The Standard Model, despite its success in providing a unified description of fundamental particles and interactions into single theory, has its flaws. These have been discussed in depth elsewhere, but include issues like the description of massive neutrinos, the failure to include gravity, and the unnaturalness of large quantum corrections to Higgs parameters. For these reasons, it seems the SM might be a lower energy approximation to a more fundamental theory. The discovery of the Higgs boson at the LHC provided a stunning verification of one of the fundamental aspects of the theory but at the same time offers new area to search for glimpses of something more fundamental. The production of samples of Higgs bosons allows for a rich array of new tests of the Standard Model, which is now finally over-constrained by experiment. Searches for the $t\bar{t}H$ production, one category of which is the topic of this thesis, provide tree-level access to a central parameter of the theory, the top Yukawa coupling, as well as access a variety of Higgs decays, which will eventually provide a rigorous new test of the SM.
Chapter 3

The Large Hadron Collider and the ATLAS Experiment

3.1 The Large Hadron Collider

Production of a sufficient number of high energy collisions to adequately explore the physics of electro-weak symmetry breaking required the development of one of the most complex machines ever built, the Large Hadron Collider or LHC.

The LHC is the world’s highest energy particle accelerator and is located 100m underneath the French-Swiss border at the European Organization for Nuclear Research (CERN) in a 26.7 km tunnel. The technology involved in the development of the LHC is an enormous achievement in its own right and is documented in detail here [25, 26, 27]. The LHC is a circular machine capable of accelerating beams of protons and colliding them at center of mass energies up to $\sqrt{s} = 14$ TeV at 4 collision sites around the ring, where 4 experiments are housed (ATLAS[28], CMS[29], LHCb[30], and ALICE[31]). Figure 3.1 is a diagram of the layout of the LHC and its experiments[32]. The LHC also operates in a mode with beams of heavy ions. The LHC is composed of thousands of super-conducting Niobium-Titantium magnets, cooled to 1.9 K with liquid Helium, which steer and focus the particle beams, and superconducting resonant-frequency (RF) cavities, which boost the beam to higher energies.
3. The Large Hadron Collider and the ATLAS Experiment

3.1.1 The Accelerator Complex

The accelerator complex is a progressive series of machines with the LHC as the final stage. Protons are obtained from hydrogen atoms and are accelerated to 50 MeV using the Linac2, a linear accelerator, before being injected into the Proton-Synchrotron Booster (PSB). In
3. The Large Hadron Collider and the ATLAS Experiment

the PSB the protons are accelerated to energies of 1.4 GeV for injection in to the Proton-Synchrotron (PS). The PS accelerates the protons to 25 GeV and dumps bunches into the Super Proton Synchrotron (SPS), where they are accelerated to 450 GeV and finally dumped into the LHC for full acceleration. The PS and SPS are circular accelerators that were important in past physics discoveries and have been re-purposed for use in the LHC complex.

3.1.2 Beam Parameters and Collisions

For the physics studied at the ATLAS experiment, the two most important parameters of the collisions are the center of mass energy (CME) and instantaneous luminosity ($\mathcal{L}$). High center of mass energies are necessary for the production of new high mass particles, and, because the constituents of the actual collisions are the partons of the proton, the CME of the collisions must in general be much higher than the mass of the particles produced.

The instantaneous luminosity of the collisions is a measure of the collision rate. The integrated luminosity over time is a measure of the size of the dataset and when multiplied by the cross-section of a particular process gives the total number of expected events produced for that process. Instantaneous luminosity depends on the number of colliding bunches of protons, the intensity of those bunches, the revolution frequency, and the normalized transverse spread of the beam in momentum and position phase space, called the emittance, and the transverse beam size. The LHC has the option for colliding beams with 2808 bunches of protons, each with around $10^{11}$ protons, at a rate of one bunch collision every 25 ns, or 40 MHz. These parameters correspond to a design luminosity of around $10^{34}$ cm$^2$ s$^{-1}$ or $10$ nb$^{-1}$ s$^{-1}$, equivalent to 1 Higgs every 5 seconds. For various reasons, the bunch collision rate was help at 20 MHz for the 2011 and 2012 runs.
3. The Large Hadron Collider and the ATLAS Experiment

3.2 The ATLAS Experiment

This section provides a brief overview of the ATLAS experiment. The ATLAS detector is centered on one of the LHC collisions points, located 100 m underground. Through the combination of a number of subsystems, it is designed to identify the particles arising from these collisions, measure the energy and momentum of these particles, and make fast decisions about the content of each collision, in order to save a small fraction of measured collision events for offline study.

ATLAS, shown in Figure 3.2, possesses cylindrical symmetry around the beam pipe. It weighs 7000 tons, has a diameter of roughly 25 m and length of 46 m. ATLAS was designed to be a multi-purpose hermetic, particle detector, able to identify many types of particles, and designed to provide a snapshot of the entire collision event. The detector sub-systems form concentric rings around the beam-line at increasing distance. From closest to the beam outward, they are:

- **Inner Detector**: The inner detector (ID)\[^{33, 34}\] is immersed in a solenoidal magnetic field\[^{35}\] and provides measurements of charge particle tracks, through three subsystems: the Pixel Detector\[^{36, 37}\], the Semi-Conductor Tracker (SCT)\[^{38, 39}\], and Transition Radiation Tracker (TRT) \[^{40, 41, 42}\].

- **Calorimeter**: The calorimeters measure the energy of particles that participate in the electromagnetic (photons, electrons) and hadronic interactions (pions, protons, neutrons, etc.), by forcing them to shower in dense material. The hermeticity of the calorimeters allows for missing transverse energy measurements. The calorimeter is composed of the liquid argon electromagnetic calorimeter (LAr)\[^{43}\], the hadronic tile calorimeter\[^{44}\], the liquid argon hadronic endcap calorimeter, and the forward calorimeters.
3. The Large Hadron Collider and the ATLAS Experiment

Figure 3.2: Diagram of the ATLAS detector and subsystems

- **Muon Spectrometer:** The muon spectrometer (MS) sub-systems[45] form the outermost detector systems and measure the momentum of minimum ionizing muon tracks, as all other particles are stopped by the calorimeters. The muon systems are immersed in a toroidal magnetic field [35] and are composed of 4 different sub-systems for triggering and tracking measurements [46, 47, 48].

- **Triggering Systems:** The trigger and data acquisition systems[49, 50] read out data from the detector through a three-tiered hardware and software decision making framework to record the most interesting physical processes for a broad physics analysis program.

These systems are discussed in depth in the following sections.
3. The Large Hadron Collider and the ATLAS Experiment

3.2.1 Detector Coordinate System

ATLAS uses a right-handed coordinate system centered at the nominal proton interaction point. The beam line defines the \( z \)-axis. The \( x - y \) plane is perpendicular to the beam line and is referred to as the transverse plane. The transverse plane holds special significance in reporting measurements, because the initial momentum of the hard collision system is 0 along the transverse plane in the laboratory rest frame. Particle momenta measured along the transverse plane is called transverse momenta, and labeled \( p_T \). The momentum of the colliding proton-proton system is also 0 along the \( z \)-axis but the colliding partons may have vastly different momenta. Thus, momentum of the hard colliding system along the \( z \)-axis differs collision to collision.

Because ATLAS possesses a rough cylindrical symmetry, cylindrical and polar coordinates are used to describe particle trajectories and detector positions. The radial coordinate, \( R \), describes transverse distances from the beam line. An azimuthal angle, \( \phi \), describes angles around the \( z \)-axis, and a polar coordinate, \( \theta \), describes angles away from the \( z \)-axis. The polar angle is often expressed in terms of pseudo-rapidity, defined as \( \eta = -\ln(\tan(\theta/2)) \).

Distances in \( \eta - \phi \) space are often used to describe the proximity of objects in the detector, \( \Delta R = \sqrt{\eta^2 + \phi^2} \).

The ‘barrel’ and ‘endcap’ are classifications that are used to label the position of sub-detectors. Barrel sub-detectors occupy positions more central to the detector at \( |\eta| \) values roughly less than 1-2, while the endcap calorimeters extend farther in \( |\eta| \). The barrel-endcap transition region contains detector services. Also, the orientation of the detector elements are often different in the barrel and endcap to have optimal particle flux.
3. The Large Hadron Collider and the ATLAS Experiment

Figure 3.3: Diagram of the ATLAS ID in the $R-\phi$ plane showing the barrel view of the Pixel Detector, SCT, and TRT.

3.2.2 The Inner Detector

The ID makes measurements of the position of charged particles as they move through the detectors 3 sub-systems (Pixel Detector, SCT, TRT). The individual position measurements can be strung together to form a particle track. The entire ID is immersed in a 2T solenoidal magnetic field allowing for measurements of particle momenta through the curvature of the tracks. The ID is contained with a radius of 1.15 m and has a total length of 7m, allowing for particle tracking out to $|\eta| < 2.5$. Figures 3.3 and 3.4 show the placement of the ID sub-systems in the $R-\phi$ and $R-z$ planes.

The Pixel Detector has 80 million silicon read out channels (pixels) and is closest to the
interaction point with the finest granularity. As charged particles traverse the silicon, they create electron-hole pairs, which are subsequently pulled apart in an electric field and can be captured and registered as a current pulse. The detector has three concentric layers of pixels in the barrel (to \( |\eta| < 1.9 \)) and three endcap disks on each side of the barrel (to \( |\eta| < 2.5 \)). The closest barrel layer to the beam pipe is called the b-layer. The pixels provide excellent hit resolution (\( R - \phi \) accuracy of 10 \( \mu \)m and \( z \) (\( R \)) accuracy of 115 \( \mu \)m in the barrel (endcap)).

The SCT uses similar silicon technology to the pixels, but the each SCT layer contains a double layer of silicon strips, which are much longer in length than width. The SCT has 4 million read out channels and is arranged in 4 barrel layers and 9 endcap layers with coverage to \( |\eta| < 2.5 \). The double layers are inclined slightly with respect to each other so that these 1D sensors have 2D resolution for coincident hits. The resolutions are 580 \( \mu \)m in \( z \) (\( R \)) for the barrel (endcap) and 17 \( \mu \)m in \( R - \phi \).

The TRT is comprised of straw drift tubes filled with a gas mixture, containing mostly Xenon gas. Particles traversing the straws ionize the gas, and the liberated electrons drift to a wire at the center of the straw, which has an applied voltage, and induce an signal on the
wire. The TRT has \( \sim 300,000 \) straws. The barrel straws are arranged cylindrically along the 
\( z \) direction out to \( \sim |\eta| < 1 \) and the endcap straws point radially outward in the \( R \) direction. 
For this reason, the barrel (endcap) straws provide no measurement in the \( R \) (\( z \)) directions. 
The drift tubes provide individual position measurements with resolutions of \( \sim 130 \mu m \). Each 
particle track has on average 35 hits, which is large compared to the Pixel and SCT tracks, 
which have on average 7 hits.

The TRT is unique in that it also provides particle identification measurements via trans-

tion radiation. Charged particles emit transition radiation when traversing a boundary 
between materials of different dielectric constants. The volume between the straws is filled 
with a radiator material, a polymer foil or foam, to provide this boundary condition. Trans-
iton radiation photons are emitted in the direction of the particle trajectory in the keV 
range and cause a much larger signal amplitude within the straw. Hits that cause a signal 
at a higher threshold are thus indicative of transition radiation. The probability for emission 
transition radiation depends on the relativistic \( \gamma \) of the traversing particle. Because electrons 
are much lighter than any other charged particle, their \( \gamma \)-factors tend to be high enough to 
induce transition radiations, as opposed to pions, muons and other particles.

Combined tracking of particles through the 3 sub-detectors results in track momentum 
measurements from 500 MeV, the minimum energy need to leave the ID due to the magnetic 
field, to a few TeV. The track \( p_T \) resolution is roughly \( 0.05\% \cdot p_T \oplus 1\% \).

3.2.3 The Calorimeter

The ATLAS calorimeters measure the energy of electrons, photons and hadrons with \( |\eta| < 4.5 \). 
They induce a particle shower via electro-magnetic and nuclear interactions with the detector 
material and are deep enough to ensure that all or most of the shower energy remains con-
tained. Exceptionally, muons pass through the ATLAS calorimeters leaving relatively little
energy behind. ATLAS calorimeters are sampling calorimeters meaning that the active material of the detector only measures a small fraction of the energy produced by the shower. The overall shower energy is inferred from this fractional measurement. The rest of the material is inactive, dense material, designed to induce showers. The calorimetry system is grossly divided longitudinally (radially) into electro-magnetic (EM) and then hadronic segments, operated with different technologies. Figure 3.5 diagrams the layout of the calorimeter system.

The EM calorimeter (LAr), which is located directly outside of the solenoid magnet but within the same cryostat, has a accordion design with lead absorber and liquid argon active material. The accordion design ensures uniform coverage in $\phi$. The barrel and endcap LAr extend to $|\eta| < 2.47$. The LAr provides highly granular measurements in $\eta - \phi$ with 4 longitudinal segments, totaling $\sim 25$-35 radiation lengths with the exception of the barrel/endcap transition region ($1.37 < |\eta| < 1.52$). The geometry of the barrel LAr calorimeter can be seen in Figure 3.6. The first longitudinal segment is called the pre-sampler, composed of a thin
3. The Large Hadron Collider and the ATLAS Experiment

layer of active liquid argon, designed to detect early particle showers. The second segment is the most highly granular segment called the 'strips', as it is composed of thin liquid argon cells. The strips have a size of 0.025/8 x 0.1 in $\eta - \phi$ in the barrel with similar sizes in the endcap and are designed to be able to resolve single and double particle showers. This resolution is particularly useful in distinguishing $\pi^0 \rightarrow \gamma\gamma$ signatures from electron and photon signatures. The bulk of the radiation lengths and therefore the primary energy measurement come from the the third layer\(^5\). Each cell in this layer is 0.025 x 0.025 in $\eta - \phi$. The final layer is coarser, thinner and designed to estimate energy leaking out of the EM calorimeter. The forward EM calorimeters extend the $\eta$ range and use the same technology, but are not used in this analysis. The energy resolution of the EM calorimeters is $\sigma_E/E = 10%/\sqrt{E} \oplus 0.7\%$, measured in test beam data and confirmed in collision data.

The hadronic calorimeter is located directly behind the EM calorimeter. It is composed of tiles of iron absorber and plastic scintillator in the barrel ($|\eta| < 1.6$), called the TileCal, and copper-liquid argon in the endcap ($1.5 < |\eta| < 3.2$), called the HEC. The calorimeters contain ~10-19 hadronic interactions lengths with multiple longitudinal segments to contain showers induced by the nuclear interaction of hadronic particles. The energy resolution of the hadronic calorimeters is $\sigma_E/E = 50%/\sqrt{E} \oplus 3\%$. The intrinsic resolution of hadron calorimeters is much worse than electro-magnetic calorimeters, because much of the energy is lost to the inelasticity of nuclear break-up.

3.2.4 The Muon Spectrometer

The MS measures the trajectory of particles outside of the calorimeters, using multiple different technologies. Generally, all charged particles except for muons are stopped by the calorimeter, and therefore the majority of particles in the MS are muons, with the exception

\(^5\)this layer is actually called 'layer 2', since the pre-sampler is referred to as 'layer 0'
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Figure 3.6: Diagram of the ATLAS LAr EM calorimeter showing the longitudinal segmentation and the $\eta - \phi$ cells for the central barrel region

of rare cases of hadronic punch-through. Particle momentum spectroscopy is made possible by an air-core toroidal magnet system, embedded in the barrel MS ($|\eta| < 1.4$), and two smaller end cap toroids that provide fields out to $|\eta| < 2.7$.

In the barrel region, the muon chambers are arranged in three cylindrical layers around the beam, while in the endcap-regions the layers are arranged perpendicular to the beam in wheels. The arrangement is depicted in Figure 3.7.

The chambers in the barrel and most of the endcap are constructed from Monitored Drift Tubes (MDTs) with an Argon gas mixture. Each chamber contains 3-7 drift tubes and provide
hit resolutions of $80 \, \mu m$ per tube and $35 \, \mu m$ per chamber in the bending plane. For $|\eta| > 2.0$, Cathode Strip Chambers (CSCs) are used, primarily to handle the higher incident particle flux. They are composed of cathode strips crossed with anode wires in the gas mixture, but use similar drift technology as the MDTs and have resolutions in the bending plane $40 \, \mu m$ per chamber.

Separate chambers, called Thin Gap Chambers (TGCs), used in the endcaps, and Resistive Plate Chambers (RPCs), used in the barrel, provide less precise hit information but within a much quicker time window, and are therefore used for triggering, as the CSCs and MDTs are too slow.
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3.2.5 The Trigger System

The ATLAS trigger system is designed to make quick decisions about individual particle collisions to reduce the enormous collision rate of 20 MHz to a much more manageable 400 Hz to be stored for offline analysis. Saving the full ATLAS data-stream would require space for 40 TB of raw data per second, but, more importantly, most of these collisions result in the uninteresting inelastic break-up of the colliding protons. To select out collisions to allow for a diverse physics program, ATLAS devotes a large portion of the bandwidth to general purpose single lepton triggers ($\sim 250$ Hz). The presence of leptons in the event indicates the presence of the weak or electro-magnetic interaction and therefore occurs at many order of magnitude less frequently then interactions involving the strong interaction. Moreover, many interesting physics signatures that are analyzable by ATLAS involve leptonic final states. The remaining bandwidth is allocated to jet, missing energy, tau, and unbiased supporting triggers.

The ATLAS trigger system is composed of 3 levels: level-1 (L1), level (L2), and the event filter (EF). The first level is a hardware only trigger that reduces the input 20 MHz rate to $\sim 75$ kHz, selecting 1 out of every 250 collisions. The available buffering on the chips means that the decisions need to be made within 2.5 $\mu$s. The L1 identifies small areas of the detector with significant energy, called Regions-of-Interest (ROIs).

The second and third stages L2 and EF are software based. The L2 algorithms perform more detailed object reconstruction for leptons, jets and photons inside of the ROIs provided by L1, by performing tracking and in depth calorimeter clustering algorithms. The decisions are made within 50 ms per event and pass 1 out of every 15 events to the EF. At the EF, events undergo full reconstruction using similar but faster versions of the algorithms used offline. The EF makes decisions on the presence of fully identified objects in the event and event topological quantities within 4s to reduce the L2 output by a factor of 10. The events
that pass this stage are then written to tape for offline study.

3.2.6 Reconstruction: Jets, Muons and Electrons

Physicists analyze the collision event as a collection of identified objects, expressed as particles’ momentum 3-vectors. The process of converting the disparate detector signatures and signals into a unified 4-momentum description of individual objects is called reconstruction. These objects arise from the final state particles in the event, which can be combined and counted to infer properties of the hard scatter. The particles that make detectable signatures are muons, electrons, photons, and jets of hadrons. Jets and b-tagged jets, muons and electrons are used in the $t\bar{t}H$ analysis to define our search regions and to separate the Higgs signal from backgrounds. Other analyses use photons, taus and missing transverse energy\(^6\), but these are not discussed in depth here. Figure 3.8 shows an $R-\phi$ schematic of the interaction of various particle signatures in the ATLAS detector.

3.2.6.1 Tracks and Clusters

The basic components of reconstruction are sensor measurements, or hits, in trackers (ID, MS) and energy measurements in the calorimeter. Hits in the ID and MS undergo pattern recognition, which identifies hits that belong to a single track, and fitting, which fits a curve to the track to assess the particle trajectory. Charged particle trajectories are generally helical in a magnetic field, but the fitting algorithm takes into more detailed information about energy loss to material along the tracks length. The result of the fitting is an estimation of particle momentum 3-vector. Electrons, photons and hadronic particles leave clustered deposits of energy in the EM and hadronic calorimeters from their showers. Electron and photon showers are primarily contained with the EM calorimeter, while hadronic showers deposit most of

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\(^6\)missing transverse energy is the presence of momentum imbalance in the transverse plane of the calorimeter due to escaping neutrinos
3. The Large Hadron Collider and the ATLAS Experiment

their energy in the hadronic calorimeters. The process of associating individual read-out cells of energy in the calorimeter to clusters of energy from the showers of individual particles is called clustering. From the basic pieces of tracks and clusters, more complex objects can be created.

3.2.6.2 Electrons

Electrons leave both a track in the ID and a narrow and isolated cluster of energy in the EM calorimeter, $\Delta R < 0.1$. Electron reconstruction proceeds using a sliding window algorithm, which scans a fixed size rectangle in $\eta - \phi$ space over the EM calorimeter cells to find relative maxima of energy in the window [51]. These maxima seed the clustering algorithms. Because electrons are light, they lose energy to the material gradually through scattering and more catastrophically through the emission of a high energy photon, through interaction with nuclei. This process is called bremsstrahlung. Tracks for electrons are reconstructed differently because they must include the hypothesis that the electron loses significant energy through bremsstrahlung. Generally, the emitted photon is contained within the same energy cluster and therefore the sliding window algorithm is always wider in the direction of bending, $\phi$. A single track is then matched to the cluster within certain minimum matching requirements in $\eta$, $\phi$, and $p_T$. Electrons are distinguished from photon conversions, which also have a track, by lack of association with conversion vertices, found with a dedicated algorithm.

Electrons have many lever arms for further identification to suppress backgrounds from fake sources. The narrowness of the shower shape, quality of track, and presence of transition radiation are used by cut-based and multivariate identification algorithms. This is discussed in depth in Chapter 4. Electrons are reliably reconstructed and identified with energies above 7 GeV.
3.2.6.3 Muons

Muons are reconstructed from a combination of ID and MS tracks, when possible. The two tracks must meet matching criteria to ensure they are from the same particle. The muon momentum 3-vector comes from the combined ID/MS fit. Muons leave little energy in the calorimeters and are generally isolated from other particles, when produced from electro-weak bosons. Identification algorithms make requirements on the number of tracking hits in the ID and MS and the quality of the matching of the two tracks. Muons are reliably reconstructed and identified with energies above 5 GeV. More about muon reconstruction and identification can be found here [52].

3.2.6.4 Jets

Quarks and gluons are colored objects that cannot exist alone on the time scales of detector measurements, due to confinement, a property of the strong force. When emitted, they undergo a process called hadronization, in which they convert into ‘jets’ of colorless hadrons that emerge collimated from the interaction point. The majority of these hadrons are charged and neutral pions, though other hadrons are often present. Jets are reconstructed using conglomerations of calorimeter energy clusters chosen via an anti-k$_{t}$ algorithm, with a radius of $\Delta R<0.4$ [53]. The algorithm has been shown to be infrared safe, meaning the jet quantities are not sensitive to low energy, small angle radiative divergences. Jets at ATLAS are reconstructed from 10 GeV, calibration of the energy scale and resolution are only available for energies greater than 20-25 GeV.

3.2.6.5 B-Tagged Jets

Generally, the flavor of the initiating quark is not known from the reconstructed jet, although gluon initiated jets and quark initiated jets have slightly different properties. Jets from b
quarks, however, are unique in that the long life-time of the produced B mesons allow for measurable decays in flight. This property is used to tag b-quark initiated jets. This analysis uses the MV1 tagging algorithm [54], which is a neural network based algorithm that looks for secondary displaced decay vertices inside the event and takes into account jet track parameters and energy flow with respect to these vertices. Jets from b quarks often involve B meson decays to leptons, especially muons, which can be used to tag an orthogonal b-jet sample for studying tagging efficiencies.
Chapter 4

Electrons

High energy electron signatures are important elements of searches and measurements at hadron colliders, because they signal the presence of important electro-weak processes in the event. Requiring well-identified electrons in collision events suppresses the overwhelming rate of strong-force mediated scattering and allows for the collection of a manageably-sized dataset with interesting physics for study. For this reason, electron signatures form one of the two pillars of the HLT trigger at ATLAS, as discussed in Chapter 3, and rigorous electron identification is an important piece of many ATLAS analyses. This section summarizes the development of ATLAS electron identification for the high luminosity 2011 and 2012 datasets and discusses the techniques involved in measuring the electron identification efficiency.

4.1 Identification of Electrons at ATLAS

Electron reconstruction is discussed briefly in Chapter 3 and, in depth here [51]. The result of electron reconstruction is called an electron candidate, which is comprised of a narrow calorimeter energy cluster with $|\eta| < 2.47$ and and ID track that matches loosely in $\eta$ and $\phi$. If the electron has $|\eta| < 2.01$, the ID detector track is fiducial to the TRT and has the possibility of having high-threshold hits, indicative of transition radiation (TR). Electron
Electrons

cluster reconstruction is extremely efficient. The track-matching requirement is less efficient, because the presence of hard bremsstrahlung may in certain cases cause the electron cluster and emitted photon cluster to have a wide separation in the calorimeter [55]. Figure 4.1 shows the reconstruction efficiency as a function $|\eta|$ for an example $p_T$ bin as well as a plot of the amount of material in front of the EM calorimeter. The efficiency loss at high $|\eta|$ is caused mostly by material-induced hard bremsstrahlung.

Objects that are not isolated electrons are often reconstructed as electrons, as the reconstruction requirements are quite loose. Objects that often ‘fake’ isolated electrons are light quark and gluon jets, heavy flavor jets that include real decays to electrons, and converted photons. Light quark and gluon jets fragment into a number of collimated hadronic particles. In rare cases, the jet may fragment most of its energy into a single charged pion, which showers early in the EM calorimeter and fakes an electron signature. In other cases, the jet may
fragment mostly into a neutral pion, which subsequently decays into a pair of photons. If one of these photons converts, a track will point to the EM energy cluster and possibly fake an electron signature. These cases would result in a reconstructed electron candidate. Although the probability for these misidentifications to happen is small, the enormous jet production rate means that it is a significant background. In general, light quark and gluon jet ‘fakes’ have larger transverse shower profiles and more energy leakage into the hadronic calorimeter. For the neutral pion case, there are generally two separated showers for lower energy decays. For both cases, there are often other particle signatures nearby. Heavy-flavor jet decays and photon conversions contain real electrons. However, heavy flavor decays also involve the production of additional hadronic particles within the jet. Both photon conversion and heavy flavor decays involved secondary vertices displaced from the primary interaction point.

In order to distinguish these fake signatures from real, isolated electrons, electron identification algorithms use a number of reconstructed variables describing the electron shower in the detector and the electron track. The details of the calculated variables can be found here [56]. In general, electron identification takes advantage of the narrowness of isolated elec-
4. Electrons

electron shower in the transverse plane and lack of energy deposition in the hadronic calorimeter. The transverse variables include measurements of the shower width in both layer 2 and the strips, where more refined measurements are possible. In fact, the strips were designed to separate single photon and electron showers from multiple showers from neutral pion decays, shown in Figure 4.2. The shower width variables are generally measured mostly in $\eta$ as bremsstrahlung tends to smear the electron energy in $\phi$. Electron tracks are required to have an adequate number of hits in the Pixel Detector, SCT and TRT. These hit requirements, especially the b-layer requirement suppress electron conversions which occur in the detector material. Track-cluster matching and geometric impact parameter variables require ID tracks to match the calorimeter energy well and to arise from the primary interaction point. Electrons with tracks explicitly associated with a conversion vertex can be rejected. Finally, the high threshold fraction of hits on the track, made by transition radiation, is an uncorrelated discriminator of pion and electron tracks. Figure 4.3 shows the average high threshold hit probability for pions and electrons as a function of their $p_T$.

Electron identification algorithms make selections in 9 bins of $|\eta|$, $[0.10, 0.60, 0.80, 1.10, 1.37, 1.52, 1.81, 2.01, 2.37, 2.47]$ and bins of $p_T$, $[7, 10, 15, 20, 30, 40, 50, 60, 70, 80+]$ GeV. The $|\eta|$ binning changes with the calorimeter geometry, which in turn affect the shower shape distributions. The shape of most of the identification variable distributions, tracking and calorimeter, are $p_T$ dependent.

4.1.1 2011 Menu

Electron identification in 2011 was accomplished through rectangular cuts on the identification variables at 3 operating points: Loose, Medium and Tight. The medium operating point was used online as the primary electron trigger. At the beginning of the 2011 run, the 3 operating points possessed the same cut-values, but tighter operating points had cuts on more variables.
4. Electrons

Figure 4.3: Electron and pion track high threshold probabilities as a function of their transverse momenta. The two scales are united through the $\gamma$-factor, on which the TR probability depends directly. Electron tracks are much more likely to have high threshold hits at electron energies typical of electro-weak decays.

The Loose operating point only cut on shower shape variables in layer 2 and hadronic leakage, the medium operating point added cuts on shower width variables in the strips, and tight added TR cuts, strict-track cluster matching, conversion rejection and a b-layer requirement. This menu, called the ‘IsEM’ menu, was the first fully data-optimized cut menu for electrons.

The demands of increasing luminosity demanded a tightening of the medium operating point midway through the data-taking, in order to maintain a EF trigger rate of around 20-25 Hz on the primary electron trigger. To accomplish this, variables cut on at the tight operating point were added to the medium operating point, and the entire set of cuts was optimized to provide the targeted fake rejection and reduction in the trigger rates at the highest possible efficiency. The same procedure was applied to the loose operating point, where the target was to provide an efficiency of 95% and the highest possible fake rejection. The re-inventing of the menu in this way allowed for not only better performance, due to the inclusion of more variables, but a more stable tightening of the backgrounds from loose to medium to tight,
4. Electrons

Figure 4.4: Comparison of the ‘IsEM’ (left) and ‘IsEM++’ electron identification operating points for Loose, Medium, and Tight. The efficiency as a function of $\eta$ for an example $p_T$ bin is shown on top and the background rejection is shown on the bottom.

where the same background types were targeted at each level. The new menu was called the ‘IsEM++’ menu and the operating points were renamed ‘Loose++’, ‘Medium++’ and ‘Tight++’. Figure 4.4 shows the comparison of the operating points for the new menu and old menu.

### 4.1.2 2012 Menu and Pile-up

Improvements in the running conditions for 2012, in particular narrowing the transverse beam emittance and size, resulted in large increase in number of proton-proton interactions during every 50 ns bunch crossing. In 2011 the average number of reconstructed primary vertices in each event, an indicator of the number of interaction per bunch crossing, was around 7, while in 2012 the average grew to 25. Some events during 2012 running had 40 reconstructed primary vertices.
The increase in energy in the calorimeters from these additional collisions, called pile-up, caused a worsening of the resolution of electron identification variables, particularly the shower shapes and hadronic leakage. The presumed cause was the increase in the number of showers of low energy hadronic particles near electrons. Figure 4.5 shows two example distributions, the hadronic leakage ($R_{Had}$) and the transverse shower profile ($R_\eta$), for high and low pile-up conditions. The distributions shows a clear widening for higher pile-up which results in a loss of efficiency.

In order to combat this loss, the ‘IsEM++’ menu was once again optimized to have a flatter efficiency profile as a function of the amount of pile-up in the event with similar performance to the 2011 menu. The strategy for this menu was to loosen selections on variables sensitive to pile-up energy. It was expected and confirmed that relying more on the strip variables for the shower shape selection and the energy in layer 3 of the EM calorimeter for the hadronic leakage would sample a smaller volume of the calorimeter and thus be less sensitive to additional energy in the neighborhood of the electron. The strategy is outlined pictorially in Figure 4.6.

The efficiency of the 2011 operating points compared to the 2012 operating points is shown
4. Electrons

Figure 4.6: Schematic of the strategy to reduce the pile-up dependence of electron identification. A EM calorimeter wedge is shown overlaid with example electron (green) and pile-up particle (red) signatures. The strategy is to loosen the dependence of the identification on layer 2 and the hadronic calorimeter, which sample large volumes, and tighten selection on variables in the the 3rd layer and strips, which sample smaller volumes.

Figure 4.7: Comparison of the efficiency of the 2011 and 2012 electron identification menus versus the number of primary vertices in the event.

in Figure 4.7, demonstrating a clear improvement in efficiency of the selections for higher pile-up conditions.
Figure 4.8: Example electron likelihood score output for electrons and fake electrons (left). A cut can be made at any point in this distribution to define a selection operating point (right). The cut-based operating point lies within the curve of possible likelihood operating points, showing that the likelihood indeed outperforms the cuts.

4.1.3 Electron Likelihood

A natural step forward for the electron identification is the use of multi-variate algorithms. Multi-variate identification algorithms use many identification variables at once. Signals and backgrounds can be separated in a multi-dimensional variable space in ways that go beyond simple rectangular cuts. For the case of electron identification, it was found that using a likelihood function, trained with electron identification variables, provided clear performance gains with respect to rectangular cuts, while also providing stable and easily understandable results. The likelihood scores each electron based on how signal-like or background-like it is for each identification variable and then multiplies these individual scores together into a final score. Figure 4.8 shows the example output of the likelihood for real electrons and fake electrons. The output distributions can be cut on continuously to produce a curve of possible selections rather than a single selection point.

There are many advantages to a likelihood-based approach. First, variables that show significant shape differences between real and fake electrons but do not have a clear cut point can still be used in a likelihood. Second, the likelihood score takes into account the entire
shape of the distribution and not simply an efficiency and fake rejection at a single cut point. Finally, the final cut on the likelihood output score can be tuned easily to achieve a desired efficiency and rejection in a way that does not overly bias selection on a single variable.

The likelihood menu for ATLAS was developed at the end of the 2012 run to be used on advanced 2012 analyses. The menu uses similar variables to the cut-based menus but adds a few additional ones, including a measurement of the amount of energy the electron track lost as it traversed the ID. The likelihood menu makes cuts on the likelihood output score at 4 different operating points with the same binning as the cut menu but tunes the cuts based on the number of primary vertices in the event. This tuning ensures a stabil response of the identification with varying degrees of pile-up. The likelihood menu greatly outperforms the rejection of the ‘IsEM++’ menu for similar efficiencies. Figure 4.9 shows a comparison of performance the cut-based and likelihood tight regime operating points. The likelihood menu, specifically the verytight operating point, is used in the $\bar{t}tH$ analysis.

4.2 Measurement of Electron Identification Efficiency at ATLAS

Precise measurements of the electron identification efficiency are important pieces of many ATLAS analyses, including the $\bar{t}tH$ multi-leptons analysis. For analyses with low $p_T$ leptons, systematic uncertainties on the electron identification efficiency can be some of the largest systematic effects. The methods used to measure the electron identification efficiency are described in depth here [51].

Electron identification efficiencies are measured using a method called tag-and-probe for $J/\Psi$ and $Z$ boson decays to electrons. One object from the decay is ‘tagged’, or fully identified, while the other is left unidentified. There is reasonable confidence that the second object is an electron based on the kinematic properties of the event, specifically the di-electron invariant
mass is near the $Z$ or $J/\Psi$ pole. The tag-and-probe method leaves a sample of unidentified and unbiased ‘probes’, where the efficiency can be measured.

As opposed to muons, contamination from fake electron make the tag-and-probe method difficult. Backgrounds from fake electrons are subtracted using fits to the $Z$ and $J/\Psi$ invariant mass distributions. For $Z$ electrons, fits to the electron isolation distribution are also used. The final efficiencies reported are the result of statistical fit among all methods. The uncertainties are at low momenta are around $\sim 5\%$ and are dominated by systematics effects from large background subtractions. They are less than $1\%$ at high momenta and dominated by tag-and-probe selection effects. The efficiency can be seen in Figure 4.11.
4. Electrons

Figure 4.10: Example bins where the electron probe distribution from Z tag-and-probe is fit by an isolation template (left) invariant mass template (right) to subtract backgrounds.

Figure 4.11: Electron identification efficiency calculated in data and MC versus electron $p_T$.

The development of low $p_T$ electron scale-factors was an integral piece in extending the sensitivity of Higgs searches in the $WW$ and $ZZ$ decays modes. Early efforts in 2012 to provide
consistent, well-measured efficiencies in this region were complicated by large disagreements in the efficiencies obtained from the three different estimation methods: $Z$ tag-and-probe with isolation background subtraction, $Z$ tag-and-probe with invariant mass background subtraction, and $J/\Psi$ tag-and-probe. This was especially true for electrons with $p_T$ of 10-20 GeV. The energy scale of $Z$ and $J/\Psi$ decays disfavor electrons of this momentum, and backgrounds are high, revealing problems disguised in higher purity regions. The background subtraction methods were studied in depth to assess possible biases, and a new lower statistics but high purity tag-and-probe method using radiative $Z \rightarrow e^+e^-\gamma$ decays was developed. The result of these studies was the development of new background subtraction templates for the isolation and invariant mass subtraction and an appropriate uncertainty to cover the systematic effects from the biases of these subtractions.
Chapter 5

Analysis Summary

This chapter provides an overview of analysis searching for SM production of the Higgs boson in association with top quarks in multi-lepton final states. The analysis searches in signal regions (SRs) with 2 same-sign, 3 and 4 light leptons ($e, \mu$), which are sensitive to Higgs decays to vector bosons, $H \rightarrow W^\pm W^\pm$ and $H \rightarrow Z^\pm Z^\pm$. We refer to these channels as $2\ell$ SS, $3\ell$, and $4\ell$ through the rest of this document.

Of this set of complementary searches, the multi-lepton and $b\bar{b}$ are the most sensitive. Based on SM production cross-sections, observation lies just outside the sensitivity of the Run I dataset, even when combining all searches. Instead, the analyses provide an opportunity to constrain for the first time the $t\bar{t}H$ production mode with limits reasonably close to the actual production rate. The multi-lepton analysis is therefore optimized to overall sensitivity to the $t\bar{t}H$ production rather than individual decay modes, which would be more useful for constraining Higgs couplings.

Detailed description of the event and objection section are provided in Chapter 7, background modeling in Chapter 8, the effect of systematic errors and the statistical analysis in...
5. Analysis Summary

Chapter 9 and final results in Chapter 10.

5.1 Signal Characteristics

The signal is expected to be characterized by the presence of 2 b-quark jets from the top quark decays, isolated leptons from vector boson and tau decays, a high jet multiplicity and missing energy from neutrinos. Three Higgs boson decays are relevant for this analysis: $W^+W^-$, $\tau^+\tau^-$ and $ZZ$. All modes are generally dominated by the $WW$ signature, though the $3\ell$ and $4\ell$ channels possess some contribution from the $\tau\tau$ and $ZZ$ decays. Table 5.1 provides the fractional contribution of the main Higgs decay modes at the generator level to $t\bar{t}H$ search channels and Figure 5.1 shows example diagrams for each channel. In general, the number of leptons is anti-correlated with the number of jets, since a vector boson can either decay leptonically or hadronically, such that:

- in the $2\ell$ SS channel, the $t\bar{t}H$ final state contains 6 quarks\(^7\). These events are then characterized by the largest jet multiplicity.
- In the $3\ell$, the $t\bar{t}H$ final state contains 4 quarks
- In the $4\ell$ channel, the $t\bar{t}H$ final state contains a small number of light quarks, 0 ($H \rightarrow W^+W^-$ case), 2 or 4 ($H \rightarrow ZZ$ case).

Table 5.1: Contributions of the main Higgs decay modes to the 3 multi-lepton $t\bar{t}H$ signatures at generation level.

<table>
<thead>
<tr>
<th>Signature</th>
<th>$H \rightarrow WW$</th>
<th>$H \rightarrow \tau\tau$</th>
<th>$H \rightarrow ZZ$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Same-sign</td>
<td>100%</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>3 leptons</td>
<td>71%</td>
<td>20%</td>
<td>9%</td>
</tr>
<tr>
<td>4 leptons</td>
<td>53%</td>
<td>30%</td>
<td>17%</td>
</tr>
</tbody>
</table>

\(^7\)this does not include additional quarks from radiation


5. Analysis Summary

5.2 Background Overview

For all channels after selection, the size of the signal is of similar order to the expected size of background. Background processes can be sorted into two categories:

- **Reducible**: These processes cannot lead to a final state compatible with the signal signature without a mis-reconstructed object. This category includes events with a prompt lepton but with mis-reconstructed charge and events with jets that ‘fake’ leptons. The main backgrounds of this sort are $t\bar{t}$ and $Z+$jets. Data-driven techniques are used to measure the rate of these processes and strict object selection and isolation requirements are used to reduce their rate.

- **Irreducible**: Events which can lead to the same final state as the signal. The main background of this category are: vector boson production ($V$) associated with top quarks ($t\bar{t}V$), a $Z$ boson produced in association with a top quark ($tZ$), $W^\pm Z$, and $ZZ$. They are modeled using the Monte Carlo simulations. In general, these backgrounds are combatted with jet and b-tagged jet requirements. Although the jet multiplicity of $t\bar{t}V$ is high, the multiplicity of $t\bar{t}H$ events is still higher.

5.3 Analysis Strategy

The analysis search is conducted in 3 channels, based on counting of fully identified leptons: $2\ell$ SS, $3\ell$, and $4\ell$, with cuts optimized separately for each. We further divide the $2\ell$ SS into sub channels based on the number of jets and flavor of the leptons and the $4\ell$ channel into sub-channels enriched and depleted in opposite-sign (OS) leptons arising from $Z$ decays.

This analysis is a counting experiment, meaning that the only quantities significant to the result are the event counts in the signal regions and not the event shapes. The measured
5. Analysis Summary

background rates, expected signal rates and systematic uncertainties are fed into a Poisson model and fit to the observed data. The parameter of interest in the fit and the result of this measurement is, $\mu$, the ratio of the fitted number of $t\bar{t}H$ events in the signal regions to expected number of $t\bar{t}H$ events in the signal regions. Since we assume SM branching ratios, $\mu$ can be considered the ratio of the measured $t\bar{t}H$ cross-section to the observed $t\bar{t}H$ cross-section, and we expect the fitted $\mu$ to be close to 1 with large statistical errors.

We express the final result as a measurement of $\mu$ with uncertainties and 95% upper limit on the value of $\mu$: $\mu$-values higher than this value will be considered excluded. We provide these results for each channel individually and combined.
Figure 5.1: Example Feynman diagrams for the 3 $t\ell H$ multi-lepton categories.
Chapter 6

Dataset and Simulation

6.1 Data

6.1.1 The 2012 Dataset

The \( t\bar{t}H \) analysis uses the entire 2012 ATLAS dataset only, collected from April to December. The size of the dataset corresponds to 20.3 fb\(^{-1}\), after passing data quality requirements, ensuring the proper operation of the tracking, calorimeter and muon subsystems. The LHC successfully produced datasets for physics studies in 2010, 2011 and 2012. The 2012 proton-proton dataset was delivered with collisions with a CME of 8 TeV with bunch collisions every 50 ns\[59\].

Figure 6.1 shows the accumulation of the 2012 dataset over time. Despite doubling the bunch spacing above the design of 25 ns, the luminosity neared the design luminosity due to unexpected improvements in the transverse beam profile\[60\]. This increased the amount of pile-up, or number of collisions per bunch crossing and in general collision events were busier due to these multiple interactions. Figure 6.2 shows the average number of interaction per bunch crossing for the 2011 and 2012 datasets. The 2012 dataset shows an average of 20-25 interactions.

The dataset must contain either a primary muon or primary electron trigger (\texttt{EF_e24vhi_medium1})
6. Dataset and Simulation

![Plot showing the accumulation of the integrated luminosity delivered to the ATLAS experiment over 2011 and 2012. The rough size of the usable, physics ready dataset for 2012 is 20 fb$^{-1}$ and is the dataset used.](image_url)

Figure 6.1: Plot showing the accumulation of the integrated luminosity delivered to the ATLAS experiment over 2011 and 2012. The rough size of the usable, physics ready dataset for 2012 is 20 fb$^{-1}$ and is the dataset used.

![The average number of interactions per bunch-crossing for the 2012 and 2011 LHC proton-proton dataset. Most of these interactions are uninteresting but leave energetic signatures in particle detectors called pile-up which interfere with measurements.](image_url)

Figure 6.2: The average number of interactions per bunch-crossing for the 2012 and 2011 LHC proton-proton dataset. Most of these interactions are uninteresting but leave energetic signatures in particle detectors called pile-up which interfere with measurements.

OR EF_e60_medium1 OR EF_24i_tight OR EF_36_tight). The electron triggers require a
electron with at least 25 GeV of calorimeter energy, passing the medium identification re-
quirement and loose tracking isolation. Above 60 GeV, the isolation requirement is dropped
and the identification is loosened slightly. The muon trigger requires a good inner detector

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track and matching hits in the muon spectrometer, as well as loose tracking isolation, which is also dropped about 36 GeV.

6.2 Simulation

Simulation samples are used to determine the overall event selection acceptance and efficiency and model the number of events in the signal regions for prompt backgrounds and signal. The simulated samples are created using standard PDF sets use Monte Carlo (MC) techniques to model the hard parton scatter, underlying event activity, parton showering, and hadronization. The samples are then passed through a full ATLAS detector simulation\cite{61} based on GEANT4\cite{62}. Small corrections are then applied to re-scale object identification efficiencies, energy scales, and the pile-up based on control regions from data. These corrections are discussed in Chapter 9.

6.2.1 Signal Simulation

The $t\bar{t}H$ production is modeled using matrix elements obtained from the HELAC-One loop package\cite{63} that corresponds to the next-to-leading order (NLO) QCD accuracy. Powheg BOX\cite{64,65,66} serves as an interface to the parton shower Monte Carlo programs. The samples created using this approach are referred to as PowHel samples. CT10NLO PDF sets are used and the factorization ($\mu_F$) and renormalization ($\mu_R$) scales are set to $\mu_0 = \mu_F = \mu_R = m_t + m_H/2$. Pile-up and the underlying events are simulated by Pythia 8.1\cite{67} with the CTEQ61L set of parton distribution functions and AU2 underlying event tune. The Higgs boson mass is set to 125 GeV and the top quark mass is set to 172.5 GeV.

The signal MC samples are summarized in Table 6.1. These large samples are generated with inclusive Higgs boson decays with branching fractions set to the LHC Higgs Cross Section.
### 6. Dataset and Simulation

#### 6.1 Signal Simulation

Table 6.1: Monte Carlo samples used for signal description.

<table>
<thead>
<tr>
<th>Process</th>
<th>Generator</th>
<th>Cross-section [fb]</th>
<th>$\mathcal{L}$ [fb$^{-1}$]</th>
<th>Detector simulation</th>
</tr>
</thead>
<tbody>
<tr>
<td>$ttH \rightarrow \text{allhad}+H$</td>
<td>PowHel+Pythia8</td>
<td>59.09</td>
<td>2146.5</td>
<td>Full</td>
</tr>
<tr>
<td>$ttH \rightarrow \text{ljets}+H$</td>
<td>PowHel+Pythia8</td>
<td>56.63</td>
<td>2238.9</td>
<td>Full</td>
</tr>
<tr>
<td>$ttH \rightarrow \ell\ell+H$</td>
<td>PowHel+Pythia8</td>
<td>13.58</td>
<td>9332.0</td>
<td>Full</td>
</tr>
</tbody>
</table>

Working Group (Yellow Report) recommendation for $m_H = 125$ GeV [68]. The inclusive cross section (129.3 fb at $m_H = 125$ GeV) is also obtained from the Yellow Report [68].

#### 6.2.2 Background Simulation

The background simulations used for this analysis are listed in Table 6.2. In general, the Alpgen[69], MadGraph[70], and AcerMC[71] samples use the CTEQ6L1[72] parton distribution function, while the Powheg[73], Sherpa[74], are generated with the CT10 PDF. The exception is the MadGraph $t\bar{t}t\bar{t}$ sample, which is generated with the MSTW2008 PDF[75]. The highest order calculations available are used for the cross sections.
Table 6.2: Monte Carlo samples used for background description. Unless otherwise specified MadGraph samples use Pythia 6 for showering and Alpgen samples use Herwig+Jimmy. $tt$, single top, and $Z$+jets samples are replaced with data-driven estimates for the final result.

<table>
<thead>
<tr>
<th>Process</th>
<th>Generator</th>
<th>Detector simulation</th>
</tr>
</thead>
<tbody>
<tr>
<td>$ttW^\pm,ttZ$</td>
<td>MadGraph</td>
<td>Full</td>
</tr>
<tr>
<td>$tZ$</td>
<td>MadGraph</td>
<td>AF2</td>
</tr>
<tr>
<td>$tt\bar{t}$</td>
<td>MadGraph</td>
<td>Full</td>
</tr>
<tr>
<td>$ttW^\pm W^\pm$</td>
<td>Madgraph+Pythia8</td>
<td>AF2</td>
</tr>
<tr>
<td>$t\bar{t}$</td>
<td>Powheg+Pythia6</td>
<td>Full/AF2</td>
</tr>
<tr>
<td>single top tchan</td>
<td>AcerMC+Pythia6</td>
<td>Full</td>
</tr>
<tr>
<td>single top schan→l</td>
<td>Powheg+Pythia6</td>
<td>Full</td>
</tr>
<tr>
<td>single top $W^\pm t$</td>
<td>Powheg+Pythia6</td>
<td>Full</td>
</tr>
<tr>
<td>$W\gamma^*$</td>
<td>MadGraph</td>
<td>Full</td>
</tr>
<tr>
<td>$W\gamma+4p$</td>
<td>Alpgen</td>
<td>Full</td>
</tr>
<tr>
<td>$W^+W^-$</td>
<td>Sherpa</td>
<td>Full</td>
</tr>
<tr>
<td>$W^\pm Z$</td>
<td>Sherpa</td>
<td>Full</td>
</tr>
<tr>
<td>Same-sign WW</td>
<td>Madgraph+Pythia8</td>
<td>AF2</td>
</tr>
<tr>
<td>ZZ</td>
<td>Powheg+Pythia8,gg2ZZ+Herwig</td>
<td>Full</td>
</tr>
<tr>
<td>$Z\gamma^*$</td>
<td>Sherpa</td>
<td>Full</td>
</tr>
<tr>
<td>$Z$+jets</td>
<td>Sherpa</td>
<td>Full</td>
</tr>
<tr>
<td>ggF Higgs</td>
<td>Powheg+Pythia8</td>
<td>Full</td>
</tr>
</tbody>
</table>
Object and Event Selection

The analysis is divided into 3 signal regions based on lepton counting: 2 same-sign leptons, 3 leptons and 4 leptons. The lepton counting occurs for fully identified leptons with full overlap removal with transverse momenta over 10 GeV to ensure orthogonality. Lepton selections are tightened afterward within each region.

The cuts for each signal region are provided in Table 7.1 and the object selections are detailed in the following selections. The selections are based on optimizations of the region sensitivity performed using MC (event for data driven backgrounds) and ad-hoc values for normalization systematic uncertainties.

All signal regions are comprised of three basic requirements: the presence of b-tagged jets, the presence of additional light jets, and a veto of same flavor opposite sign leptons with an invariant mass within the Z window. Additional requirements on the invariant mass of the leptons, the missing transverse energy in the event, and the total object energy ($H_T$) proved to have negligible additional benefit at our level of statistics. Figure 7.1 shows the background and signal fractions as a function number of jets and number of b-tagged jets for otherwise fully selected events.

The objects of optimization were the lepton momenta, identification operating points, isolation and event

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8the sensitivity was approximated using the $\frac{\sqrt{b+\Delta b}}{b}$ formula. The systematic errors considered were 20% for $t\bar{t}V$ and $VV$ and 30% for fakes. These ended up being close the final systematic errors assessed in Chapter 9. The objects of optimization were the lepton momenta, identification operating points, isolation and event
### 7. Object and Event Selection

#### Table 7.1: Selections in the 2\(\ell\) SS, 3\(\ell\) and 4\(\ell\) Signal Regions

<table>
<thead>
<tr>
<th>Signal Region</th>
<th>2(\ell) SS</th>
<th>3(\ell)</th>
<th>4(\ell)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Trig. Matched Lepton</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>(N_{l}^{\mu})</td>
<td>=2, (N_{e} = 0)</td>
<td>=3</td>
<td>=4</td>
</tr>
<tr>
<td>Lepton Charge Sum</td>
<td>+2 or -2</td>
<td>+1 or -1</td>
<td>0</td>
</tr>
<tr>
<td>Lepton (p_T) (GeV)</td>
<td>(p_{T0} &gt; 25)</td>
<td>(p_{T0} &gt; 10)</td>
<td>(p_{T0} &gt; 25)</td>
</tr>
<tr>
<td></td>
<td>(p_{T1} &gt; 20)</td>
<td>(p_{T1,2} &gt; 25, 20)</td>
<td>(p_{T1} &gt; 20)</td>
</tr>
<tr>
<td>Jet Counting</td>
<td>(N_{b} \geq 1, N_{jet} = 4)</td>
<td>(N_{b} \geq 1, N_{jet} \geq 4)</td>
<td>(N_{b} \geq 1, N_{jet} \geq 2)</td>
</tr>
<tr>
<td>Mass Variables (GeV)</td>
<td>(</td>
<td>M_{SFOS} - M_{Z}</td>
<td>&lt; 10)</td>
</tr>
<tr>
<td>Sub-channels</td>
<td>2 ((N_{jet} = 4, N_{jet} \geq 5)) (\times) 3((ee, e\mu, \mu\mu))</td>
<td>none</td>
<td>2 (No SFOS leps, SFOS leps)</td>
</tr>
</tbody>
</table>

#### 7.1 2\(\ell\) Same-Charge Signal Region

The 2 lepton signal region requires two leptons of similar charge (2\(\ell\) SS). The signal is symmetric in charge but the background from opposite-sign \(t\bar{t}\) di-lepton production would be overwhelming. Requiring only two leptons allows the extra 2 W bosons in the event to decay hadronically, resulting in on average 4 additional light jets plus 2 additional b-quark jets from the top decays.

We require a leading lepton with transverse momentum of at least 25 GeV that matches to a trigger and a sub-leading lepton of at least 20 GeV, a b-tagged jet, and at least 4 jets in total.

In order to suppress non-prompt backgrounds, the lepton isolation criteria for tracking and calorimeter are tightened from less than 10% of the lepton momentum to 5%. To suppress charge misidentification, the electron is required to be extremely central (|\(\eta\)| < 1.37) to avoid the material-rich regions of the detector. Additionally, ee events with a lepton pair invariant mass within 10 GeV of the Z pole are removed. To maintain orthogonality with the \(\tau\) analyses, kinematic variables...
events with fully identified taus are vetoed.

For the statistical combination the channel is divided into 6 sub-channels: 2 jets counting bins ($N_{jet} = 4, N_{jet} \geq 5$) x 3 lepton flavor bins (ee, $\mu\mu$, $e\mu$).

### 7.2 3$\ell$ Signal Region

The 3 lepton channel requires 3 leptons, whose summed charge is either $-1$ or $+1$. The leptons are ordered in this way:

- **lep0**: the lepton that is opposite in charge to the other two leptons
- **lep1**: the lepton that is closer in $\Delta R$ to lep0
- **lep2**: the lepton that is farther in $\Delta R$ from lep1

Since events with a fake lepton arise exclusively from opposite sign di-lepton processes, $t\bar{t}$ and $Z$+jets, where additional jets are misidentified as the third lepton, lep0 is never the fake lepton. As a result, the transverse momentum requirement of lep0 ($> 10$ GeV) is lower than the other two, $> 20$ GeV. One lepton must match a trigger and have $p_T > 25$ GeV.

The 3$\ell$ channel further requires at least one b-tagged jet and at least 4 jets in total, or two b-tagged jets and exactly 3 jets in total. Additionally, to suppress $W^\pm Z$ and $Z$+jets events, events with same-flavor opposite-sign (SFOS) pairs within 10 GeV of the $Z$ pole are vetoed.

Additional cuts, including a di-lepton mass cut, and splittings were investigated but low statistics proved to wash out any advantages. The di-lepton mass cut will be a useful discriminator in future analyses since the spin statistics of Higgs decay in $W$ bosons often causes the two emitted opposite-sign leptons to point in the same direction, resulting in a small measured invariant mass.
7. Object and Event Selection

7.3 4ℓ Signal Region

In the four lepton signal region, selected events must have exactly four leptons with a total charge of zero. At least one lepton must be matched to one of the applied single lepton trigger and have a transverse momentum above 25 GeV. The leading and sub-leading leptons are required to have transverse momentum of 25 and 15 GeV respectively. In order to suppress background contributions from low-mass resonances and Drell-Yan radiation, all SFOS lepton pairs are required to have a dilepton invariant mass of at least 10 GeV.

The four-lepton invariant mass is required to be between 100 and 500 GeV. This choice of mass window suppresses background from the on-shell $Z \rightarrow 4\ell$ peak and exploits the high-mass differences between the signal and the dominant $t\bar{t}Z$ background. Events containing an SFOS lepton pair within 10 GeV of the $Z$ boson mass are discarded. This $Z$-veto procedure greatly reduces background contributions from $ZZ$ and $t\bar{t}Z$. Finally, selected events are required to have at least two jets, at least one of which must be tagged as a $b$-quark jet.

The contribution from $t\bar{t}Z$ comprises approximately 75% of the total background in the inclusive signal region. A signal region categorization which factorizes $t\bar{t}Z$ from the remaining backgrounds is thus beneficial. The signal region is accordingly divided into two categories based on the presence of SFOS lepton pairs in the final state.

7.4 Electron Selection

The electrons are reconstructed by a standard algorithm of the experiment [51] and the electron cluster is required to be fiducial to the barrel or endcap calorimeters: $|\eta_{\text{cluster}}| < 2.47$. Electrons in the transition region, $1.37 < |\eta_{\text{cluster}}| < 1.52$, are vetoed. Electrons must have $p_T>10$ GeV and pass the verytight likelihood identification criteria.

In order to reject jets misidentified as electrons, electron candidates must also be well
isolated from additional tracks and calorimeter energy around the electron cluster. Both the tracking and calorimeter energy within $\Delta R = 0.2$ of the electron cluster must be less than 5% of the electron transverse momentum: $p_{T\text{cone20}}/P_T < 0.05$ and $E_{\text{cone20}}/E_T < 0.05$. All quality tracks with momentum greater than 400 MeV contribute to the isolation energy. Calorimeter isolation energy is calculated using topological clusters with corrections for energy leaked from the electron cluster. Pile-up and underlying event corrections are applied using a median ambient energy density correction.

The electron track must also match the primary vertex. The longitudinal projection of the track along the beam line, $z_0 \sin \theta$, must be less than 1 cm) and the transverse projection divided by the parameter error, $d\theta$ significance, must be less than 4. These cuts are used in particular to suppress backgrounds from conversions, heavy-flavor jets and electron charge-misidentifications.

The electron selection is summarized in Table 7.2.

### 7.5 Muon Selection

Muons used in the analysis are formed by matching reconstructed inner detector tracks with either a complete track or a track-segment reconstructed in the muon spectrometer (MS), called Chain 2 muons. The muons have $p_T > 10$ GeV and satisfy $|\eta| < 2.5$. The muon track are required to be a good quality combined fit of inner detector hits and muon spectrometer segments, unless the muon is not fiducial to the inner detector, $|\eta| > 2.47$. Muons with inner detector tracks are further required to pass standard inner detector track hit requirements [52].

As with electrons, muons are required to be isolated from additional tracking or calorimeter energy: $p_{T\text{cone20}}/P_T < 0.1$, $E_{\text{cone20}}/E_T < 0.1$. A cell-based $E_{\text{cone20}}/P_T$ relative isolation variable is used. A pile-up energy subtraction based on the number of reconstructed vertices
7. Object and Event Selection

in the event is applied. The subtraction is derived from a Z boson control sample.

The muons must also originate from the primary vertex and have impact parameter requirements, \(d_0\) significance < 3, and \(z_0 \sin \theta < 0.1\) cm, similar to the electrons.

The muon selection is summarized in Table 7.2.

7.6 Jet and b-Tagged Jet Selection

Jets are reconstructed in the calorimeter using the anti-\(k_t\) [53] algorithm with a distance parameter of 0.4 using locally calibrated topologically clusters as input (LC Jets). Since the jets in the \(t\bar{t}H\) signal mostly arise from the decay massive resonances and not radiation, they are expected to be central and high energy. Jets must have \(p_T > 25\) GeV and \(|\eta| < 2.5\).

Jets must also pass loose quality requirement, ensuring the proper functioning of the calorimeter at the time of data taking. Jets near a hot calorimeter cell in data periods B1/B2 are rejected. The local hadronic calibration is used for the jet energy scale, and ambient energy corrections are applied to account for energy due to pileup.

Jets within \(|\eta| < 2.4\) and \(p_T < 50\) GeV are further required to be associated with the primary vertex. The fraction of track \(p_T\) associated with the jet that comes from the primary vertex, must exceed 0.5 (or there must be no track associated to the jet). This requirement rejects jets that arise from pile-up vertices.

B-jets are tagged using a Multi-Variate Analysis (MVA) method called MV1 and relying on information of the impact parameter and the reconstruction of the displaced vertex of the hadron decay inside the jet[54]. The output of the tagger is required to be above 0.8119 which corresponds to a 70\% efficient Working Point (WP).
7. Object and Event Selection

7.7 Object Summary and Overlap

Since many fully identified objects may be reconstructed as two different objects, an overlap removal procedure is applied. Electrons within $\Delta R < 0.1$ of muons are rejected in favor of the muon. Jets within $\Delta R < 0.3$ of electrons are then removed. Finally, muons within $\Delta R < 0.04 + 10 \text{GeV}/p_T$ of jets are rejected, as these muons are thought to arise from jet fragmentation.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Values</th>
<th>Remarks</th>
</tr>
</thead>
<tbody>
<tr>
<td>$p_T$</td>
<td>$&gt; 10$ GeV</td>
<td></td>
</tr>
<tr>
<td>$</td>
<td>\eta</td>
<td>$</td>
</tr>
<tr>
<td>ID</td>
<td>Very Tight Likelihood</td>
<td></td>
</tr>
<tr>
<td>Electrons</td>
<td></td>
<td>&lt; 1.37 for 2$\ell$ SS channel</td>
</tr>
<tr>
<td>Isolation</td>
<td>$E_{T\text{Cone}}20/p_T \cdot p_T/\text{Cone}20 &lt; 0.05$</td>
<td></td>
</tr>
<tr>
<td>Jet overlap removal</td>
<td>$\Delta R &gt; 0.3$</td>
<td></td>
</tr>
<tr>
<td>$</td>
<td>d_0^{\text{xy}}</td>
<td>$</td>
</tr>
<tr>
<td>$z_0\sin\theta$</td>
<td>$&lt; 1 \text{ cm}$</td>
<td></td>
</tr>
<tr>
<td>Muons</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$p_T$</td>
<td>$&gt; 10$ GeV</td>
<td></td>
</tr>
<tr>
<td>$</td>
<td>\eta</td>
<td>$</td>
</tr>
<tr>
<td>ID</td>
<td>Tight</td>
<td></td>
</tr>
<tr>
<td>Jet overlap removal</td>
<td>$\Delta R &gt; 0.04 + 10 \text{GeV}/p_T$</td>
<td></td>
</tr>
<tr>
<td>Isolation</td>
<td>$E_{T\text{Cone}}20/p_T \cdot p_T/\text{Cone}20 &lt; 0.1$</td>
<td>&lt; 0.05 for 2 leptons</td>
</tr>
<tr>
<td>$</td>
<td>d_0^{\text{xy}}</td>
<td>$</td>
</tr>
<tr>
<td>$z_0$</td>
<td>$&lt; 1 \text{ cm}$</td>
<td></td>
</tr>
<tr>
<td>Jets</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$p_T$</td>
<td>$&gt; 25$ GeV</td>
<td></td>
</tr>
<tr>
<td>$</td>
<td>\eta</td>
<td>$</td>
</tr>
<tr>
<td>JVF</td>
<td>JVF &gt; 0.5 or no associated track or $p_T &gt; 50$ GeV</td>
<td></td>
</tr>
<tr>
<td>b-Tag</td>
<td>MV1 70% operating point</td>
<td></td>
</tr>
</tbody>
</table>

Table 7.2: Object identification and selection used to define the 5 channels of the multi-lepton $t\bar{t}H$ analysis. Some channels use a sub-sample of objects as explained in the Remarks column.
Figure 7.1: Number of jets vs. number of b-tagged jet plot for the fully selected multi-lepton channels. Signal regions are outlined with a dashed line. Sub-channels are defined later in the 2ℓ SS and 4ℓ SRs. The fractional background contribution to each jet and b-tagged jet bin are shown for non-prompt (red), ttV + tZ (yellow), and VV (green). The expected signal fraction is shown in white. The expected non-prompt fraction contains charge misidentifications and fakes. It is shown for MC only, although data-based methods are used for the final result.
Chapter 8

Background Estimation

The $t\bar{t}H$ multi-lepton signal regions discussed in Chapter 5 are contaminated by background contributions at a similar order of magnitude to the signal. The dominant background for each region is $t\bar{t}V$. Sub-dominant but important backgrounds include the production of vector boson pairs in association with jets and b-quark jets ($VV$) and $t\bar{t}$ production with a jet misidentified as a lepton (fakes). The $2:\ell SS$ regions possesses a unique background of charge misidentification from $Z$ and top events. The methods for estimating these backgrounds are discussed in this chapter. Monte Carlo simulation is used for the prompt $t\bar{t}V$ and $VV$ contributions. The non-prompt backgrounds from $t\bar{t}$ jet-misidentification and charge-misidentification are estimated using data-driven methods. Table 8.1 provides a summary of the $t\bar{t}H$ signal and background expectation for each of the signal regions, including the data-driven estimates discussed in this section.

8.1 Vector Boson ($W^\pm$, $Z$) production in association with top quarks: $t\bar{t}V$, $tZ$

Production of top quarks plus vector boson is an important background in all multi-lepton channels. A large part of the $t\bar{t}V$ component, arising from on-shell $Z \rightarrow \ell\ell$, can be removed via
## Table 8.1: Expected number of signal and background events in 2\(\ell\) SS, 3\(\ell\) and 4\(\ell\) signal regions.

<table>
<thead>
<tr>
<th></th>
<th>(\geq 5) jets</th>
<th>Same-sign</th>
<th>4 jets</th>
<th>3 leptons</th>
<th>4 leptons</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(e^+e^+)</td>
<td>(e^+\mu^+)</td>
<td>(\mu^+\mu^+)</td>
<td>(e^+e^+)</td>
<td>(e^+\mu^+)</td>
</tr>
<tr>
<td>(ttH)</td>
<td>0.73 ± 0.03</td>
<td>2.13 ± 0.05</td>
<td>1.41 ± 0.04</td>
<td>0.44 ± 0.02</td>
<td>1.16 ± 0.03</td>
</tr>
<tr>
<td>(ttV)</td>
<td>2.60 ± 0.13</td>
<td>7.42 ± 0.17</td>
<td>5.01 ± 0.16</td>
<td>3.05 ± 0.13</td>
<td>8.39 ± 0.24</td>
</tr>
<tr>
<td>(t\bar{t}Z)</td>
<td>0.71 ± 0.03</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>fake leptons (DD)</td>
<td>0.48 ± 0.25</td>
<td>0.37 ± 0.23</td>
<td>0.68 ± 0.30</td>
<td>0.77 ± 0.27</td>
<td>1.93 ± 0.80</td>
</tr>
<tr>
<td>Q misid (DD)</td>
<td>2.33 ± 0.92</td>
<td>6.66 ± 1.06</td>
<td>2.89 ± 0.67</td>
<td>3.45 ± 1.36</td>
<td>12.33 ± 1.56</td>
</tr>
<tr>
<td>Tot Background</td>
<td>6.52 ± 1.45</td>
<td>15.30 ± 1.64</td>
<td>8.85 ± 1.18</td>
<td>9.07 ± 1.42</td>
<td>23.97 ± 2.70</td>
</tr>
</tbody>
</table>
a $Z$ mass veto on SFOS leptons. However the $Z \rightarrow \tau\tau$ and $\gamma^*$ components remain. The $t\bar{t}W^\pm$ and $tZ$ processes generally require extra jets to reach the multiplicity of our signal regions, as such it is important to ascertain uncertainties associated with QCD radation. We consider uncertainties on both the $t\bar{t}W^\pm$ and $t\bar{t}Z$ production cross-sections of these two processes and event selection efficiencies in the signal regions. The latter is sensitive to the NJet modelling in the MC. We assess the size of these uncertainties by investigating the effects of the choice of the factorization ($\mu_F$) and renormalisation $\mu_R$ scales and PDF sets.

Monte Carlo events for these processes are generated with MadGraph 5 and showered with Pythia 6. $t\bar{t}W^\pm$ events are generated with up to two extra partons at matrix element level, while for $t\bar{t}Z$ up to one extra parton at matrix-element level is produced. The $tZ$ process is simulated without extra partons. The next-to-leading-order (NLO) cross sections are implemented by applying a uniform $k$-factor to the leading-order (LO) events for each process. For $t\bar{t}Z$, the $k$-factor is determined by comparing LO and NLO cross sections for on-shell $Z$ production only and then applied to the off-shell signal regions.

The $t\bar{t}V$ uncertainties are calculated using the internal QCD scale and PDF re-weighting that is available with MadGraph5+aMC@NLO. The prescription for the scale envelope is taken from [76]: the central value $\mu = \mu_R = \mu_F = m_t + m_V / 2$ and the uncertainty envelope is $[\mu_0/2, 2\mu_0]$. The PDF uncertainty prescription used is the recipe from [77]: calculate the PDF uncertainty using the MSTW2008nlo [75] PDF for the central value and then the final PDF uncertainty envelope is derived from three PDF error sets each with different $\alpha_S$ values (the central value and the upper and lower 90% CL values). The final NLO cross section central values and uncertainties are given in Table 8.2.

The $tZ$ process is normalized to NLO based on the calculation in Ref. [78]. Here the scales are set to $\mu_0 = m_t$ and the scale variations are by a factor of four; the scale dependence is found to be quite small.
8. Background Estimation

Table 8.2: NLO cross section and theoretical uncertainty calculations derived from MadGraph5 + aMC@NLO.

<table>
<thead>
<tr>
<th>Process</th>
<th>$\sigma_{NLO}$ [fb]</th>
<th>Scale Uncertainty [%]</th>
<th>PDF Uncertainty [%]</th>
<th>Total symmetrized uncertainty [%]</th>
</tr>
</thead>
<tbody>
<tr>
<td>$ttW^+$</td>
<td>144.9</td>
<td>+10</td>
<td>-11</td>
<td>+7.7</td>
</tr>
<tr>
<td>$ttW^-$</td>
<td>61.4</td>
<td>+11</td>
<td>-12</td>
<td>+6.3</td>
</tr>
<tr>
<td>$ttZ$</td>
<td>206.7</td>
<td>+9</td>
<td>-13</td>
<td>+8.0</td>
</tr>
<tr>
<td>$tZ$</td>
<td>160.0</td>
<td>+4</td>
<td>-4</td>
<td>+7</td>
</tr>
<tr>
<td>$tZ$</td>
<td>76.0</td>
<td>+5</td>
<td>-4</td>
<td>+7</td>
</tr>
</tbody>
</table>

Table 8.3: Theoretical uncertainties of the $ttW^\pm$ and $ttZ$ event yields in the signal regions due to the impact of matching, modelling, parton shower, QCD scale, and PDF differences on the event selection.

<table>
<thead>
<tr>
<th>Matching [%]</th>
<th>2l4jets</th>
<th>2l$\geq$5jets</th>
<th>3l</th>
<th>4l</th>
</tr>
</thead>
<tbody>
<tr>
<td>$ttZ$</td>
<td>16.0</td>
<td>9.7</td>
<td>0.5</td>
<td>2.0</td>
</tr>
<tr>
<td>$ttW^\pm$</td>
<td>4.2</td>
<td>0.2</td>
<td>10.2</td>
<td>—</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Modeling [%]</th>
<th>2l4jets</th>
<th>2l$\geq$5jets</th>
<th>3l</th>
<th>4l</th>
</tr>
</thead>
<tbody>
<tr>
<td>$ttZ$</td>
<td>3.5</td>
<td>8.7</td>
<td>6.2</td>
<td>10.5</td>
</tr>
<tr>
<td>$ttW^\pm$</td>
<td>0.1</td>
<td>10.8</td>
<td>15.6</td>
<td>—</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Parton Shower [%]</th>
<th>2l4jets</th>
<th>2l$\geq$5jets</th>
<th>3l</th>
<th>4l</th>
</tr>
</thead>
<tbody>
<tr>
<td>$ttZ$</td>
<td>2.4</td>
<td>10.2</td>
<td>2.4</td>
<td>2.4</td>
</tr>
<tr>
<td>$ttW^\pm$</td>
<td>2.4</td>
<td>10.2</td>
<td>13.0</td>
<td>—</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>QCD Scale [%]</th>
<th>2l4jets</th>
<th>2l$\geq$5jets</th>
<th>3l</th>
<th>4l</th>
</tr>
</thead>
<tbody>
<tr>
<td>$ttZ$</td>
<td>1.5</td>
<td>2.3</td>
<td>1.4</td>
<td>0.9</td>
</tr>
<tr>
<td>$ttW^\pm$</td>
<td>1.1</td>
<td>2.5</td>
<td>3.6</td>
<td>—</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>PDF [%]</th>
<th>2l4jets</th>
<th>2l$\geq$5jets</th>
<th>3l</th>
<th>4l</th>
</tr>
</thead>
<tbody>
<tr>
<td>$ttZ$</td>
<td>1.5</td>
<td>2.3</td>
<td>1.4</td>
<td>0.9</td>
</tr>
<tr>
<td>$ttW^\pm$</td>
<td>1.1</td>
<td>2.5</td>
<td>3.6</td>
<td>—</td>
</tr>
</tbody>
</table>

Acceptance uncertainties on $ttV$ MC modelling for considered for 5 separate effects: the matrix element to parton shower matching algorithm, the modelling of the jet multiplicity, the modelling of the the parton shower, the QCD scale, and the choice of PDF set. These uncertainties are considered by comparing event yields in the signal regions with different modelling choices for each effect and are summarized in Table 8.3.
8. Background Estimation

8.1.1 $t\bar{t}Z$ Validation Region

Unlike $t\bar{t}W^\pm$ a $t\bar{t}Z$ validation region can be obtained by simply inverting the veto on SFOS lepton pairs near the Z pole in the 3 lepton signal region. This region thus requires 3 leptons (with momentum and identification cuts discussed in Chapter 7, at least one SFOS pair of leptons within 10 GeV of the Z mass, and either 4 jets and at least 1 b-tagged jet or exactly 3 jet and 2 or more b-tagged jets. The resulting region has low statistics and is not used as a control region but is instead used as a validation to demonstrate that the normalization uncertainty, discussed above, is properly evaluated.

The region defined by this is predicted to be 67% $t\bar{t}Z$, 17% $W^\pm Z$, and 13% $tZ$. We predict 19.3 ± 0.5 events and observe 28, giving a observed-to-predicted ratio of $1.45 ± 0.27 ± 0.03$, where the errors are from data and simulation statistics, respectively. Given the large errors, the region is still in agreement with the predictions to within 1-1.5 $\sigma$. Distributions of various variables are shown in Fig. 8.1.

8.2 Di-boson Background Estimation: $W^\pm Z$, ZZ

$W^\pm Z$ and ZZ di-boson production with additional and b-tagged jets constitute small contributions to the $3\ell$ and $4\ell$ channels. For the $3\ell$ case $W^\pm Z$ comprises $\sim$ 10% of the total background, while for the $4\ell$ case ZZ contribution accounts comprises $\sim$ 10% of the total background. Because of the small size of these contributions, each of the above processes can be assigned a non-aggressive uncertainty based on similar previous analyses with ATLAS and cross-checked with data validation regions and MC truth studies.

Both $W^\pm Z$ and ZZ production have been studied by ATLAS [79][80], but neither process has been investigated thoroughly in association with multiple jets and b-quark jets. However, single boson production with b-quark jets has been investigated. Both $W + b$ [81] and $Z + b$
Figure 8.1: Data/MC comparison plots for \( t\bar{t}Z \) control region A (\( \geq 4 \) jets, \( \geq 1 \) b-tag and 3 jets, \( \geq 2 \) b-tag). In all plots, the rightmost bin contains any overflows. Top left: number of electrons. Top right: \( 10^8 \) the number of b-tags + the total number of jets. Middle left: the invariant mass of the (0,1) lepton pair (see the text for the definition of the lepton ordering). Middle right: the invariant mass of the (0,2) lepton pair.

\[82\] production in 7 TeV data have been shown to agree with MC models to within 20-30%.

A single \( W \) produced in association with b-tagged jets possesses a similar topology to the \( W^\pm Z + b \) process at a different energy scale and has been shown to be dominated by c mis-tags and b-jets from gluon splitting and multiple parton interaction. The \( W + b \) analysis, referenced above, uses Alpgen MC with Herwig PS modeling, only provides results to 1 additional jet, and uses the CombNN tagger (we use MV1). Its results are therefore not directly comparable to this \( t\bar{t}H \) analysis (where \( W^\pm Z \) is modeled using Sherpa with massive c and b quarks). Z + b production originates from slightly different diagrams than \( ZZ + b \), but the sources of
the b-tags are similar. The 7 TeV analysis, referenced above, provides results with Sherpa MC with an agreement of $\sim 30\%$. However, it also used the CombNN tagger instead of MV1. Because of the differences of the 2011 single boson analyses (type of tagger used, type of MC and tunes used), we would like to verify the general 20-30\% level of agreement in 2012 data with the simulation and tagger used in the $t\bar{t}H$ analysis: Sherpa MC, 2012 tunes, MV1. With the data skims available to use we are able to do this in the $Z + b$ region but not the $W + b$.

Figure 8.2 shows the spectrum of the number of reconstructed and selected jets (NJet) in a $Z + b$ validation region, defined by 2 tight-isolated leptons within 10 GeV of the Z mass and with at least one b-tagged jet, using the $t\bar{t}H$ analysis definitions. The level of agreement in this region confirms at the 30\% level seen in the 7 TeV analysis, discussed above.

![Figure 8.2: NJet spectrum for 2 tight-isolation leptons with 1 b-tagged jet (MV1_70)](image)

In the following two sections, we assess the truth origin of jets in the $W^\pm Z + b$ and $ZZ + b$ regions and leverage data/MC agreement where we can. We see that the data allows us to constrain the $W^\pm Z$ to 50\%. We claim this 50\% as a systematic. The 20-30\% agreement in the single boson regions above bolsters our confidence in this number.
8. Background Estimation

8.2.1 $W^\pm Z$ Normalization Uncertainty

The $t\bar{t}H$ analyses have two validation regions to test the Sherpa agreement with data for $W^\pm Z$: one inclusive 3 lepton region, using the three-lepton channel object and $p_T$ cuts and a $W^\pm Z + b$ region with 1 b-tagged jet and a requirement that at least one SFOS pair have an invariant mass within 10 GeV of the Z mass. The region with fewer than 4 jets is $W^\pm Z$ dominated. Figure 8.3 shows kinematic variables for the inclusive region. The overall data normalization is $\sim$10% higher than MC, but this will be well within our systematic uncertainty. The NJet shape shows good agreement across the full spectrum, giving confidence about the Sherpa high NJet SR extrapolation. Figure 8.4 shows NJet spectrum for the $W^\pm Z + b$ validation region with agreement within statistical uncertainties. The region has low statistics and around $\sim$ 60% purity and statistical analysis of the region suggests that a 50% normalization error on the $W^\pm Z$ component is enough to cover any possible mismodelings, especially in higher NJet bins, which are closer to the signal regions.

We also examine the $W^\pm Z$ truth origins of the b-jet in the $W^\pm Z + b$ validation region (VR) and the signal region using MC to assess the validity of the extrapolation from the VR to the SR and to confirm the similarity in jet origin to the single boson analyses, references above. The flavour of the closest matching truth particle ($p_T > 5$ GeV, after FSR) in $\Delta R$ determines the true-jet flavor. If there are no quarks, taus or gluons within $\Delta R$ of 0.3, the label defaults to light. Table 8.4 shows the origin fraction of b-tagged jets in the various $W^\pm Z + b$ VRs and the SR. If there are two b-tagged jets, the highest $p_T$ is used, but this is a small fraction of the number of b-tags. As expected the c and b contributions dominate, as was the case with the 2011 single boson analyses referenced above. It is important also that the VR has similar composition to the SR. There is a small dependence on the number of jets.
8. Background Estimation

8.2 ZZ Normalization Uncertainty

In order to investigate the MC agreement with data in the ZZ case, two validation regions similar to the $W^\pm Z$ case are defined. First, a 4 lepton ZZ region is constructed using the object selections for the 4-lepton channel and requiring exactly two pairs of SFOS leptons with a di-lepton invariant mass within 10 GeV of the Z mass. Additionally, the ZZ + b process is investigated directly using a similar validation region which again requires exactly two Z-
candidate lepton pairs as well as at least 1 b-tagged jet. Some kinematic distributions are shown in Figures 8.5 and 8.6, and particular attention should be paid to the NJet spectrum, which shows good data-MC agreement in the high-jet bins, with a slight discrepancy in the 1-jet bin. The agreement for the region with at least 2 jets yields confidence in the NJet MC modeling in this region which lies close to the 4-lepton signal region.

Based on the study of the $ZZ$ and $ZZ + b$ validation regions and the overall agreement noted with the $Z + b$ analysis, we expect a similar error to $W^{\pm}Z$ to be appropriate in the $ZZ$ case. A truth origin study is undertaken in MC to demonstrate a similar b-jet origin to the $W^{\pm}Z$ case. The true origin of the leading (highest energy) b-tagged jet is shown in Table 8.5 for the 4-lepton signal region as well as the $ZZ + b$ validation region described above divided into jet bins. As it was in the $W^{\pm}Z$ case above, the true origin of the b-jet in
8. Background Estimation

Figure 8.5: Jet-inclusive 4-lepton $ZZ$ validation region using the $ttH$ lepton identification and momentum cuts

Figure 8.6: $ZZ + b$ validation region using the $ttH$ lepton identification and momentum cuts
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ZZ + b is dominated by c and b. Taking this study in tandem with the results from the $W^\pm Z$ investigation, it is appropriate to take the central value of the ZZ + b background contribution in the 4-lepton SR from MC and to assign an overall systematic of 50% in order to account for the MC modeling limitations.

<table>
<thead>
<tr>
<th></th>
<th>Bottom</th>
<th>Charm</th>
<th>Light</th>
</tr>
</thead>
<tbody>
<tr>
<td>ZZ + b VR 1 Jet</td>
<td>0.56 ± 0.03</td>
<td>0.24 ± 0.01</td>
<td>0.20 ± 0.01</td>
</tr>
<tr>
<td>ZZ + b VR 2 Jet</td>
<td>0.52 ± 0.05</td>
<td>0.25 ± 0.02</td>
<td>0.23 ± 0.02</td>
</tr>
<tr>
<td>ZZ + b VR 3 Jet</td>
<td>0.53 ± 0.11</td>
<td>0.25 ± 0.08</td>
<td>0.22 ± 0.07</td>
</tr>
<tr>
<td>4l SR</td>
<td>0.34 ± 0.15</td>
<td>0.42 ± 0.16</td>
<td>0.24 ± 0.10</td>
</tr>
</tbody>
</table>

Table 8.5: Truth origin of highest energy b-tagged jet in the ZZ + b VR and 4l SR

8.3 Charge-Misidentification Background

Charge-misidentification contributes to the background for 2$\ell$ SS case and only for flavor channels, which include electrons. The same-sign requirement is essential in removing large SM opposite sign-backgrounds, but because of their size even small charge misidentification rates result in contamination in same-sign regions. For the 2$\ell$ SS signal regions, charge-misidentification background arise primarily from $t\bar{t}$ di-lepton events with a smaller contribution from leptonic Z decays.

In general, charge-misidentification can arise in two ways. The first occurs for ultra-high energy electrons and muons, which leave tracks in the detector that are too straight for the fit to determine the direction of curvature with high confidence. This type of charge misidentification is not a concern to the $t\bar{t}H$ multi-lepton analysis, as most of the leptons have transverse momentum $< 150$ GeV. The second source of charge misidentification is from 'tridents', which only occurs for electrons, because their low mass allows for high rate bremsstrahlung in the detector material. In some cases, after an electron releases a photon through bremsstrahlung, the photon may convert nearby resulting in three electron tracks. The reconstruction algo-
Background Estimation

Algorithms may sometimes match the wrong track to the calorimeter energy deposit, resulting in a possible charge misidentification. As discussed in the selection, tight track-cluster geometric and energy matching requirements are applied on the electron candidates to reduce the overall rate and the electron acceptance is narrowed to ($|\eta| < 1.37$), since most of the material is concentrated more forward in the detector.

We estimate the contribution of charge-misidentification events in our $2\ell$ SS signal regions and relevant control regions by applying a weight per electron in the OS region with otherwise identical cuts. The weight is related to the charge-misidentification rates. We measure these rates using a likelihood method in the OS and SS $Z \rightarrow ee$ control region in data. The rate measured from these control regions is binned in electron $p_T$ and $\eta$, to account for dependencies in these variables. The method, validations and associated errors are discussed in detail in the following sub-sections.

### 8.3.1 Likelihood Method

The number of reconstructed same-sign ($N_{ss}$) $Z \rightarrow ee$ events is related to total number of produced $Z \rightarrow ee$ ($N$) through factors related to the charge misidentification rate, $\epsilon$:

$$N_{ss}^{ij} = N^{ij}(\epsilon_i + \epsilon_j - 2\epsilon_i \epsilon_j)$$  \hspace{1cm} (8.1)

where $\epsilon_i$ and $\epsilon_j$ are the charge misidentification rates for each electron separately. If we drop terms quadratic in $\epsilon$, we have:

$$N_{ss}^{ij} = N^{ij}(\epsilon_i + \epsilon_j).$$  \hspace{1cm} (8.2)

Although it is impossible to know event-by-event which electron’s charge was misidentified, we can use a likelihood method over the whole $Z$ sample to measure how $\epsilon$ depends on the
8. Background Estimation

electron $p_T$ and $|\eta|$. As illustration, we first consider the case, where $\epsilon$ depends on only one variable, $|\eta|$, and then generalize to the two-dimensional case of $|\eta|$ vs $p_T$.

$N_{ss}^{ij}$ is described by a Poisson distribution:

$$f(k, \lambda) = \frac{\lambda^k e^{-\lambda}}{k!},$$

where $k$ is the observed number of occurrences of the event, i.e. $k = N_{ss}^{ij}$, and $\lambda$ is the expected number, i.e. $\lambda = N^{ij}(\epsilon_i + \epsilon_j)$. Thus, the probability for an observed number of same-sign $Z$ events given the sample size and charge misidentification rates is expressed by:

$$P(N_{ss}^{ij} | N_{ss}, \epsilon_i, \epsilon_j) = \frac{[N^{ij}(\epsilon_i + \epsilon_j)]^{N_{ss}^{ij}} e^{-N^{ij}(\epsilon_i + \epsilon_j)}}{N_{ss}^{ij}!}.$$  

(8.4)

The likelihood $L$ for all the events is obtained by evaluating all the $|\eta|$ combinations:

$$L(\epsilon | N_{ss}, N) = \prod_{i,j} \frac{[N^{ij}(\epsilon_i + \epsilon_j)]^{N_{ss}^{ij}} e^{-N^{ij}(\epsilon_i + \epsilon_j)}}{N_{ss}^{ij}!}.$$  

(8.5)

In this process, the $-\ln L$ is used in order to simplify and make easier the minimization. Terms which do not depend on the rates $\epsilon_i$ and $\epsilon_j$ are removed in this step. This way, the final function to minimize is given by the following expression:

$$-\ln L(\epsilon | N_{ss}, N) \approx \sum_{i,j} \ln[N^{ij}(\epsilon_i + \epsilon_j)]N_{ss}^{ij} - N^{ij}(\epsilon_i + \epsilon_j).$$  

(8.6)

The likelihood can be easily extended to depend on the charge misidentification rates as a function of two parameters. The probability to find a same-sign event given the rates for each electron is $(\epsilon_{i,k} + \epsilon_{j,l})$, where the two indices represent binned $|\eta|$- and $p_T$-dependence. Thus, the Eq. 8.6 transforms into

$$-\ln L(\epsilon | N_{ss}, N) \approx \sum_{i,j,k,l} \ln[N^{ij,kl}(\epsilon_{i,k} + \epsilon_{j,l})]N_{ss}^{ij,kl} - N^{ij,kl}(\epsilon_{i,k} + \epsilon_{j,l}).$$  

(8.7)

We use events selected within the $Z$ peak using the $t\bar{t}H$ electron object cuts. The events are stored in two matrices: one for the same-sign events $N_{ss}^{ij,kl}$, and the other one for all
events $N^{ij,kl}$. Small backgrounds need to be subtracted. The background subtraction is done using a simple side-band method. This method consists in dividing the $Z$ invariant mass in three regions, i.e. $A$, $B$ and $C$, where $B$ is the central region corresponding to the $Z$ peak. The number of events is counted in the regions on the sides of the peak, i.e. $n_A$ and $n_C$, and removed from the total number of events in the peak region $B$, $n_B$. This way, the number of signal events $N_Z$ is given by

$$N_Z = n_B - \frac{n_A + n_C}{2}. \quad (8.8)$$

Once the background has been subtracted, the likelihood is minimized for the 2D matrix of $\epsilon$ bins. Knowing $\epsilon$ as a function of $|\eta|$ and $p_T$ for any single electron, it is now possible to estimate the number of same-sign events from the number of opposite sign events in any sample:

- $N^{ss} = \frac{\epsilon_i \epsilon_j - 2 \epsilon_i \epsilon_j}{1 - \epsilon_i - \epsilon_j + 2 \epsilon_i \epsilon_j} N^{os}$ for $ee$ channels
- $N^{ss} = \frac{\epsilon}{1 - \epsilon} N^{os}$ for the $e\mu$ channels

### 8.3.2 Results

The charge misidentification rate is calculated in 7 $|\eta|$ bins [0.0, 0.6, 1.1, 1.37, 1.52, 1.7, 2.3, 2.47] by 4 $p_T$-bins [15, 60, 90, 130, 1000] GeV. For $p_T$ bins above 130 GeV, the $Z$ dataset becomes too small and the rates are calculated using $t\bar{t}$ MC, scaled by the data-MC ratio of the rates in the lower $p_T$ bins, [90-130] GeV. Figure 8.7 shows the extracted rates in all bins.

As a cross-check, we apply the full method to the $Z$ MC samples (extracting rates via a likelihood fit and applying them to opposite sign events) and compare to the MC predicted number of same-sign events. The invariant mass of the $Z$ from our charge misidentification and directly from the MC can be seen on Figure 8.8. In the simulated $Z$ samples, the number
Figure 8.7: Electron charge misidentification rates measured in data with the likelihood method on $Z$ events (black points, red squares and blue triangles) as a function of $|\eta|$ and parametrized in $p_T$. The full 2012 dataset has been used to estimate the rates below 130 GeV. Above this value, the charge misidentification rates have been estimated by extrapolating the rates in the region where the $p_T \in [90, 130]$ GeV with a $p_T$ dependent factor extracted from simulated $t\bar{t}$ events (green triangles). Statistical and systematic uncertainties have been included in this plot.

of same-sign $Z$ events is 5 049 while the estimation is $5 031^{+375}_{-365}$. The uncertainties combine both statistical systematic uncertainties, which are discussed in depth below. The validation gives compatible results within uncertainties.

8.3.3 Systematic and Statistical Uncertainties

Statistical uncertainties dominate the combined uncertainty on the charge misidentification estimate. The statistical uncertainties come primarily from the size of the $Z$ same-sign sample in data and are especially large for central, material-poor regions where the charge misidentification rate is extremely low. Additional systematic uncertainties are included for a comparison between the positron and electron rate, the per-bin MC closure test discussed above, and for the effect of varying the invariant mass window used for the background subtraction for three
Figure 8.8: Closure test on simulated $Z \rightarrow e^+ e^-$ events (a) and data (b). The black circles show the distribution of same-sign events while the blue histograms show the distribution of the re-weighted opposite-sign events together with the statistical and systematic uncertainties. The distributions are not expected to overlay exactly, due to the loss of energy of the trident electrons for the same-sign peak.

For different cases. Figure 8.9 shows the relative uncertainties for all rate bins.

Figure 8.9: Relative systematic uncertainty contributions on the charge misidentification rate, for different bins in $p_T$ and $|\eta|$. 

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8. Background Estimation

We apply the rates to estimate the charge misidentification background in the $2\ell$ SS signal regions, and find $\sim 25\%$ contamination in the $e^\pm e^\pm$ regions and a $\sim 10\%$ contribution to the $e^\pm \mu^\pm$ regions with a $10\%$ systematic error overall. The low overall error can be attributed to the fact that the statistical error is lowest where the bulk of charge misidentifications occur. The charge flip contribution measured in the signal regions from this method is detailed in Table 8.1.

8.4 Fake Lepton Backgrounds

Fake leptons, from the misidentification of jets as either electrons or muons, primarily arise from $t\bar{t}$ and single top processes in the $2\ell$ SS, $3\ell$ and $4\ell$ channels. Smaller contributions come from $Z$+jet events. Fake backgrounds are sub-dominant but important in the $2\ell$ SS and $3\ell$ channels. They are extremely small in the $4\ell$ channels. Truth studies suggest that these misidentified leptons arise overwhelmingly from b-quark initiated jets. The general method for estimating fakes in all channels is to define a reversed object selection control region (usually isolation) for each lepton flavor with otherwise identical signal region selection ($N_{e CR}^e$, $N_{CR}^\mu$).

This region is fake-dominated. The total number of fake events in these regions are then scaled by transfer factors ($\theta$) to estimate the number of fake events of the appropriate flavor in the signal region. The simple formula for determining fakes is defined in Equation 8.9.

$$N_{fake} = \theta_e \cdot N_{CR}^e + \theta_\mu \cdot N_{CR}^\mu$$ (8.9)

This approach factorizes the background model into two separate measurements. $N_{CR}^f$ is sensitive the overall $t\bar{t}$ production rate, especially in the presence of additional jets from QCD ratio, as well as the object-level misidentification of a jet as a lepton. The transfer factors are sensitive to only the object level properties of the misidentified jet, and in particular only the
variables which are reversed in the anti-tight identification.

The transfer factors are obtained in a different way for each channel, due to unique issues with statistics and contamination, but each method relies heavily on the data-based control regions with fewer jets. Figure 8.10 shows a truth study of the stability of the transfer factor for the $2\ell$ SS and $3\ell$ cases as a function of the number of jets in the event for events with one-b-tagged jet. This suggest that the regions with fewer jets are a good model of the fakes in the signal regions with more jets and is expected because of the homogeneity of origin of the fakes across all jet bins.

The details of the methods for each channel are discussed in depth in the following sections. For all methods, the overall systematic uncertainty on the normalization of the fake estimate is in the range 30%-50% and arise primarily from statistics and the closure on assumptions used to obtain the transfer factor.

![Figure 8.10: Ratios of regions with tight and anti-tight leptons in 2-lepton and 3-lepton channels from $t\bar{t}$ MC. These ratios are the MC calculated transfer factors for each region, i.e. $\theta_e = eee/eed, ee/ed$ and $\theta_{\mu} = mmp/mmm, mm/mp$, where 'd' refers to anti-tight electrons and 'p' refers to anti-tight muons. The transfer factors are seen to be similar in the $2\ell$ and $3\ell$ cases and stable as a function of the number of jets.](image)

Because these methods do not provide a per-object transfer-factor that depends on the properties of the faking object, we must use the MC to model the shapes of the fake kinematic
8. Background Estimation

distributions in the signal regions. This is not an essential issue, since the analysis only considers only the total number of events in each signal region in the final measurement of $t\bar{t}H$ production.

8.4.1 2$\ell$ SS Fakes

The 2$\ell$ SS fake method follows the procedure outlined in general above. We define anti-tight electron and muon control regions with reversed particle identification criteria for each signal region, including the 6 flavor and jet-counting sub regions. The anti-tight muon and electron criteria are provided below:

- **anti-tight electron** (d): fails the verytight likelihood operating point, but still passes the veryloose operating point. fails relative tracking and calorimeter isolation, $E_T^{rel} > 0.05$ and $p_T^{rel} > 0.05$.

- **anti-tight muon** (p): $6 \text{ GeV} < p_T < 10 \text{ GeV}$

The electron and muon transfer factors, $\theta_e$ and $\theta_\mu$, are calculated in the region with signal region selection but fewer jets, $NJet = 2$ or $NJet = 3$ and are defined as the ratio of the number of events for two fully identified leptons to the number of events with one fully identified lepton and one anti-identified lepton, after the prompt and charge misidentification backgrounds are subtracted. Only same-flavor channels are used to ensure that muon and electron transfer factors maybe estimated separately: on every region, the prompt and charge-misidentification backgrounds are subtracted from the data.

$$\theta_e = \frac{N_{ee}}{N_{ed}} = \frac{N_{ee}^{Data} - N_{ee}^{Prompt SS} - N_{ee}^{QMisId}}{N_{ed}^{Data} - N_{ed}^{Prompt SS} - N_{ed}^{QMisId \ MC}} \quad (8.10)$$

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8. Background Estimation

Table 8.6: Number of events of the main simulated background processes and of the data in the e±e± and µ±µ± channels used for the measurement of \( \theta_e \) and \( \theta_\mu \). VV, Vγ, \( t\bar{t}V, tV \) and \( t\bar{t} \) prompts (or charge misID) are the backgrounds which lead to prompt same-sign dileptons and are subtracted from the data to get a measured number of fakes. Uncertainties are statistical. The numbers labeled Data fakes are used to measure \( \theta_\mu \).

\[
\theta_\mu = \frac{N_{\mu\mu}}{N_{\mu\mu}} = \frac{N_{Data}^{\mu\mu} - N_{Prompt\ SS}^{\mu\mu}}{N_{Data}^{\mu\mu} - N_{Prompt\ SS}^{\mu\mu}} \tag{8.11}
\]

The 2,3 jet anti-tight regions used in obtaining the transfer factors are shown in Table 8.6 and the 4,5 jet anti-tight regions, scaled by the transfer factors to get the fake estimates in the SR are shown in Figure 8.11. The \( t\bar{t} \) and single top MC are included in the plots and tables for reference, although they are not used in the measurements.
Figure 8.11: 4,5 Jet SS 2ℓ ed (above) and μp control regions with at least one b-tagged jet. After subtraction of prompt and charge misidentification backgrounds, these regions are scaled by the transfer factors, θ_e and θ_μ, to obtain the final number of fake events in the CR. The top MC (red) is used for reference but not in the actual calculation.

The transfer factors obtained from the 2 and 3 jet regions are shown in 8.7 with statistical errors and propagated systematic errors from the subtraction of relevant backgrounds (t¯tV and charge misidentification). The MC values are just for comparison. An additional systematic error is added by comparing the transfer factors, obtained from the low jet control region, to those obtained from the higher jet signal regions, using different t¯t MC. The value of this systematic is 20-30%. Since we consider only the closure effects of t¯t fakes, we risk possible effects from non-t¯t fakes in assessing the appropriateness of the low NJet extrapolation. These include W+jet and di-jet fakes. In order to ensure that the extrapolation is under control with the possible presence of these fakes, we vary the b-tagged Jet p_T and missing energy cut,
8. Background Estimation

<table>
<thead>
<tr>
<th>Factor</th>
<th>Expected (MC)</th>
<th>Measured (data)</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \theta_e )</td>
<td>0.0136 ± 0.0062</td>
<td>0.01569 ± 0.00619</td>
</tr>
<tr>
<td>( \theta_\mu )</td>
<td>0.1211 ± 0.0175</td>
<td>0.2468 ± 0.0539</td>
</tr>
</tbody>
</table>

Table 8.7: Expected and measured values of the \( \theta \) factors.

<table>
<thead>
<tr>
<th>Uncertainties</th>
<th>4 jets</th>
<th>( \geq 5 ) jets</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \Delta \theta_e ) (stat)</td>
<td>39.6</td>
<td>39.6</td>
</tr>
<tr>
<td>( \Delta \theta_\mu ) (stat)</td>
<td>21.9</td>
<td>21.9</td>
</tr>
<tr>
<td>( \Delta N_{\ell-\text{anti-}\ell}(n \text{ jets})(\text{stat}) )</td>
<td>19.9</td>
<td>29.6</td>
</tr>
<tr>
<td>Statistical</td>
<td>9.71</td>
<td>16.0</td>
</tr>
<tr>
<td>Systematics</td>
<td>6.8</td>
<td>8.9</td>
</tr>
<tr>
<td>( \Delta \theta_\mu ) (closure)</td>
<td>6.8</td>
<td>9.2</td>
</tr>
<tr>
<td>( \Delta \theta_\mu ) (other fakes)</td>
<td>24.8</td>
<td>20.6</td>
</tr>
<tr>
<td>( \Delta \theta_\mu ) (other fakes)</td>
<td>14.0</td>
<td>9.2</td>
</tr>
<tr>
<td>Q Mis Id (( \ell-\text{anti-}\ell ))</td>
<td>2.2</td>
<td>6.5</td>
</tr>
<tr>
<td>Q Mis Id (( \ell-\ell ))</td>
<td>24.0</td>
<td>7.92</td>
</tr>
<tr>
<td>HW</td>
<td>24.0</td>
<td>4.1</td>
</tr>
<tr>
<td>HW XS</td>
<td>2.75</td>
<td>4.1</td>
</tr>
<tr>
<td>HW</td>
<td>2.75</td>
<td>4.1</td>
</tr>
<tr>
<td>ttZ</td>
<td>0.49</td>
<td>0.48</td>
</tr>
</tbody>
</table>

Table 8.8: Summary of the uncertainties (in %) in \( e^+e^- \) (reverse Id + reverse isolation method), \( \mu^+\mu^- \) and \( e^+\mu^- \). Statistical uncertainty is splitted into statistical uncertainties on \( \theta_e \) and \( \theta_\mu \) and uncertainty due to the Control Region size (\( \Delta N_{\ell-\text{anti-}\ell}(n \text{ jets}) \)). The correlated systematics are anti-correlated to the systematic on other background processes on the signal region.

and recalculate the transfer factors. The largest deviations we see in the electron and muon transfer factors as a result are 14\% and 17\% respectively, and we include these as additional systematic uncertainties.

The overall systematic uncertainties and contribution from each source in all of the sub-channels of the signal region are shown in Table 8.7 and the final contribution of fake events to the signal region are show in Table 8.1 found at the beginning of the chapter.

8.4.2 3\( \ell \) Fakes

The 3\( \ell \) fake method follows the same general strategy as the 2\( \ell \) SS case. Transfer factors are used to extrapolate from anti-tight, fake-rich control regions in data into the signal region.
However, the equivalent low jet control regions are too low in statistics to provide the transfer factors from data directly. Instead, the transfer factors are obtained directly from the $t\bar{t}$ simulation. Data control regions, called auxiliary regions, are used to determine the modeling of the identification and isolation variables, used in the transfer factor extrapolation. The low jet regions are still employed in a low statistics validation of the entire fake procedure.

Anti-tight electrons and muons are defined in slightly different ways, compared to the $2\ell$ SS case:

- **anti-tight electron (d):** fails to pass the verytight likelihood operating point, but still verifies the veryloose operating point. The isolation selection is released $E_{T}^\text{rel} > 0.05$, $p_{T}^\text{rel} > 0.05$.

- **anti-tight muon (p):** muons must pass identification but the $p_{T}$ cuts is lowered to 6 GeV. The overlap removal with jets and isolation cuts are released.

The transfer factors, $\theta_e$ and $\theta_\mu$, extracted from MC, is defined as the ratio of the number of top ($t\bar{t} + \text{single-top}$) events in the signal region, to the number of $t\bar{t}$ events in the anti-tight regions. The factors are calculated in separate flavor regions to ensure that the electron jet fakes and muon jet fakes are calculated separately. The calculation follows the same form as for the $2\ell$ SS case, but now lep0, which by construction is almost never a fake is allowed to be either electron or muon in both cases, denoted below in Equations 8.12 and 8.13.

\[
\theta_e = \frac{N_{\text{top}}^{\text{exe}}}{N_{\text{top}}^{\text{xed}}} \quad (8.12)
\]

\[
\theta_\mu = \frac{N_{\text{top}}^{\text{xmu}}}{N_{\text{top}}^{\text{xip}}} \quad (8.13)
\]

The MC modeling of the variables involved in the transfer factor can be verified when another variable fails. For instance, the MC modeling of the electron isolation variable can be
8. Background Estimation

compared to data when the particle identification variable fails and vice-versa. The modeling of muon-jet $\Delta R$, involved in the overlap removal, can be compared when either the isolation variable or the $p_T$ fails. The comparison of the electron variables in this manner can be seen in Figure 8.13 and the muon variables in Figure 8.12. The regions used have the same selection as the signal region with an added missing transverse energy requirement, $> 60 \text{ GeV}$, to ensure only top fakes. 20% and 30% systematic uncertainties are assigned to the muon and electron transfer factors, respectively, to account for data-MC discrepancies. This method for evaluating data-MC agreement for individual electron and muon variables in turn relies on the assumption that these variables are largely uncorrelated and that the transfer factor itself is factorizable into pieces for each variable. Factorized and fully correlated transfer factors have been compared using MC and shown to have differences smaller than the systematic quoted, suggesting that the uncorrelated assumption is reasonable.

The electron and muon anti-tight control regions, which are scaled by the transfer factors are shown in Figure 8.14. The prompt MC subtracted data in these regions are scaled by the transfer factors to obtain the overall contribution of fake electron and muon events in the signal region. The systematic uncertainties are split between the statistical error on the transfer factor and normalization of the anti-tight control regions and the data-MC comparisons outlined above. For muon fakes the total systematic uncertainty is 25% and for electrons it is 34%. The numbers and uncertainties involved in the calculation are shown in Table 8.9.

<table>
<thead>
<tr>
<th>Stage</th>
<th>Muon</th>
<th>Electron</th>
</tr>
</thead>
<tbody>
<tr>
<td>Anti-Tight CR Normalization</td>
<td>364.62 ± 20.02 (5%)</td>
<td>38.2 ± 6.9 (17%)</td>
</tr>
<tr>
<td>Transfer factor</td>
<td>0.0047 ± 0.0011 (23%)</td>
<td>0.0240 ± 0.0064 (36%)</td>
</tr>
<tr>
<td>SR Contribution</td>
<td>1.71 ± 0.42 (25%)</td>
<td>0.91 ± 0.35 (39%)</td>
</tr>
</tbody>
</table>

Table 8.9: Summary of regions and inputs to the extraction of the number of $t\bar{t}$ events with a fake muon in the SR

The low jet region (1, 2, 3) is used as a validation for the method. The $t\bar{t}$ and single
Figure 8.12: Distributions of the properties of the anti-tight muons in data (dots), compared with the total simulation (red line), rescaled to the integral of the data for a shape comparison. The uncertainty on the data distribution is statistical. The number of events for each of them is also presented in the legend. The variables probed are, top: $p_T$ and $\Delta R(\mu, closest selected jet)$; bottom: $p_{Tcone20}/p_T$ and $E_{Tcone20}/p_T$. The selection is the signal region event selection with one anti-tight muon (failing at least one of the isolation, muon-jet overlap, or $p_T$ selection criteria). A ratio plot is containing the 20% area around 1, is displayed, demonstrating that a 20% data-MC comparison systematic is sufficient.
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Figure 8.13: Distributions of anti-tight electron variables. The variables presented are, from top left to bottom right, $p_T$, $\eta$, verytight Likelihood value, $p_{Tcone20}/p_T$, $E_{Tcone20}/p_T$. The plotted regions have the same cuts as the signal region, except the anti-tight electron must fail isolation for the plot of the verytight identification word or fail the verytight identification word for the plots of the isolation. Data (dots) are compared with a stacked histogram of the various simulated samples: top in red, $V+$jets (blue), $VV$ (purple) and $t\bar{t}V$ (yellow). The uncertainty on the data distribution is statistical.

top fakes in this region are estimated using the procedure above. Similar systematics are assessed. This region with the fake estimate is plotted in Figure 8.15. The agreement of data and summed prediction for the fakes and prompt backgrounds is well within the systematic and statistical uncertainties. The figure also shows the same region with relaxed $p_T$ cuts on all leptons to 10 GeV, which enriches the fake contributions greatly. The data and summed fake and prompt predictions are also well within the statistical and systematic uncertainties.
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Figure 8.14: Muon-xxp (above) and electron-xxd (below) anti-tight control regions: jet variables. Note: the $t\bar{t}$ and single top MC in the plots is used only as comparison, but is not included in the fake measurement.

8.4.3 $4\ell$ Fakes

We will not discuss the $4\ell$ fakes in depth, as it is a very small background - at the % level and will have almost no impact on the final result. The fake method used in the the $4\ell$ case is similar to the $2\ell$ and $3\ell$ cases discussed above. All fakes arise from $t\bar{t}$ and single-top events, where two jets are misidentified as leptons. To measure the contribution of this background, control regions with 2 fully identified and 2 anti-identified leptons are created. These control regions do not have a number of jets requirement in order to increase statistics. From these control regions, two extrapolations are made. First, a transfer factor is applied to extrapolate from the anti-tight to tight regions for electrons and muons. The regions are defined with
8. Background Estimation

Figure 8.15: 3ℓ fake validation regions for nominal $p_T$ selection (above) and relaxed $p_T$ selection, $> 10$ GeV, (below). Plotted are the number of jets and the number of electrons in each event. The data and MC ratio below each plot agree with 1 within the statistics of the region and the overall systematic assigned for the fake component (red)

identical object identification selection and reversal as the 3ℓ case, and the same transfer factors can be used. They must be used twice however, because there are two anti-identified leptons in each event. Second, the jet inclusive regions are extrapolated into the 2-jet signal region, using a second extrapolation factor derived from $t\bar{t}$ events. Since, the majority of fake leptons arise from b-quark initiated jets, the jet spectrum $t\bar{t}$ events with the additional requirement of 2-b-tagged jets from data are used as a model for the jet extrapolation. The overall systematic uncertainty on this measurement arises from the statistics in the control regions and MC based assessments of non-closure and are 35%-50% depending on the sub-
8. **Background Estimation**

channel.
Chapter 9

Summary of Systematic Uncertainties

This chapter summarizes the systematic uncertainties that enter the measurement of the limit of $t\bar{t}H$ multi-lepton analysis. The systematic uncertainties arise from three main sources. The first are the normalization uncertainties on the background process estimation methods, which are discussed in depth in Chapter 8. The second source is the theoretical uncertainties on the $t\bar{t}H$ production cross-section and acceptance. The final source are the experimental and detector related systematic uncertainties related to event selection efficiencies and measurements and identification of the objects. They affect only the non-data driven backgrounds and the $t\bar{t}H$ signal, as simulation is used to model their acceptance and efficiency for the analysis selection.

These systematic uncertainties, the estimated background and signal event counts in each of the signal regions, and the observed data in each signal region are combined in a statistical fit to an analysis model to extract the measurement of interest. We measure per-channel and combined ratios of the observed production rate to the theoretically predicted production rate of $t\bar{t}H$, a parameter called $\mu$. In the absence of a statistically significant observation, this measurement is translated into a upper confidence limit on $\mu$. The details of this procedure are discussed in the following sections and the results with the observed data are discussed in Chapter 10.
9. Summary of Systematic Uncertainties

9.1 Systematic Uncertainties on Signal Cross-section and Acceptance

The $t\bar{t}H$ signal is simulated with matrix elements at NLO in QCD with Powhel. The simulation details are discussed in Chapter 6. The production cross section and the Higgs boson decay branching fractions together with their theoretical uncertainties from the QCD scale and PDF choice are taken from the NLO theoretical calculations reported in [68]. The uncertainty from the QCD scale estimated by varying $\mu_0$ by a factor of 2 from the nominal value is $^{+3.8\%}_{-9.3\%}$, while the uncertainty from the PDF set and the value of $\alpha_S$ is $^{\pm8.1\%}$.

The impact of the choice of the QCD scale on the simulation of the $t\bar{t}H$ event selection efficiency is estimated in two independent ways.

First, the factorization and renormalisation scales $\mu_0$ are varied by a factor of 2, as $\mu = 2\mu_0$ and $\mu = \mu_0/2$. The effects of these new scales are estimated via the application of event re-weighting procedures on the nominal simulation using kinematic distributions at parton level. The weights used are dependent on the transverse momenta of both the $t\bar{t}H$ system and of the top quark, as described in [83].

Second, the choice of the factorization and renormalisation scales, dependent on fixed (static) parameters in the nominal simulation, is tested comparing its prediction with an alternative (dynamic), but still physics motivated choice $\mu_0 = (m_{t\bar{t}}^2 - m_t^2 - m_H^2)^{1/3}$, which depends on kinematic variables. This comparison is performed via event re-weighting of the nominal static simulation based on weights derived as a function of the $t\bar{t}H$ transverse momentum [83].

In order to take the difference between the choices of scale as systematic uncertainties, a symmetric envelope around the nominal simulation is built applying the weights and also their inverses.

In order to not double-count the variations on the total cross section the predictions
Table 9.1: Theoretical uncertainties of the signal event yields in the signal regions due to the impact of QCD scale uncertainties on the event selection.

<table>
<thead>
<tr>
<th>QCD scale [%]</th>
<th>2\ell4jets</th>
<th>2\ell≥5jets</th>
<th>3\ell</th>
<th>4\ell</th>
</tr>
</thead>
<tbody>
<tr>
<td>Static</td>
<td>0.6</td>
<td>2.7</td>
<td>2.3</td>
<td>0.9</td>
</tr>
<tr>
<td>Dynamic</td>
<td>-0.0</td>
<td>-1.3</td>
<td>-0.2</td>
<td>-0.2</td>
</tr>
</tbody>
</table>

from the different QCD scales are normalized to the same total cross section. That means that the observed differences are only coming from the event selection. Significant variations on the jet multiplicities can be seen and these translate into different predictions on the signal event yields in the signal regions. Such differences, listed in Table 9.1, are taken as theoretical systematic uncertainties in addition to the ones affecting the total \( t\bar{t}H \) production cross section. The static uncertainties come from the variations by a factor of 2 from the nominal scale and they are correlated with the uncertainties on the total cross section, which are estimated with the same procedure. The dynamic uncertainties come from the difference between the nominal and the alternative dynamic scale and are treated as an independent source of theoretical uncertainty.

The uncertainty of the \( t\bar{t}H \) event selection due to the PDF sets is estimated comparing the predictions with three different PDF sets, varying each set within errors and taking the width of the envelope as systematic uncertainty. The recommended sets are CT10, MSTW2008nlo68cl and NNPDF21_100.

Figure 9.1 shows the estimated PDF systematic uncertainties as a function of the jet multiplicity in \( t\bar{t}H \) events with at least two leptons. The uncertainties are compatible with the uncertainty on the production cross section estimated in [68] and indicated by the dashed red lines in the lower panel. Table 9.2 shows the half-width of the envelope of the acceptance under all eigenvector variations of the three PDF sets. No significant dependence on the event topology is observed, so that the PDF systematic uncertainty on the \( t\bar{t}H \) event selection is
9. Summary of Systematic Uncertainties

Table 9.2: Uncertainties on $t\bar{t}H$ acceptance in signal regions due to PDF variation.

<table>
<thead>
<tr>
<th>Sample</th>
<th>$t\bar{t}H$</th>
<th>$2\ell 4j$</th>
<th>$2\ell 5j$</th>
<th>$3\ell$</th>
<th>$4\ell$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0.3%</td>
<td>1.0%</td>
<td>0.5%</td>
<td>1.4%</td>
<td></td>
</tr>
</tbody>
</table>

neglected.

Figure 9.1: PDF systematic uncertainty on the jet multiplicities in $t\bar{t}H$ events with at least 2 leptons. The dashed red lines in the lower panel indicate the systematic uncertainty on the $t\bar{t}H$ production cross section.

The acceptance uncertainty related to the parton shower and underlying event modelling is estimated by comparing the event yields in the signal regions with the nominal parton shower and underlying event generator (PYTHIA) with HERWIG++. The statistical uncertainties on these comparison are larger than any observable systematic effects but are still small compared to the above uncertainties (1-3%).

9.2 Experimental and Detector Systematic Uncertainties

Experimental and detector systematic uncertainties affect the efficiencies of identifying objects and the efficiencies for events to pass our cuts. These uncertainties affect only MC models of physics processes, $t\bar{t}V$, $t\bar{t}H$, $VV$ and thus alter their number of expected events from
9. Summary of Systematic Uncertainties

signal and background in our signal regions. Data-driven backgrounds take into account these uncertainties by construction. We consider systematic effects from a number of sources: the lepton and jet energy scale measurements, the lepton identification and isolation selections, the efficiency and misidentification rate associated with tagging b-quark jets. Effects due to modeling the energy and objects from additional vertices were studied and found to be negligible. The vast majority of the individual detector systematics effects are small. The sum total of the systematic effects are comparable to the overall normalization and cross-section uncertainties on some of the physics processes and is shown in Table 9.3.

9.2.1 Lepton Identification, Energy Scale, and Trigger

The electron\cite{51} and muon identification efficiencies\cite{84} are measured in data using Z boson and $J/\Psi$ control samples. They muon efficiencies are shown in Figure 9.2, while the electron efficiencies are shown in Figure 4.11. The uncertainty on the muon efficiencies are measured as functions of $\eta$ and $p_T$ and are generally less 1%. The uncertainty on the electron and muon efficiencies are also measured as functions of $\eta$ and $p_T$ and are at the 1% level for $p_T$ above 30 GeV, but become much larger 5-10% for the lower $p_T$ regimes. These translate into sub-1% level effects on the $t\bar{t}V$ and $t\bar{t}H$ event counts in the signal regions for the muons and 1% level effects for the electrons. The effects become more important with increasing numbers of leptons.

The electron\cite{85} and muon\cite{84} energy scale and resolution are also measured using the Z-boson control samples in data. The uncertainties related to the scale and resolution for the leptons affect the overall event acceptance through the lepton momentum cuts primary and have negligible impact on the event count uncertainties in the signal regions.

The efficiencies for muons and electrons to pass muon\cite{86} and electron triggers\cite{87} have been calculated with respect to the offline identification operating points using the Z boson
9. Summary of Systematic Uncertainties

control samples. They are in the range of 90% for electron triggers and 70% for muon triggers, owing to gaps in muon trigger coverage, and have 1% level uncertainties. When statistically combined for $2\ell$ SS, $3\ell$ and $4\ell$ lepton signal regions, the overall trigger efficiency is high and the uncertainties on the number of expected events is negligible.

### 9.2.2 Lepton Isolation and Impact Parameter

The isolation and impact parameter selections are specific to this analysis and are discussed in depth in Chapter 7. We calculated their combined efficiency with respect to the full lepton identification selection using the $Z$ boson control samples and define data-MC scale factors to correct the efficiency in the simulation. Background are subtracted using shape templates in the di-lepton invariant mass spectrum. The $Z$-event template is derived from MC, while the background template is derived from the same-sign control region. We measure the efficiency scale-factors in bins of lepton momentum. Uncertainties are assigned per-bin to account for the level of statistics and variations caused by the fit parameters. An additional 1% uncertainty
9. Summary of Systematic Uncertainties

envelope is added to both the electron and muon measurements to account for trends observed in the dependence of the data-MC efficiency scale-factor as a function of the number of jets. Stability of the efficiency scale-factor as a function of the number of jets is important for this analysis, because event activity in the low jet $Z$ sample, where the efficiency is measured, is much different from the high jet signal regions, where the efficiency is applied. The dependence of the scale-factor on the number of jets can be seen Figure 9.3. The isolation scale-factor uncertainties are around 1-3% depending on the particle momentum, but these uncertainties propagate to 2-5% (some of the largest) effects in the event counts in the signal regions. The uncertainties are more important in the regions with more leptons.

Figure 9.3: Muon (left) and electron (right) isolation efficiency scale-factors from the $Z$ control sample as a function of the number of jets in the event. An additional systematic uncertainty of 1% is added to encompass the variation in the number of jets variable.
9. Summary of Systematic Uncertainties

9.2.3 Jet Energy

The jet energy scale (JES) is calculated using a combination of data-based in-situ techniques, where jet transverse momentum is balanced with respect to a reference photon or a Z boson, as well as single particle test-stand studies\(^88\). Additional smaller effects are taken into account including the b-quark jet specific response, near-by jets, the effects of pile-up and an inter-calibration of similar \(\eta\) regions using di-jet events. These effects are measured in 2012 data. The JES systematic errors arises from numerous sources that are diagonalized into eigenvectors so that they can be combined in an uncorrelated way. The combined uncertainty is plotted in Figure 9.4 as a function of jet \(\eta\) and \(p_T\) and is the range 2-4\% for jets used in this analysis. The jet energy resolution is calculated in a similar way with slightly larger errors, 10\% \(^89\). The combined scale and resolution systematics are of non-negligible effects 6-7\% on the signal and background event counts in the signal regions.

![Figure 9.4](image.png)

Figure 9.4: JES systematic uncertainties as a function of jet \(\eta\) (for jets \(p_T > 25\) GeV) and \(p_T\) (for jets \(|\eta| < 0.4\)). The combined systematic uncertainty is shown with contributions from the largest sources.
9. Summary of Systematic Uncertainties

9.2.4 B-Tagged Jet Efficiency

The $b$-quark tagging efficiency must be calculated separately for charm, light and $b$-quarks. ATLAS uses three data based control regions: an inclusive jet sample for mistagged light quarks\textsuperscript{90}, the $t\bar{t}$ sample for $b$-quarks\textsuperscript{91}, and a sample of $D^*$ mesons for charm quarks\textsuperscript{92}. These efficiencies and rates are well-measured in MC and the data-based corrections are small. The data-MC efficiency scale-factor shown in Figure 9.5 is close to 1 and has an overall systematic uncertainty of around 5%. The uncertainties are applied to the analysis via a number of eigenvectors. Together these uncertainties have a 4\% effect in the event expectation in the signal regions.

Figure 9.5: $b$-Tagging data-MC efficiency scale-factors versus jet $p_T$ calculated in the $t\bar{t}$ sample from 2012 data. The uncertainties are combined statistical and systematic.

9.2.5 Summary

The combined effect of these detector and experimental systematics on the $t\bar{t}V$ and $t\bar{t}H$ is provided in Table 9.3. The effects are smaller than the normalization uncertainties on some of the backgrounds. They are dominated by the lepton isolation scale-factor measurements and the electron identification with smaller contributions from the JES and $b$-tagging efficiencies. These detector systematic uncertainties enter the fit individually and the most important to the overall measurement uncertainty can be seen in Figure 10.7.
### 9. Summary of Systematic Uncertainties

<table>
<thead>
<tr>
<th>Total Systematic Uncertainty</th>
<th>2ee4j Down-Up</th>
<th>2ee5jincl Down-Up</th>
<th>2em4j Down-Up</th>
<th>2em5jincl Down-Up</th>
</tr>
</thead>
<tbody>
<tr>
<td>ttH</td>
<td>-4.68 5.84</td>
<td>-8.24 6.14</td>
<td>-5.10 3.50</td>
<td>-5.52 6.40</td>
</tr>
<tr>
<td>ttW</td>
<td>-7.20 5.45</td>
<td>-8.72 11.30</td>
<td>-3.63 6.22</td>
<td>-9.72 7.95</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Total Systematic Uncertainty</th>
<th>2mm4j Down-Up</th>
<th>2mm5jincl Down-Up</th>
<th>3ℓ Down-Up</th>
<th>4ℓ Down-Up</th>
</tr>
</thead>
<tbody>
<tr>
<td>ttH</td>
<td>-5.20 7.51</td>
<td>-7.28 6.75</td>
<td>5.59</td>
<td>-6.54 6.54</td>
</tr>
<tr>
<td>ttW</td>
<td>-4.54 5.23</td>
<td>-8.63 6.88</td>
<td>8.16</td>
<td>— —</td>
</tr>
<tr>
<td>ttZ</td>
<td>-5.24 8.69</td>
<td>-9.73 8.18</td>
<td>6.66</td>
<td>-9.58 6.94</td>
</tr>
</tbody>
</table>

Table 9.3: Sum in quadrature of all the systematic uncertainties on the number of event yields per channel.

### 9.3 Summary of Background and Signal Normalization Uncertainties

Table 9.4 gives the summary of the systematic uncertainties that are included in the analysis for the normalization and acceptance of each process. The relative importance of these uncertainties to the final fit can be seen in Figure 10.7.
### Summary of Systematic Uncertainties

<table>
<thead>
<tr>
<th>Type</th>
<th>Description</th>
<th>Uncertainty</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Signal (ttH)</strong></td>
<td>Cross Section (Dynamic Scale)</td>
<td>+3.8% –9.3%</td>
</tr>
<tr>
<td></td>
<td>Analyses Acceptance</td>
<td>0.2%</td>
</tr>
<tr>
<td><strong>PDF+αS</strong></td>
<td>Cross Section</td>
<td>± 8.1%</td>
</tr>
<tr>
<td></td>
<td>Analyses Acceptance</td>
<td>0.3-1.0%</td>
</tr>
<tr>
<td><strong>Parton Shower</strong></td>
<td>Analyses Acceptance</td>
<td>0.2-1.4%</td>
</tr>
<tr>
<td><strong>ttW (Irreducible background)</strong></td>
<td>Cross Section (Dynamic Scale)</td>
<td>± 15% (Section 8.1)</td>
</tr>
<tr>
<td></td>
<td>Analyses Acceptance</td>
<td>0.4-3.5%</td>
</tr>
<tr>
<td><strong>PDF+αS</strong></td>
<td>Cross Section</td>
<td>± 13%</td>
</tr>
<tr>
<td></td>
<td>Analyses Acceptance</td>
<td>1.1-4.8%</td>
</tr>
<tr>
<td><strong>Matching</strong></td>
<td>Analyses Acceptance</td>
<td>0.2-10%</td>
</tr>
<tr>
<td><strong>Modelling</strong></td>
<td>Analyses Acceptance</td>
<td>0.1-15.6%</td>
</tr>
<tr>
<td><strong>Parton Shower</strong></td>
<td>Analyses Acceptance</td>
<td>2.4-13.0%</td>
</tr>
<tr>
<td><strong>ttZ (Irreducible background)</strong></td>
<td>Cross Section (Dynamic Scale)</td>
<td>± 12% (Section 8.1)</td>
</tr>
<tr>
<td></td>
<td>Analyses Acceptance</td>
<td>0.1-3.1%</td>
</tr>
<tr>
<td><strong>PDF+αS</strong></td>
<td>Cross Section</td>
<td>± 9%</td>
</tr>
<tr>
<td></td>
<td>Analyses Acceptance</td>
<td>0.9-2.7%</td>
</tr>
<tr>
<td><strong>Matching</strong></td>
<td>Analyses Acceptance</td>
<td>0.5-16%</td>
</tr>
<tr>
<td><strong>Modelling</strong></td>
<td>Analyses Acceptance</td>
<td>3.5-10.5%</td>
</tr>
<tr>
<td><strong>Parton Shower</strong></td>
<td>Analyses Acceptance</td>
<td>2.4-13.0%</td>
</tr>
<tr>
<td><strong>VV Backgrounds</strong></td>
<td><strong>Normalization Uncertainty</strong> W^{±}Z, ZZ Processes</td>
<td>± 50% (Section 8.2)</td>
</tr>
<tr>
<td><strong>Data-Driven Backgrounds</strong></td>
<td><strong>Normalization Uncertainty</strong> Jet Fakes</td>
<td>± 30-50% (Section 8.4)</td>
</tr>
<tr>
<td></td>
<td><strong>Normalization Uncertainty</strong> Charge MisID</td>
<td>± 30-40% (Section 8.3)</td>
</tr>
</tbody>
</table>

Table 9.4: Summary of systematic uncertainties for processes present in the signal regions in the analysis, with their type, description, name, values and uncertainties, and status of inclusion in the final results.
Chapter 10

Results and Statistical Model

The predicted number of background and signal events and the observed data for each of the signal regions (including sub-channels) are provided in Table 10.1. We observe an excess of events in many of the $2\ell$ and $3\ell$ channels over the expected background. We provide a preliminary measurement of $\mu$, which is a ratio of the observed $t\bar{t}H$ production rate to the predicted SM production rate. We also interpret the results as a 95% exclusion level on possible $\mu$ values. The statistical model used to make these measurements is discussed in depth below.

Table 10.1: Results in the $2\ell$, $3\ell$, and $4\ell$ signal regions with flavor and jet sub-channels for $2\ell$ and SFOS and non-SFOS sub-channels for $4\ell$. The results included only statistical normalization

<table>
<thead>
<tr>
<th>$2\ell$ SS</th>
<th>$t\bar{t}H$</th>
<th>$t\bar{t}V$</th>
<th>$t\bar{t}Z$</th>
<th>VV</th>
<th>Fakes</th>
<th>QMis</th>
<th>Sum Background</th>
<th>Data</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>6.74 ± 0.0</td>
<td>31.00 ± 1.0</td>
<td>1.39 ± 0.2</td>
<td>5.30 ± 2.6</td>
<td>24.63 ± 4.3</td>
<td>4.87 ± 1.0</td>
<td>67.41 ± 6.6</td>
<td>98</td>
</tr>
<tr>
<td>3ee4j</td>
<td>0.95 ± 0.9</td>
<td>2.86 ± 0.3</td>
<td>0.20 ± 0.3</td>
<td>0.89 ± 0.4</td>
<td>3.45 ± 1.7</td>
<td>1.82 ± 0.3</td>
<td>9.22 ± 1.8</td>
<td>9</td>
</tr>
<tr>
<td>2e5jincl</td>
<td>0.74 ± 0.1</td>
<td>2.86 ± 0.3</td>
<td>0.13 ± 0.2</td>
<td>0.60 ± 0.2</td>
<td>2.33 ± 2.0</td>
<td>1.11 ± 0.2</td>
<td>6.63 ± 2.1</td>
<td>10</td>
</tr>
<tr>
<td>2em4j</td>
<td>1.18 ± 0.1</td>
<td>7.90 ± 1.0</td>
<td>0.59 ± 0.2</td>
<td>1.78 ± 0.2</td>
<td>12.33 ± 1.5</td>
<td>1.29 ± 0.2</td>
<td>25.17 ± 2.1</td>
<td>26</td>
</tr>
<tr>
<td>2em5jincl</td>
<td>2.17 ± 0.2</td>
<td>7.21 ± 0.9</td>
<td>0.29 ± 0.2</td>
<td>0.64 ± 0.2</td>
<td>6.66 ± 1.2</td>
<td>0.85 ± 0.2</td>
<td>17.84 ± 1.7</td>
<td>22</td>
</tr>
<tr>
<td>2mm4j</td>
<td>0.76 ± 0.0</td>
<td>5.63 ± 0.7</td>
<td>0.23 ± 0.0</td>
<td>0.56 ± 0.1</td>
<td>6.32 ± 1.3</td>
<td>0</td>
<td>12.62 ± 1.9</td>
<td>20</td>
</tr>
<tr>
<td>2mm5jincl</td>
<td>1.44 ± 0.1</td>
<td>4.94 ± 0.6</td>
<td>0.14 ± 0.0</td>
<td>0.83 ± 0.2</td>
<td>2.89 ± 0.9</td>
<td>0</td>
<td>8.58 ± 1.2</td>
<td>11</td>
</tr>
<tr>
<td>$3\ell$</td>
<td>2.39 ± 0.3</td>
<td>6.66 ± 0.8</td>
<td>0.58 ± 0.1</td>
<td>1.81 ± 0.3</td>
<td>2.62 ± 0.5</td>
<td>0</td>
<td>11.57 ± 1.3</td>
<td>18</td>
</tr>
<tr>
<td>$4\ell$</td>
<td>0.20 ± 0.1</td>
<td>0.35 ± 0.1</td>
<td>0.07 ± 0.0</td>
<td>0.03 ± 0.0</td>
<td>0.03 ± 0.0</td>
<td>0</td>
<td>0.07 ± 0.0</td>
<td>1</td>
</tr>
</tbody>
</table>

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10. Results and Statistical Model

10.1 Results in Signal Regions

Plots of event variables are shown in Figures 10.1 - 10.2 for the 2\(\ell\) SS signal region and Figures 10.3 - 10.4 for the 3\(\ell\) signal. The 4\(\ell\) regions have too few events to be informative. Likewise, the statistics of the backgrounds models are too poor in the sub-channels of the 2\(\ell\) signal region. The results are shown instead for the inclusive 2\(\ell\) signal region. The charge misidentification and fake backgrounds take their normalizations from the measurements in Chapter 8, while their shapes are directly from MC. The plots show the combined statistical uncertainties and systematic uncertainties from theory and background normalization as well as experimental and detector effects.

10.2 Statistical Model

We use the above results to make two sets of measurements: an upper confidence limit on \(\mu\), the signal strength parameter, and a measurement of \(\mu\). These measurements are done for each channel individually and then combined. The interpretation of the results in the form of a statistical model follow the procedure, discussed here [93]. We interpret the results as counting experiments in each signal region. Therefore agreement in kinematic shapes do not affect the statistical procedure.

10.2.1 The Likelihood

The observed and expected event yields in the signal regions are analyzed using a binned likelihood function (\(\mathcal{L}\)), built from product of Poisson models of expected event counts for each bin, where the bins are the separate signal regions:

\[
\mathcal{L} \propto \prod_{i=0}^{N_{SR}} P(N_{obs}^{i}| \mu \cdot s_{\exp}^{i} + b_{\exp}^{i})
\]  

(10.1)
Figure 10.1: Distributions for combined 2-lepton signal region without hadronic taus. Jet and b-tagged jet multiplicities (top row); $10\times n(\text{b-tags})+n(\text{jets})$ and electron multiplicity (middle row); scalar sum of the $p_T$ of selected leptons and jets in the event (bottom left) and only of leptons (bottom right).
Figure 10.2: Distributions for combined 2-lepton signal region without hadronic taus. Leading and sub-leading lepton $p_T$ (top); leading jet $p_T$ and $\eta$ (middle right); scalar sum of the $p_T$ of selected jets in the event (bottom left) and only of b-tagged jets (bottom right).
10. Results and Statistical Model

Figure 10.3: Jet and b-tagged jet multiplicities (top row); $10^n(b\text{-tags})+n(jets)$ and electron multiplicity (middle row); invariant mass of opposite sign lepton pairs; scalar sum of the $p_T$ of selected leptons and jets in the event (bottom left) and only of leptons (bottom right).
Figure 10.4: Lepton 0 $p_T$ (top left) and lepton 1 $p_T$ (top right); lepton 2 $p_T$ (middle left) and leading jet $p_T$ (middle right); scalar sum of the $p_T$ of selected jets in the event (bottom left) and only of b-tagged jets (bottom right). Lepton 0 is the one with opposite charge with respect to lepton 1 and 2, where lepton 2 has lower $p_T$ than lepton 1.
where $s^i_{\text{exp}}$ is the SM signal expectation in the signal region, $b^i_{\text{exp}}$ are the background expectations, $i$ counts over the signal regions, and $P$ is the Poisson distribution. The signal strength parameter is the parameter of interest in the model (POI) and acts as a simple scale-factor to the SM $t\bar{t}H$ production rate and is common to all channels. Setting $\mu$ to 0 corresponds to the background only scenario. The background parameter, $b$, is a sum over all background processes.

The signal and background expectations, $s$ and $b$, depend on systematic errors. These are included in the likelihood function in the form of a vector nuisance parameters, $\vec{\theta}$, which are constrained to fluctuate within Gaussian distributions. These fluctuations affect the back-
ground and signal expectations by response functions, \( \nu(\theta) \), set by systematic uncertainties measured in the previous section. For instance, the \( W^\pm Z \) normalization uncertainty is 50\% from Section 8.2 and is included in the fit as its own unit Gaussian, \( G(\theta | 0, 1) \). The fluctuations of the Gaussian, \( \theta_{WZ} \), scale the background contribution via the form, \( 0.5 \cdot (1 + \theta_{WZ}) \cdot b_{WZ} \). For many of the detector systematics, the uncertainties are two sided and are included as piecewise Gaussians. We add correlations to various uncertainties by hand, when appropriate. With these nuisance parameters, the likelihood takes this form:

\[
L(\mu, \tilde{\theta}) = \left( \prod_{i=0}^{N_{ch}} P(N_{obs}^i, \mu, \nu_s(\theta) \cdot s_{exp}^i + \nu_b(\theta) \cdot b_{exp}^i) \right) \times \prod_{j} G(\theta_j | 1, 0) \tag{10.2}
\]

### 10.2.2 Test Statistic and Profile Likelihood

Values of \( \mu \) are tested with the negative log quantity, \( q_\mu = -2 \ln(\lambda(\mu)) \), where \( \lambda(\mu) \) is the test statistic. \( \lambda(\mu) \) is defined as:

\[
\lambda(\mu) \equiv \frac{L(\mu, \hat{\theta}_\mu)}{L(\hat{\mu}, \hat{\theta})} \tag{10.3}
\]

where \( \hat{\theta}_\mu \) are values of the nuisance parameter vector that maximize the likelihood for a given value of \( \mu \) and \( \hat{\mu} \) and \( \hat{\theta} \) are the fitted values of signal strength and nuisance parameters that maximize the likelihood overall. \( \mu \) is constrained to be positive.

### 10.2.3 CL\(_s\) Method

Exclusions limits on the signal strength are calculated with the test statistic using a modified frequentist method, called the CL\(_s\) method\[94\]. CL\(_s\) is defined as a ratio of two frequentist quantities. The numerator quantifies the probability of finding the observed data given the signal + background hypothesis. The denominator quantifies the probability of the data given the background only hypothesis.
10. **Results and Statistical Model**

Using the numerator alone has the undesirable property that, if the data fluctuates below the expectation, an exclusion limit can be reached that is far beyond the sensitivity of the experiment. Normalizing to the background only hypothesis penalizes these low sensitivity cases.

The probability of obtaining an observation as extreme as the data given a particular signal + background hypothesis is given by the p-value, \( p_\mu \) defined as:

\[
p_\mu = \int_{q_\mu}^{\infty} f(q_\mu) dq_\mu
\]

(10.4)

and the probability of obtaining an observation as extreme as the data given the background hypothesis, \( p_b \) is:

\[
p_b = \int_{q_\mu=0}^{\infty} f(q_\mu=0) dq_\mu=0
\]

(10.5)

where \( f(q_\mu) \) is the distribution of \( q_\mu \) for all possible observations for a given \( \mu \) and \( q \) is defined above. Therefore,

\[
CL_s = \frac{p_\mu}{1 - p_b}
\]

(10.6)

A \( \mu \) value is considered excluded at 95% confidence when \( CL_s \) is less than 5%.

### 10.2.4 Exclusion Limits

Figure 10.6 and table 10.2 show the expected and observed exclusion limits for all channels.

<table>
<thead>
<tr>
<th></th>
<th>Expected Limit</th>
<th>Expected SM Signal Injected Limit</th>
<th>Observed Limit</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Combined</strong></td>
<td>2.55</td>
<td>3.42</td>
<td>5.50</td>
</tr>
<tr>
<td><strong>2\ell SS</strong></td>
<td>3.58</td>
<td>4.51</td>
<td>6.50</td>
</tr>
<tr>
<td><strong>2\ell ee</strong></td>
<td>8.95</td>
<td>9.81</td>
<td>12.62</td>
</tr>
<tr>
<td><strong>2\ell em</strong></td>
<td>4.89</td>
<td>5.82</td>
<td>7.84</td>
</tr>
<tr>
<td><strong>2\ell mm</strong></td>
<td>5.30</td>
<td>6.22</td>
<td>8.30</td>
</tr>
<tr>
<td><strong>3\ell</strong></td>
<td>3.67</td>
<td>4.65</td>
<td>6.86</td>
</tr>
<tr>
<td><strong>4\ell</strong></td>
<td>14.89</td>
<td>16.45</td>
<td>18.05</td>
</tr>
</tbody>
</table>
10. Results and Statistical Model

Figure 10.6: Plot of the $2\ell$ SS, $3\ell$, $4\ell$, and combined 95% CLs observed limits on $\mu$. The expected 1-$\sigma$ (green) and 2-$\sigma$ (yellow) error bands are shown around the expected limit. The expected limit with SM signal injection ($\mu = 1$) is included as well.

10.2.5 $\mu$ Measurement

In addition to setting a limit on the signal strength, we also fit the best value of the signal strength for $\mu$. We do this by minimizing the negative log likelihood value, $q_{\mu}$, or conversely maximizing the likelihood. The 1-$\sigma$ error band is set via a profile likelihood scan, where the value $q_{\mu}$ is scanned as a function of $\mu$. Values of $\mu$ that increase $q_{\mu}^{\text{min}}$ by 1 form the edges of the error band. The fitted value of $\mu$ for all channels separately and combined is shown in Figure 10.3. The overall uncertainty derives almost equally from statistical and systematic uncertainties.
10. Results and Statistical Model

<table>
<thead>
<tr>
<th>Channels</th>
<th>( \mu ) value</th>
<th>stat</th>
<th>syst</th>
<th>tot</th>
</tr>
</thead>
<tbody>
<tr>
<td>2l</td>
<td>2lee</td>
<td>3.74</td>
<td>+3.89</td>
<td>+4.75</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>−3.25</td>
<td>−4.06</td>
</tr>
<tr>
<td></td>
<td>2lem</td>
<td>2.97</td>
<td>+2.09</td>
<td>+2.77</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>−1.83</td>
<td>−2.41</td>
</tr>
<tr>
<td></td>
<td>2lmm</td>
<td>2.68</td>
<td>+2.61</td>
<td>+3.20</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>−2.22</td>
<td>−2.67</td>
</tr>
<tr>
<td></td>
<td>All</td>
<td>2.85</td>
<td>+1.47</td>
<td>+2.15</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>−1.35</td>
<td>−1.86</td>
</tr>
<tr>
<td>3l</td>
<td></td>
<td>2.93</td>
<td>+1.97</td>
<td>+2.19</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>−1.68</td>
<td>−1.79</td>
</tr>
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<td>4l</td>
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<td>1.83</td>
<td>+6.81</td>
<td>+6.91</td>
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<td>234l</td>
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<td>+1.58</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>−1.06</td>
<td>−1.35</td>
</tr>
</tbody>
</table>

Table 10.3: \( \mu \) measurement for all channels and their combination, with asymmetric minos errors. Statistical, systematics and total error are provided. Results are given on a fit to data for all channels.

10.2.6 Nuisance Parameter Impact on the Signal Strength

Finally, we examine the post-fit impact of the various nuisance parameters in Figure 10.7. The fake nuisance parameters are divided for 2\( \ell \) into the systematic uncertainty on the transfer factors for electrons and muons (\( \alpha_{\text{Theta}_{mm}} \), \( \alpha_{\text{Theta}_{ee}} \)) and the systematic uncertainties on the number of events in the anti-tight control regions (e.g. \( \alpha_{\text{Fakes}_{2lem5j}} \)). The 3\( \ell \) fake uncertainties are contained in a single parameter (\( \alpha_{\text{Fakes}_{3l}} \)). The theory cross-section (XS) uncertainties are divided into PDF and scale nuisance parameters separately for each background (\( t\bar{t}W^\pm, t\bar{t}Z, t\bar{t}H \)). The most important nuisance parameters associated with the detector and experimental uncertainties are the JES, the b-tag scale-factor weights, and the lepton isolation.

We have measured the various analysis uncertainties well and do not expect the fit to have much further constraint. For that reason, we expect the pulls of the nuisance parameters to be
10. Results and Statistical Model

close to 0 and the measured uncertainties on those parameters to be consistent with the input uncertainties. This is true for all but the 4$\ell$ fake transfer factor which is pulled slightly high by the excess in the $\mu$ channels. The pull is well within the uncertainty. The uncertainties that dominate this fit are those associated with the $t\bar{t}V$ cross-section and the fake estimates.

Figure 10.7: Figure of the post- and pre-fit impacts of the top nuisance parameters on the combined $\mu$ measurements

10.3 Discussion of Results and Significance of the Excess

The results show an overall excess of events over the background-only hypothesis. An excess is observed in both the 2$\ell$ and 3$\ell$ channels. However, the excess is not a considered significant enough to warrant an observation of new physics.

A first suspicion would be that two dominant backgrounds are not well modeled: $t\bar{t}V$ and
fake. The fake backgrounds from top have been validated in low jet control regions, and the extrapolation to higher number of jets is constrained by simulation. The anti-tight control regions, shown in Chapter 8, which are enriched in fake events do not show a similar shape to the excesses in the tight signal regions. The $t\bar{t}V$ cross-section is constrained only by theoretical methods and the $t\bar{t}Z$ validation region used does show an excess of data events. A rescaling of the $t\bar{t}V$ by the data/MC ratio show in the $t\bar{t}Z$ validation regions would not explain the size or shape of the excess, though the significance of the excess would decrease. The $t\bar{t}Z$ validation region excess is compatible with a statistical fluctuation of the backgrounds, as discussed in Section 8.1. Indeed, an public ATLAS measurement of the $t\bar{t}Z$ rate in this 3$\ell$ region shows a deficit of events \cite{95} using the same MC models. It is therefore not clear that re-scaling the $t\bar{t}V$ cross-section is warranted.

The overall excess of events has peculiar properties: it is found predominantly in events with a large number of jets and b-tagged jets. For the 2$\ell$ channel, the excess is found primarily in the $\mu\mu$ and $e-\mu$ flavor bins. Events with large numbers of b-tagged jets and flavor asymmetry are difficult to describe with the standard model backgrounds, even including a standard model Higgs hypothesis. The high $p_T$ scale of the excess for sub-leading leptons suggest that the fakes are well understood and the agreement in the 1 b-tagged jet bin suggest that the combined $t\bar{t}V$ and fakes are under control.
This thesis has presented a preliminary search for the $t\bar{t}H$ process in multilepton final states using the 2012 8 TeV dataset, collected by ATLAS. The signal regions, which are binned in number of leptons, show an interesting excess of events. The level of excess is not large enough to claim statistically significant observation of a new process, whether SM $t\bar{t}H$ production or otherwise. As a result, we proceed by setting a 95% confidence limit on the $t\bar{t}H$ production rate compared to the SM production, which is much less strict than expected and provide a fitted value of $\mu$, the ratio of the observed production rate to the theoretical SM $t\bar{t}H$ production rate.

We believe the background processes are well-measured via simple and straightforward procedures. These procedures either rely on or are verified by data control and validation regions surrounding the signal regions. The good data-MC agreement in these regions suggests that the data excesses are characteristic of the signal regions only and that the background processes are well-understood within the systematic uncertainties assigned.

The signal regions are constructed with simple selection criteria, requiring only certain number of leptons, jets, and $b$-tagged jets within standard acceptance criteria. Additional selection criteria, namely vetoes of dilepton invariant mass ranges, are well motivated by the removal of backgrounds involving $Z$ resonance production. The selection criteria and
background measurement procedures were set prior to viewing the data in the signal region.

This analysis shares parts of signal regions with other ATLAS super-symmetric and exotic analyses, which are under internal review. If similar excesses are seen in these analyses, it will provide some cross-check to the \( \bar{t}tH \) analysis, which is done with a different procedure for assessing fake background contributions.

This multilepton analysis will be combined with the already public \( H \rightarrow b\bar{b} \) \[^{57}\] and \( H \rightarrow \gamma\gamma \) \[^{58}\] analysis, which have observed(expected) 95\% confidence limits on \( \mu \) of 4.1(2.6) and 4.9(6.7), respectively. Both have seen small, non-significant excesses with fitted \( \mu \) values of \( 1.7 \pm 1.4 \) and \( 1.3 + 2.62 - 1.75 \), respectively. When approved, the multilepton analysis will be combined with other analyses in fit constraining the parameters of the Higgs sector.

As it is primarily dependent on the top Yukawa coupling and Higgs coupling to W bosons, it will have the greatest effect on the measurement of these parameters.

It is interesting to note that the CMS experiment observes a similar excess in their multilepton search for \( \bar{t}tH \) production. Their observed(expected) 95\% limit on \( \mu \) is 6.6(2.4) and their fitted value of \( \mu \) is \( 3.7 + 1.6 - 1.4 \) \[^{96}\].

Observing \( \bar{t}tH \) production is really a task for the second LHC run. The increased luminosity and collision energy (13 TeV) will ensure that the \( \bar{t}tH \) process is observed with that run’s dataset \[^{19}\]. The overall cross-section of \( \bar{t}tH \) production will increase by a factor of roughly 4, due to accessing more of the gluon PDFs in the collisions. The cross-sections of most of the backgrounds (\( \bar{t}tV \) and top fakes) will also increase by this factor, but the increase in the signal cross-section is more important: the second run dataset will have twice the sensitivity to \( \bar{t}tH \) per amount of collected data. While there will likely not be any conclusive resolution of the excesses found in the multilepton signal regions with the first run dataset, the second run dataset will surely shed light on this issue.


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