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Consistency in a Partitioned Network: A Survey

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Abstract
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Comments

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CONSISTENCY IN A PARTITIONED NETWORK: A SURVEY

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ABSTRACT

Recently, several strategies for transaction processing in partitioned distributed database systems with replicated data have been proposed. We survey these strategies in light of the competing goals of maintaining correctness and achieving high availability. Extensions and combinations are then discussed, and guidelines for the selection of a strategy for a particular application are presented.

INTRODUCTION

In a distributed database system, data is often replicated to improve performance and

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availability. By storing copies of shared data on processors where it is frequently accessed, the need for expensive, remote read accesses is decreased. By storing copies of critical data on processors with independent failure modes, the probability that at least one copy of the data is accessible increases. Through replication, it is possible, in theory, to provide arbitrarily high data availability.

In practice, realizing the benefits of data replication is difficult since the correctness of data must be maintained. One important aspect of correctness with replicated data is that of mutual consistency: all copies of the same logical data-item must agree on exactly one "current value" for the data-item. Furthermore, this value should "make sense" in terms of the transactions executed on copies of the data-item. This agreement process is obviously complicated when communication between sites containing copies of the same logical data-item fails. The most disruptive of these failures are partition failures, communication failures that fragment the network into isolated subnetworks, called partitions. Unless detected and recognized by all affected processors, such failures provide the opportunity for independent, uncoordinated updates to be applied to different copies of the data, thereby compromising the correctness of data. Consider, for example, an Airline Reservation System implemented by a distributed database that splits into two partitions as the result of a failure in the communication network. If at the time of the failure all the nodes have one seat remaining for PAN AM 537, and reservations are made in both partitions, correctness has been violated: who should get the last seat? There should not be more seats reserved for a flight than physically exist on the plane. (Some airlines do not implement this constraint and allow overbookings.)

The design of a replicated data management algorithm tolerating partition failures is a notoriously hard problem. Typically, the cause or extent of a partition failure can not be discerned by the processors themselves. At best, a processor may be able to identify the other processors in its partition; but, for the processors outside of its partition, it will not be able to distinguish between the case where those processors are simply isolated from it and the case where those processors are down. In addition, slow responses from certain processors can
cause the network to appear partitioned even when it is not, further complicating the design of a fault-tolerant algorithm.

As far back as 1977, Rothnie and Goodman in their well-known survey paper [ROGO77] identified partitioned operation as one of the important and challenging open issues in distributed data management. Since then our understanding of the problem has increased dramatically, while numerous and diverse solutions have been proposed. In this paper, we survey several of the more general solutions, and discuss current research trends in this still young and active research area.

Although our discussion is couched within a database context, most results have more general applications. In fact, the only essential notion in many cases is that of a transaction. Hence, these strategies are immediately applicable to mail systems, calendar systems, object-oriented systems—applications using transactions as their underlying model of processing.

The remaining sections of the survey are organized as follows. Section 1 discusses the principal consideration in the design of a processing strategy for a partitioned system, the trade-off between correctness and availability. Section 2 discusses the notion of correctness in a replicated database system, and introduces a taxonomy of partition processing algorithms. Sections 3 and 4 survey the current solutions for transaction processing while the system is partitioned, and suggest extensions and combinations. Section 5 discusses a somewhat different problem: how to complete transactions in progress at the time of a partition failure. Guidelines for the selection of a partition strategy are presented in section 6, along with suggestions for future research.

1. CORRECTNESS VERSUS AVAILABILITY

When designing a system which is to operate in the presence of partitioning, the two competing goals of availability—the normal function of the system should be disrupted as little as possible—and correctness—data must be correct when recovery is complete—must somehow be met. These goals are not independent; hence, trade-offs are involved.
Correctness can be achieved simply by suspending operation in all but one of the partition groups and forwarding updates at recovery; however availability has been severely compromised. In some applications, this is not acceptable. Typically in these applications either partitions occur frequently or occur at critical moments when access to the data is imperative. For example, in the Airline Reservation System it may be too expensive to have a high connectivity network and partitions may occasionally occur. Many transactions are executed each second (TWA's centralized reservations system [GISP84] estimates 170 transactions per second at peak time), and each transaction that is not executed may represent the loss of a customer. In a military command and control application, a partition can occur because of an enemy attack, and it is precisely at this time that we do not want transaction processing halted.

On the other hand, availability can be achieved simply by allowing all nodes to process transactions "as usual" (note that transactions can only execute if the data they reference is accessible). However, correctness may now be compromised. Transactions may produce "incorrect" results (e.g., reserving more seats than physically available) and the databases in each group may diverge. In some applications, such "incorrect" results may be acceptable in light of the higher availability achieved: when partitions are reconnected, the problems may be corrected by executing transactions missed by a partition, and by choosing certain transactions to "undo." If the chosen transactions have had no real worlds effects, they can be undone using standard database recovery methods. If, on the other hand, they have had real world effects, then appropriate compensating transactions must be run, transactions that not only restore the values of the changed database items but also issue real world actions to nullify the effects of the chosen transactions (e.g., by canceling certain reservations and sending messages to affected users). Alternatively, correcting transactions can be run, transforming the database from an incorrect state to a correct state without undoing the effects of any previously ran transactions. For instance, in a banking application the correction for overdrawing a checking account during a partitioning is the application of an overdraft charge. Of course, in
some applications incorrect results are either unacceptable or incorrectable. For example, it may not be possible to undo or correct a transaction that effectively hands $1,000,000 to a customer.

Since it is clearly impossible to satisfy both goals simultaneously, one or both must be relaxed to some extent depending on the application's requirements. Relaxing availability is fairly straightforward; one simply disallows certain transactions at certain sites. Relaxing correctness, on the other hand, usually requires extensive knowledge about what the information in the database represents, how applications manipulate the information, and how much undoing/correcting/compensating inconsistencies costs. The first step in choosing a partition processing strategy is to determine which is more important—correctness or availability; the second step is to try understand the trade-offs between the two properties for the database at hand.

2. THE NOTION OF CORRECTNESS

What does correct processing mean in a database system? Informally, a database is correct if it correctly describes the external objects and processes that it is intended to model. In theory, such a vague notion of correctness could be formalized by a set of static constraints on objects and their attributes and a set of dynamic constraints on how objects can interact and evolve. In practice, the complete specification of the constraints governing even a small database is impractical (besides, even if it were practical, the enforcement of the constraints would not be). Consequently, database systems enforce a less ambitious, very general notion of correctness based on the order of transaction execution and on a small set of static data constraints, known as integrity constraints.

In this section, we examine the notion of correctness, beginning informally with examples illustrating incorrect behavior, followed by a more formal definition of correctness in the traditional database system. When referring to the state of the database, we use the terms "correct" and "consistent" interchangeably.
2.1. Anomalies

Consider a banking database that contains a checking account and a savings account for a certain customer, with a copy of each account stored at both Site A and Site B. Suppose a communications failure isolates the two sites. Figure 1 shows the result of executing a checking withdrawal at A (for $100) and two checking withdrawals at B (totaling $100).

<table>
<thead>
<tr>
<th>SITE A</th>
<th>SITE B</th>
</tr>
</thead>
<tbody>
<tr>
<td>Checking: $100</td>
<td>Checking: $100</td>
</tr>
<tr>
<td>Savings: $200</td>
<td>Savings: $200</td>
</tr>
</tbody>
</table>

\[
\begin{align*}
\text{Checking} & := \text{Checking} - $100 \\
\text{Checking} & := \text{Checking} - $25 \\
\text{Checking} & := \text{Checking} - $75 \\
\text{Checking} & := 0 \\
\text{Savings} & := 200
\end{align*}
\]

Fig. 1 An anomaly due to concurrent write operations on the same data item in separate partitions.

Although the resulting copies of the checking account contain the same value, we know intuitively that the actions of the system are incorrect—the account owner extracted $200 from a checking account containing only $100. The anomaly is caused by a conflicting write operations issued in parallel by transactions executing in different partitions.

An interesting aspect of this example is that in the resulting database all copies are mutually consistent\(^1\), i.e., all copies of a data item contain the same value. Mutual consistency is not a sufficient condition for correctness in a (transaction-oriented) database system, although it commonly used the correctness criterion for replicated file systems and for information databases, such as telephone directories. It is also not a necessary condition: consider the example where A executes the $100 withdrawal while B does nothing. Although the resulting copies of the checking account contain different values, the resulting database is

---

\(^1\) This is the narrowest interpretation of several uses of the term "mutual consistency" that appear in the literature. Some authors use mutual consistency synonymously with one-copy equivalence (defined in the next section).
correct if the system recognizes that the value in A's copy is the most recent one.

A different type of anomaly on the same database is illustrated in Figure 2. Here, we assume that the semantics of the checking withdrawal allow the account to be overdrawn as allowed as long as the overdraft is covered by funds in the savings account (i.e., checking + savings ≥ 0).

<table>
<thead>
<tr>
<th>SITE A</th>
<th>SITE B</th>
</tr>
</thead>
<tbody>
<tr>
<td>Checking: $100</td>
<td>Checking: $100</td>
</tr>
<tr>
<td>Savings: $200</td>
<td>Savings: $200</td>
</tr>
</tbody>
</table>

If checking + savings > $200
then checking := checking − $200

If checking + savings > $200
then savings := savings − $200

| Checking: $100 |
| Savings: $200 |
| Checking: $100 |
| Savings: $0 |

Fig. 2 An anomaly due to concurrent read and write operations in different partitions.

In the execution illustrated, however, these semantics are violated: $400 is withdrawn, whereas the accounts together contain only $300. The anomaly was not caused by conflicting writes (none existed since the transactions updated different accounts), but instead because accounts are allowed to be read in one partition and updated in another.

Concurrent reads and writes in different partitions are not the only sources of inconsistencies in a partitioned system—more will be identified shortly. Nor do they always cause inconsistencies: for example, if the savings withdrawal in Figure 2 is changed to a deposit, the intended semantics of the database would not be violated. However, the above are typical anomalies that can occur if conflicting transactions are executed in different partitions.

2.2. Database Model

A database is a set of logical data items that support the basic operations read and write. The granularity of these items is not important: they could be records, files, relations, etc.
The state of the database is an assignment of values to the logical data items. For brevity, logical data items are subsequently called data items or, more simply, items.

A transaction is a program that issues read and write operations on the data items. In addition, a transaction may have effects that are external to the database, such as dispensing money or displaying results on a user's terminal. The items read by a transaction constitute its readset; the items written, its writeset. A readonly transaction neither issues write requests nor has external effects. Transactions are assumed to be correct. More precisely, a transaction, when executed alone, transforms an initially correct database state into another correct state [TGGL82].

Transactions interact with one another indirectly by reading and writing the same data items. Two operations on the same item are said to conflict if at least one of them is a write. Conflicts are often labeled either read-write, write-read, or write-write depending on the types of data operations involved and their order of execution [BEGO81]. Conflicting operations are significant because their order of execution affects the final database state.

A generally accepted notion of correctness for a database system is that it executes transactions so that they appear to users as indivisible, isolated actions on the database. This property, referred to as atomic execution, is achieved by guaranteeing the following properties:

1. The execution of each transaction is an "all or nothing": either all of the transaction's writes and external operations are performed or none are performed. In the former case the transaction is said to be committed; in the latter case, aborted. The property is often referred to as atomic commitment.

2. The execution of several transactions concurrently produces the same database state as some serial execution of the same transactions. The execution is then said to be serialisable.

The first property is established by the commit and recovery algorithms of the database system; the second, by the concurrency control algorithm.
Atomic transaction execution together with the aforementioned correctness-preserving assumption imply that the execution of any set of transactions transforms an initially correct database state into a new, correct state. (This follows from a simple induction argument on the number of transactions.) Of course, atomic execution is not always necessary to preserve correctness (we explore this more later on). Nonetheless, most real database system implement it as their sole correctness criteria because of its simplicity and generality. Atomic execution can be enforced by very general mechanisms that carefully order the execution of conflicting data operations, mechanisms that are independent of the semantics of the data being stored and of the transactions manipulating it. Moreover, atomic execution corresponds to most users' intuitive model of processing—that of sequential processing.

Some systems allow additional correctness criteria to be expressed in the form of integrity constraints. Unlike atomicity, these are semantic constraints. They may range from simple constraints—e.g. the balance of checking accounts must be nonnegative—to elaborate ones that relate the values of many data items. In systems enforcing integrity constraints, a transaction is allowed only if its execution is atomic and its results satisfy the integrity constraints. To simplify the discussion, throughout the rest of the paper we will assume that integrity constraints are checked as part of the normal processing of a transaction.

Notice that we have not specified whether we were discussing a centralized or a distributed database system—it has not been necessary to do so since the definitions, the properties of transaction processing, and the correctness criteria are the same in both. Of course, the algorithms for achieving correct transaction processing differ markedly between the two types of implementations.

In a replicated database, the value of each logical item \( x \) is stored in one or more physical data items, which are referred to as the copies of \( x \). Each read and write operation issued by a transaction on some logical data item must be mapped by the database system to corresponding operations on physical copies. To be correct, the mapping must ensure that the concurrent execution of transactions on replicated data is equivalent to a serial execution on nonreplicated
data, a property known as \textit{one-copy serializability}. The logic that is responsible for performing this mapping is called \textit{the replica control algorithm}.

As a correctness criterion, one-copy serializability is attractive for the same reasons that (normal) serializability is: it is intuitive, and it can be enforced using general-purpose mechanisms that are independent of the semantics of the database and of the transactions executed.

The literature on the model and problems discussed above is extensive. The transaction concept was first introduced in [EGLL76]. A single-site recovery algorithm is presented in [GMBLL81]. Single-site concurrency control algorithms are too numerous to list, but three influential proposals are two-phase locking [EGLL76], timestamp ordering [BEGO80], and optimistic concurrency control [KURO81]. The seminal paper on serializability theory is [PAPA79]. [BLAU81] discusses the enforcement of integrity constraints. [GRAY78] contains an in-depth treatment of many issues in the implementation of a database system.

For nonpartitioned distributed database systems, concurrency control algorithms are surveyed in [BEGO81] and [KOHL81]. Atomic commitment protocols are discussed in [GRAY78], [HASH80], and [SKEE82]. Replica control algorithms are contained in [GIFF79], [STON79], and [GSCDFR83]. A good discussion of the requirements for maintaining one-copy serializability in the presence of failures can be found in [BEGO83].

\subsection{2.3. Partitioned Operation}

Let us now consider transaction processing in a partitioned network, where the communication connectivity of the system is broken by failures or by anticipated communication shutdowns. To keep the exposition simple, let us assume that the network is "cleanly" partitioned, that is, any two sites in the same partition can communicate and any two sites in different partitions can not communicate. Let us assume for now the traditional correctness criterion—\textit{one-copy serializability}.

During the time the system is partitioned, each partition must determine which transactions can be executed in that partition without violating the correctness criteria. Actually,
this can be thought of as two problems: the first is that each partition must maintain correctness within the part of the database stored at the sites comprising the partition, and the second is that each partition must make sure that its actions do not conflict with the actions of other partitions so that the database is correct across all partitions.

If we make the assumption that each site in the network is capable of detecting partition failures, then correctness within a partition can be maintained by adapting one of the standard replica control protocols for nonpartitioned systems. For example, the sites in a partition can implement a write operation on a logical object by writing all copies in the partition. This, along with a standard concurrency control protocol, ensures one-copy serializability in the partition.

The really difficult problem is ensuring one-copy serializability across partitions. For this, it is not sufficient to run just a correct replica control algorithm in each partition, as the examples in Figures 1 and 2 illustrate, where transaction execution within each partition is one-copy serializable, but the overall execution is not, because of the execution of conflicting operations in different partitions.

Numerous solutions have been proposed for keeping data globally consistent, and most of the remainder of the survey is devoted to discussing these solutions. Many of these solutions are based on the simple observation that a sufficient (but not necessary) condition for correctness is that no two partitions execute conflicting data operations. However, not all partition processing solutions use one-copy serializability as their correctness criteria, nor do all attempt to maintain correctness across partitions. We discuss these alternatives in the next section.

Although a partition processing strategy can be thought of as being composed of two algorithms: an algorithm to ensure correctness globally across partitions, and an replica control algorithm to ensure one-copy behavior, in practice, many strategies are composed of a single algorithm that solves both problems. Most “single” algorithms do not require partitions to be detected and tolerate more than just “clean” network failures. Such algorithms are attractive
for their additional fault tolerance. In the next sections, we present these "single algorithms", along with "partition control" algorithms. However, in both, we emphasis the partition control aspect.

In addition to solving the problem of global correctness, a partition processing strategy must solve two other problems of a different sort. First, when the partitioning occurs, the database is faced with the problem of atomically committing ongoing transactions. The complication is that the sites executing the transaction may find themselves in different partitions, and thus unable to communicate a decision regarding whether to complete the transaction (commit) or to undo it (abort). Note that the problem of atomic commitment in multiple partitions does not arise for a transaction submitted after the partitioning occurs, since such a transaction will be executed in only one partition. Note also that this problem arises in any partitioned database system whether the database is replicated or not.

Second, when partitions are reconnected, mutual consistency\(^2\) between copies in different partitions must be reestablished. That is, the updates made to a logical data object in one partition must be propagated to its copies in the other partitions. Conceptually, this problem can be solved in a straightforward manner by extra bookkeeping whenever the system partitions. For example, each update applied in a partition can be logged, and this log can be sent to other partitions upon reconnection. (Such a log may be integrated with the "recovery log" that is already kept by many systems.) In practice, an efficient solution to this problem is likely to be intricate and very dependent on the normal recovery mechanisms employed in the database system. For this reason, we do not discuss it further.

2.4. Classification of Strategies

Partition processing strategies can be classified along two orthogonal dimensions.

The first dimension concerns the trade-off between consistency and availability. At one extreme lies the pessimistic strategies, which prevent inconsistencies by limiting availability.

\(^2\)As before, by “mutual consistency” we that the copies contain the same value.
Each partition makes worst case assumptions about what other partitions are doing. Hence, each partition operates under the pessimistic assumption that if an inconsistency can occur, it will occur. These strategies differ primarily in the policy used to restrict transaction processing. Since they ensure consistency, it is straightforward to merge the results of individual partitions at reconnection time: Updates are merely propagated from copies in one partition to their counterparts in the other partitions.

At the other extreme lie the optimistic strategies, which do not limit availability. Any transaction may be executed in any partition containing copies of the items read and written by the transaction. Hence, inconsistencies may be introduced. These strategies operate under the optimistic assumption that inconsistencies, even if possible, rarely occur. During reconnection, the system must first detect inconsistencies and then resolve them. Although optimistic policies allow global inconsistencies, transaction processing within each partition is consistent. Thus, no user staying within a single partition could detect an inconsistency.

Optimistic strategies differ primarily in how they detect and resolve inconsistencies. In section 1 we have already discussed several different ways that can be used to resolve conflicts. These range from simply undoing a set of the transactions that have generated no significant external actions, to running compensating transactions to nullify the effects of transactions generating external actions, to running corrective transactions that transform the database to a "correct," but not necessarily serializable, state. Obviously, the latter approach requires finding a suitable correctness criteria in lieu of one-copy serializability.

The second dimension in the classification concerns the type of information used in determining correctness. Syntactic approaches use one-copy serializability as their sole correctness criteria and check serializability by examining readsets and writesets of the executed transactions. Hence neither the semantics of the transactions (i.e. how the read items are used to generate the result) nor the semantics of the data items are used in ascertaining correctness. Syntactic approaches are implemented using general-purpose concurrency control algorithms, such as two-phase locking [EGLT76].
Semantic approaches use either the semantics of the transactions or the semantics of the database in defining correctness. Although this is somewhat of a "catch-all" category, there are two discernible subcategories. The first uses serializability as the correctness criteria but also uses the semantics of the transactions in testing serializability. The second abandons serializability altogether and instead defines correctness in terms of the contents of the database itself; the correctness criteria is intended to capture the semantics of the data stored in the database. Such semantic constraints fall outside of the traditional model of transaction processing.

3. SYNTACTIC APPROACHES

All approaches in this section use serializability as the correctness criteria and check serializability by comparing transactions' readsets and writesets. We assume that a correct concurrency control mechanism coordinates transaction execution within a partition; hence, transaction execution within a partition is serializable. We also assume that at the time of the partitioning all copies are mutually consistent and there are no in-progress transactions. Note that this assumption is not realistic and is made to simplify the presentation. In general, copies of data items may not be consistent at partition time because some have processed updates of a committed transaction while others have not. How the system resolves these "blocked" transactions will be discussed in the section dealing with atomic commitment (section 5). Transactions at earlier stages of processing can be aborted and rerun in the partition containing their site of origin.

3.1. Optimistic Strategies

Version Vectors [PPR81]

Version vectors, proposed for use in the distributed operating system LOCUS [POPE81], detect write-write conflicts between copies of files. Each copy of a file $f$ has associated with it a version vector which counts the number of updates to $f$ originating at each site at which it is stored. That is, the vector consists of a sequence of $n$ pairs, where $n$ is the number of
sites at which $f$ is stored; the $i^{th}$ vector entry $(S_i, v_i)$ counts the number $v_i$ of updates to $f$ originating at site $S_i$. Conflicts occur when more than one partition updates the file, and can be detected by comparing version vectors.

Vector $v$ is said to dominate vector $v'$ if $v$ and $v'$ are version vectors for the same file and $v_i \geq v'_i$ for $i = 1, \ldots, n$. Intuitively, if $v$ dominates $v'$, the copy with vector $v$ has seen a superset of the updates seen by the copy with vector $v'$. Two vectors are said to conflict if neither dominates. In this case, the copies have seen different updates. For example, $<A:3, B:4, C:2>$ dominates $<A:2, B:1, C:2>$ since $3 > 2$, $4 > 1$ and $2 = 2$, but $<A:3, B:1, C:2>$ and $<A:2, B:4, C:2>$ conflict since $3 > 2$ but $1 < 4$.

When two sites discover that their version vectors for $f$ conflict, an inconsistency has been detected. How to resolve the inconsistency is left up to the system administrator.

**EXAMPLE:** Consider the following partition graph for file $f$. Sites A, B and C initially have the same version of $f$. The system then partitions into groups AB and C, and A updates $f$ twice. Hence both A and B have version vectors of $<A:2, B:0, C:0>$, while C is $<A:0, B:0, C:0>$. Site B then splits off from site A and joins site C. Since C did not update $f$ and B has the current version, there is no conflict ($<A:2, B:0, C:0>$ dominates $<A:0, B:0, C:0>$), and B's version (and vector) is adopted for the new group BC. During this new partition failure, A updates its version of $f$ once, making group A's version vector $<A:3, B:0, C:0>$, and C updates its version of $f$ once, making group BC's version vectors $<A:2, B:0, C:1>$. When groups A and BC now combine, there is a conflict and neither of $<A:2, B:0, C:1>$ or $<A:3, B:0, C:0>$ dominates the other.

![Partition Graph Example](image)

**NO CONFLICT:** B's version adopted. C updates $f$ once.

**CONFLICT:** $3 > 2$, $0 = 0$, but $0 < 1$.

Manual assistance required.

Version vectors detect write-write conflicts only. Read-write conflicts cannot be
detected because the files read by a transaction are not recorded. Hence, the approach works well for transactions accessing a single file, which are typical in many file systems, but not for multi-file transactions, which are common in database systems.

EXAMPLE: Consider applying version vectors to the banking example of Figure 1, where communication between sites A and B fails. During the failure, the transaction executed at A updates the checking balance based on the value of the savings balance; the transaction executed at B updates the savings balance based on the value of the checking balance. No conflict will be detected, even though the above is clearly not serializable.

\[
\begin{align*}
\text{checking balance} & \\
A & < A:0, B:0 > \\
B & < A:0, B:0 > \\
A & B
\end{align*}
\]

\[
\begin{align*}
\text{savings balance} & \\
A & < A:0, B:0 > \\
B & < A:0, B:1 > \\
A & B
\end{align*}
\]

NO CONFLICT detected
A's version adopted.
\(< A:1, B:0 >\)

NO CONFLICT detected
B's version adopted.
\(< A:0, B:1 >\)

To extend the version vectors algorithm so that read-write conflicts are detectable, read-set and writes of transactions must be logged. This leads to an algorithm very similar to the one presented in the next section.\(^3\)

The Optimistic Protocol [DAVI82]

The optimistic protocol detects inconsistencies by using a precedence graph, which models the necessary ordering between transactions. Precedence graphs, used to checking serializability across partitions, are adapted from serialization graphs [PAPA79], which are used to check serializability within a site. In the following we assume that the readset of a transaction contains its writset. (The reason for this assumption is to avoid certain NP-complete problems in checking serializability.)

In order to construct the precedence graph, each partition maintains a log, which

\(^3\)Historical note: such an extension was proposed in [PARA82]. Their conflict detection algorithm, however, is incorrect: it does not detect all inconsistencies and falsely detects inconsistencies.
records the order of reads and writes on the data items. From this log, the readsets and write sets of the transactions and a serialization order on the transactions can be deduced. (A serialization order exists since, by assumption, transaction execution within a partition is serializable.) For partition , let be the set of transactions, in serialization order, executed in .

The nodes of the precedence graph represent transactions; the edges, interactions between transactions. The first step in the construction of the graph is to model interactions between transactions in the same partition. Two types of edges (interactions) are identified:

(a) **(Data) Dependency Edges** \( (T_{ij}, \rightarrow \rightarrow T_{ik}) \): these edges represent the fact that one transaction \( T_{ik} \) read a value produced by another transaction \( T_{ij} \) in the same partition \( \text{READSET}(T_{ij}) \cap \text{WRITESET}(T_{ik}) \neq \emptyset, j < k \)

(b) **Precedence Edges** \( (T_{ij}, \rightarrow \rightarrow T_{ik}) \): these edges represent the fact that one transaction \( T_{ij} \) read a value that was later changed by another transaction \( T_{ik} \) in the same partition \( \text{READSET}(T_{ij}) \cap \text{WRITESET}(T_{ik}) \neq \emptyset, j < k \)

A dependency edge from \( T_{ij} \) to \( T_{ik} \) indicates that the output of \( T_{ij} \) influenced the execution of \( T_{ik} \), hence the "existence" of \( T_{ik} \) depends on the "existence" of \( T_{ij} \). The meaning of a precedence edge \( T_{ij} \) from \( T_{ik} \) is more subtle: \( T_{ik} \) does not influence \( T_{ij} \) only because \( T_{ij} \) executed before it. In this case the "existence" of \( T_{ik} \) does not depend on the existence of \( T_{ij} \). In both cases, an edge from \( T_{ij} \) to \( T_{ik} \) indicates that the order of execution of the two transactions is reflected in the resulting database state. Note that the graph constructed so far must be acyclic since the orientation of an edge is always consistent with the serialization order.

To complete the precedence graph, conflicts between transactions in different partitions must be represented. A new type of edge is defined for this purpose:

(c) **Interference Edges** \( (T_{ij}, \rightarrow \rightarrow T_{ik}, i \neq l) \): these edges indicate that \( T_{ij} \) read an item that is written by \( T_{ik} \) in another partition \( \text{READSET}(T_{ij}) \cap \text{WRITESET}(T_{ik}) \neq \emptyset \).

\(^4\)In [DAV132], these edges are called *ripple edges.*
The meaning of interference edge is the same as a precedence edge: an interference edge from $T_{ij}$ to $T_{ik}$ indicates that $T_{ij}$ logically "executed before" $T_{ik}$ since it did not read the value written by $T_{ik}$. An interference edge signals a read-write conflict between the two transactions. (A write-write conflict manifests as a pair of read-write since each transaction's readset contains its writeset.)

EXAMPLE: Suppose the serial history of transactions executed in $P_1$ is \{T_{11}, T_{12}, T_{13}\}, and that of $P_2$ is \{T_{21}, T_{22}\}. The precedence graph for this execution is given below, where the readset of a transaction is given above the line and the writeset below the line. (Thus, transaction $T_{12}$ reads $b,c$ and writes $c$.)

\begin{center}
\begin{tabular}{l|ll}
\hline
& PARTITION 1 & PARTITION 2 \\
\hline
$T_{11}$ & $a,b$ & $e,f$ \\
$T_{12}$ & $b,c$ & $a,f$ \\
$T_{13}$ & $c,d,e$ & \\
\hline
\end{tabular}
\end{center}

Intuitively, cycles in the precedence graph are bad: if $T$ and $T'$ are in a cycle then the database reflects the results of $T$ executing before $T'$ and of $T'$ executing before $T$—a contradiction. Conversely, the absence of cycles is good: the precedence graph for a set of partitions is acyclic if and only if the resulting database state is consistent [DAVI82]. An acyclic precedence graph indicates that the transactions from both groups can be represented by a single serial history, and the last updated copy of each data-item is the correct value. A serialization order for the transactions can be obtained by topologically sorting the precedence graph.

Inconsistencies are resolved by rolling back (undoing) transactions until the resulting subgraph is acyclic. When a transaction is rolled back, transactions connected to it by dependency edges must also be rolled back, since these transactions read the values produced by the
selected transaction. Hence rolling back one transaction may precipitate the rolling back of many, a problem known as *cascading rollbacks*. Transactions connected to a rolled back transaction by precedence edges are not rolled back since they did not read the results of the rolled back transaction. In the above example, if \( T_{11} \) is selected, then \( T_{12} \) and \( T_{13} \) must also be selected. However, simply selecting \( T_{13}, T_{21} \), or \( T_{22} \) also breaks the cycle and involves only one transaction. Note that transactions must be rolled back in reverse order of execution; that is, within each partition, the value of a data item that is updated by one or more rolled back transactions from that group will be restored to the value read by the *earliest* rolled back transaction. To merge the partitioned databases, the final value of each updated data item in each partition group can simply be forwarded to the other group (a data item cannot be updated by both groups after transactions have been rolled back since the resulting precedence graph is acyclic).

Note that the notion of "committing" a transaction has been somewhat violated. A transaction \( T \) is "committed" during a failure subject to confirmation at recovery. If all actions performed by \( T \) are recoverable, rolling back is not a problem; one merely replaces the values updated by \( T \) by the values read by \( T \). However, some unrecoverable actions may also have been performed. For example, an automatic teller may have handed money to a customer, results may have been reported to a user, or a missile may have been fired. Some such actions may be compensated for, that is, there could be some \( T^* \) that can be executed to nullify the effect of \( T \). For example, the bank could charge the account of the customer who accidentally received cash from the automatic teller, or the reporting procedure could inform the user that the reported results were inaccurate due to system failure (hopefully the user would have been made aware of this possibility from the start). Other actions—such as the firing of a missile—may have no compensation. Such actions should not be permitted during failure since there can be no guarantee that the transaction will not be rolled back.

The algorithm used to select which transactions to roll back should strive to minimize some cost function, for example, the number of rolled-back transactions, or the sum of the
weights of the rolled-back transactions (where the assignment of weights can be application dependent). Unfortunately minimizing either the number of transactions or the sum of their weights is an NP-Complete problem [DAVI82]. Hence, heuristics must be used.

The most promising heuristics use the following observation: breaking all two-cycles in a precedence graph tends to break almost all cycles. A two-cycle is a cycle consisting of two transactions connected by a pair of interference edges in opposite directions. These cycles tend to represent write-write conflicts on data-items. Two cycles can be broken optimally using a polynomial algorithm. After the two-cycles have been broken, the few remaining cycles can be broken by a greedy algorithm, one that repetitively selects the lowest weight transaction involved in a cycle. Simulation studies have shown that such heuristics work very well, out-performing all other strategies tested [DAVI82].

The performance of the optimistic protocol is studied in [DAVI82]. A probabilistic model is developed that yields a formula for estimating rollback rate given the number of transactions, a model of the average transaction, and the size of the database. Simulation results in the same paper yield additional insight into rollback rates. These studies indicate that the optimistic protocol performs best when:

1. a small percentage of items are updated during the partitioning, and
2. few transactions have large writesets.

Whenever (1) holds, the probability that a given transaction will be rolled back depends more on the size of its writeset than its readsset. Regarding (2), not only is the occasional large transaction more likely to conflict with another transaction, but in addition its rollback is likely to cause other rollbacks. Consequently, the rollback rate is quite sensitive to variance in transaction size.

3.2. Pessimistic Approaches

The first group of pessimistic strategies, primary site (copy), tokens, and voting, were initially proposed as distributed concurrency control mechanisms. However, they can also be used to
prevent conflicts between transactions when the network partitions. Missing writes is an adaptive voting strategy which improves performance when there are no failures in the system. The last approach, designed specifically for partitioned networks, strives to increase availability by exploiting known characteristics of the workload.

*Primary Site, Copy [ALDA76], [STON79]*

Originally presented as a resilient technique for sharing distributed resources, this approach suggests that one copy of an item be designated the primary and as such be responsible for that item's activity. All reads for a data item must be performed at the primary site for that data item. Updates are propagated to all copies. In the case of a partition failure, only the partition containing the primary copy can access the data item. Updates are simply forwarded at recovery to regain consistency.

This approach works well only if site failures are distinguishable from network failures. If this is the case and the primary site for a data-item fails, a new primary can be elected (for a discussion of election protocols, see [GARC83b]). However, if it is uncertain whether the primary failed or the network failed, the assumption must be that the network failed and no new primary can be elected.

*Tokens [MIWI82]*

This approach is very similar to that above except that the primary copy of an item can change for reasons other than site failure. Each item has a token associated with it, permitting the bearer to access the item. In the event of a network partition, only the group containing the token will be able to access the item.

The major weakness with this scheme is that accessibility is lost if the token is lost due to site or communication medium failure.

---

5 Normally only the lock for a data item must be acquired at the primary site: the actual read may be performed on any copy once the lock has been granted.
Voting [Giff79]

The first voting approach was the majority consensus algorithm described in [THOM78]. What we now describe is the generalization of that algorithm proposed by Gifford [Giff79].

In this approach, every copy of a replicated item is assigned some number of votes. Every transaction must collect a read quorum of \( r \) votes to read an item, and a write quorum of \( w \) votes to write an item. Quorums must satisfy two constraints:

1. \( r + w \) exceeds the total number of votes \( v \) assigned to the item, and
2. \( w > \frac{v}{2} \).

The first constraint ensures that there is a non-null intersection between every read quorum and every write quorum. Any read quorum is therefore guaranteed to have a current copy of the item. (Version numbers are used to identify the most recent copy.) In a partitioned system, this constraint guarantees that an item cannot be read in one partition and written in another. Hence, read-write conflicts cannot occur between partitions.

The second constraint ensures that two writes cannot happen in parallel or, if the system is partitioned, that writes cannot occur in two different partitions. Hence, write-write conflicts cannot occur between partitions.

**EXAMPLE:** Suppose sites \( S_1, S_2 \) and \( S_3 \) all contain copies of items \( f \) and \( g \), and that a partition \( P_1 \) occurs, isolating \( S_1 \) and \( S_2 \) from \( S_3 \). Initially, \( f = g = 0 \), each site has 1 vote for each of \( f \) and \( g \), and \( r = w = 2 \) for both \( f \) and \( g \).

\[
\begin{array}{c|c|c}
S_1 & \{f, 0\} & \{f, 0\} \quad S_3 \\
\{g, 0\} & \{g, 0\} \\
S_2 & \{f, 0\} & \\
\{g, 0\} & \\
\end{array}
\]

During the partitioning, transaction \( T_1 \) wishes to update \( g \) based on values read for \( f \) and \( g \). Although it cannot be executed at \( S_3 \) since it cannot obtain a read quorum for \( f \), or read and write quorums for \( g \), it can be executed at \( S_1 \), and the new value \( g = 1 \) is propagated to \( S_2 \).
Now suppose $P_1$ is repaired, and a new failure $P_2$ isolates $S_1$ and $S_3$ from $S_2$. During this new failure, transaction $T_2$ wishes to update $f$ based on values read for $f$ and $g$. It cannot be executed at $S_2$ since it cannot obtain a read quorum for $g$, or read and write quorums for $f$. However, it can be executed at $S_3$. Using the most recent copy of $g=1$ (obtained by reading copies at both $S_1$ and $S_3$ and taking the latest version) $T_2$ computes the new value $f=1$ and propagates the new value to $S_1$.

Notice that the above example reduces to a majority vote [THOM78] since each copy has exactly one vote and $r$ and $w$ are a simple majority.

Varying the weight of a vote can be used to reflect the needed accessibility-level of an item. For example, in a banking application, a customer may use certain branches more frequently than other branches. Suppose there are 5 branches of the bank, and that the customer uses branches 1, 2, and 3 with equal frequency, but never goes to branches 4 or 5. Assigning $r=w=2$ and his account at branches 1, 2 and 3 a vote of 1 but 0 elsewhere would reflect this usage pattern.

The quorum algorithm differs from those previously discussed in two important ways. First, by choosing $r < v/2$, it is possible for an item to be read-accessible in more than one partition, in which case it will be write-accessible in none. Read-accessibility can be given a high priority by choosing $r$ small. Second, the algorithm does not distinguish between communication failures, site failures, or just slow response. A serious weakness of the previous schemes is that availability is severely compromised if a distinction can not be made.

A weakness of the quorum scheme is that reading an item is fairly expensive. A read quorum of copies must be read in this scheme, whereas a single copy suffices for all other schemes.
Missing Writes [EASE83]

Eager and Sevcik's algorithm ([EASE83]; see also [BEGO83]) is based on the observation that requiring a quorum for items in the readset as well as for those in the writeset is a sufficient restriction to guarantee correct or serializable execution during partition failures; however, it is not necessary. Performance is unnecessarily degraded by requiring a readset quorum when there are no failures; however, the requirement is necessary when there are failures. Thus transactions run in two modes, normal and failure. When in normal mode, transaction \( T \) reads one copy of each data-item in its readset, and updates all copies in its writeset. If some copy cannot be updated, \( T \) becomes "aware" of a missing update, and must run in failure mode, which is very similar to the majority consensus algorithm alluded to above: quorums must now be obtained for each data-item in the readset and writeset.\(^6\) This "missing update information" is then passed along to all following transactions that need the information, i.e. all transactions connected to \( T \) by a path of dependency and precedence edges originating at \( T \). These transactions also become aware of missing updates, and must run in failure mode. Since \( T \) cannot see the future and does not know what transactions these will be, the missing update information is posted at sites as a level of indirection. When the failure is repaired, the missing update information will eventually be posted at the sites that "caused" the missing updates, i.e. those that did not receive the updates. The updates can then be applied, and postings removed from other sites throughout the system.

The algorithm hinges on the ability to recognize "missing writes", and to propagate the information to later transactions so that cycles in the precedence graph of committed transactions are avoided. Note, however, that certain transactions may be able to execute without restriction even if there are partition failures present in the system; there is no harm in allowing readonly transactions to "run in the past" during a failure, i.e. read an old value of a data-item, as long as no cycles result in the precedence graph of committed transactions. This

\(^6\)A quorum can essentially be thought of as the \( w > \frac{v}{2} \) from condition 2 in the previous section; it is a set of (possibly weighted) votes from sites containing copies of the data-item such that any two quorums for that data-item intersect.
ability to run in the past allows a site that has become isolated from the rest of the network to execute readonly transactions even if updates are being performed on remote copies of the data-items stored at that site.

EXAMPLE: Suppose that there are four sites in the system $S_1$, $S_2$, $S_3$, and $S_4$. Sites $S_1$, $S_2$, and $S_3$ contain copies of data-item $a$; site $S_1$, $S_3$, and $S_4$ contain copies of data-item $b$. Now suppose a failure occurs, isolating sites $S_1$ and $S_2$ from site $S_3$ and $S_4$; transactions $T_1$, $T_2$, $T_3$ are initiated at site $S_1$ (in that order), while transaction $T_4$ is initiated at $S_4$. The readsets, writesets and precedence graph are depicted below. (The precedence graph shown is of uncommitted transactions since cycles in the precedence graph of committed transactions will obviously be avoided.)

\[
\begin{align*}
T_1: & \quad a, b \\
T_2: & \quad a \quad \leftarrow \quad a \\
T_3: & \quad a, b \\
T_4: & \quad a, b
\end{align*}
\]

$T_1$ is unaware of the failure, since it can obtain a copy of $a$ and $b$ at $S_1$; it can happily run in the past. $T_2$ becomes aware of the failure when it is unsuccessful at updating the copy of $a$ at $S_3$; it is allowed to commit, however, since it can receive a quorum for each data-item in its read and write sets (assuming that each copy has a weight of 1). $T_2$ is then required to pass all of its missing update information to transactions that are incoming nodes for outgoing edges from $T_2$, such as $T_3$ in this example. If $T_3$ were to successfully commit, it would also be required to pass on the missing update information. However, in this example, $T_3$ is not allowed to commit; since it is aware of missing updates, it is required to obtain a quorum for data-items in its readset, which it cannot for $b$. Transaction $T_4$ would also not be allowed to commit since although it can obtain a quorum for $b$, it finds that it cannot update the copy of $b$ at $S_2$, and must then run in failure mode. Since it cannot obtain a quorum for $a$, it cannot complete successfully. Thus in this example (as well in all others), there are no cycles in the precedence graph of committed transactions. Note that the restriction that $T_2$ and $T_4$ be rerun in failure mode is necessary: suppose that $T_2$ and $T_4$ both read $a$ and $b$, but $T_2$ updated $a$ while $T_4$ updated $b$. If they both executed in normal mode and did not switch to failure mode when they became aware of missing updates, a cycle would result in the precedence graph of committed transactions.

In order to implement this method, regardless of the concurrency control mechanism being used, several files must be kept at each site. They include:
(a) A file for posted missing updates, with indications of which transactions need to be informed about the missing updates.

(b) A file containing the values of missing updates, to be applied to the appropriate copies when recovery occurs.

(c) A file indicating the transaction restarts, aborts, or commits of which the site is aware, used to resolve the "blocked" transactions alluded to in the introduction to section 3.

(d) A record of the missing updates that have been applied at the site.

Although these files can grow very rapidly if the system is active during failures, they must only be maintained when failures are present in the system, and thus do not impact performance in the absence of failures. Furthermore, since quorums are only required when a transaction is aware of a missing update, when there are no failures or the transaction is not required to know about the failure, reading an item incurs no additional overhead. The method is also very flexible: it requires no "detection" of failure other than the inability to perform updates, no special "global" action or temporary cessation of activity to propagate updates when the failure is repaired.

Improvements on this algorithm can also be found in [HERL84]. Better availability is provided by exploiting type-specific properties of the data. Necessary and sufficient constraints on availability are derived from the data type specification. For example, Enqueue and Dequeue operations for a replicated FIFO queue are allowed to execute concurrently in distinct partitions; however, in Eager and Sevcik's version, this could only execute in one partition since the operations would be treated as writes.

Class Conflict Analysis [SKWR84]

The pessimistic strategies discussed so far strive to make each data record available for reading and writing in some partition by arbitrary transactions. These strategies, then, emphasize the general availability of individual records. An alternate strategy, Class Conflict Analysis, strives to ensure the capability of performing important high-level operations on the
data. Hence, this strategy emphasizes the availability of high-level data operations, possibly at the expense of the general availability of records.

To illustrate the difference between the two approaches consider again the banking example discussed in Section 1, where a customer can overdraw his checking account as long as the overdraft is covered by funds in his saving account. If the system partitions, none of the discussed pessimistic strategies would allow a checking withdrawal (which requires reading the balance of both accounts) to occur in one partition and allow a savings deposit to occur in another partition. However, executing these transactions in parallel in different partitions violates neither the bank's policy nor the one-copy serializability. Hence, these transactions should be allowed.

The approach assumes that transactions are divided into classes as proposed in [BSR80]. A class may be a well-defined transaction type, such as the "savings withdrawal," or it may be syntactically defined, e.g., the class containing all transactions reading and writing a subset of items $a$, $b$, and $c$.

Like transactions, classes are characterized by their readset and writesets. The readset (resp. writeset) of a class is the union of the readsets (resp. writesets) of all of its member transactions. As before, it is assumed that a class's readset contains its writeset, so that certain NP-complete problems are avoided. Two classes conflict if one's readset intersects the other's writeset. A class conflict indicates a potential read-write conflict between member transactions of the classes. (A conflict may not actually occur because the transactions' readsets and writesets may be proper subsets of the classes' readsets and writesets.)

When a failure occurs, each partition group must decide what classes of transactions it will execute so as to avoid potential conflicts with transactions executed in other partitions. As a first step, it must decide what classes are "assigned" to its partition as well as those that are assigned to the other partitions. For example, if classes are executable at specific sites, the classes assigned to a partition would be those executable at sites within the partition. Note that classes may be assigned to more than one partition, and there may be conflicts between
classes in different partitions.

The second step for each partition is to analyze the assignment and discover the class conflicts that can lead to nonserializable executions. The analysis uses a graph model that is similar to the one used in the optimistic protocol. Whereas the precedence graphs used in that protocol give the actual orderings between conflicting transactions, class conflict graphs give all potential orderings between conflicting classes. Defined below is a simplified version of the model presented in [SKWR84].

A node of the class conflict graph represents the occurrence of a given class in a given partition. Edges are drawn between occurrences of conflicting classes according to the rules given below. Let \( C_i \) and \( C_j \) be classes such that \( \text{readset}(C_i) \cap \text{writeset}(C_j) \) is not empty.

1. If \( C_i \) and \( C_j \) are in the same partition, then a pair of edges pointing in opposite directions connects them.

2. If \( C_i \) and \( C_j \) are in different partitions, then a directed edge extends from \( C_i \) to \( C_j \).

The direction of the edges indicate the possible logical orderings of transactions from conflicting classes. In particular, in the case of classes \( C_i \) and \( C_j \) in rule (2), the transactions of \( C_i \) can not logically succeed those of \( C_j \) because \( C_i \)'s transactions can not read the updates of \( C_j \)'s transactions. Therefore, the only order possible is that all transactions of \( C_i \) precede all transactions of \( C_j \), as indicated by the single directed edge.
EXAMPLE: Below is a class conflict graph for the banking example for two partitions. Boxes denote classes. Readsets are shown above the line; writsets, below. Data items $s$, $c$, and $i$ are the savings account, the checking account, and the interest rate, respectively. Classes $C_d$ and $C_w$ include the saving deposit transactions and checking withdrawal transactions discussed in section 1. Class $C_t$ transactions change the interest rate, class $C_s$ transactions add an interest payment to the savings account, and class $C_r$ transactions are readonly.

The third step in the analysis is to identify those assignments that could lead to nonserializable executions. Cycles play a key role here, but not all cycles are bad. Among class occurrences in the same partition, cycles are both common and harmless, since the concurrency control algorithm operating in the partition will prevent nonserializable executions. On the other hand, cycles spanning multiple (>1) partitions are not harmless, since there is no mechanism preventing them in an execution. Hence, multipartition cycles indicate the potential for nonserializable executions. In the example, if transactions from classes $C_t$, $C_r$, and $C_w$ execute in that order in partition 1 and a transaction from $C_s$ executes in partition 2, the result is nonserializable. (This can be checked by constructing the precedence graph for the execution.)

Whenever the preliminary class assignment yields a (multipartition) cyclic graph, further constraints on transaction processing must be imposed. The most straightforward approach is to delete classes from partitions until the class conflict graph is rendered multipartition acyclic. In the above example, one of $C_t$, $C_r$, $C_w$, or $C_s$ must be deleted. For availability
reasons, it is desirable to delete a minimum set of classes. Not surprisingly, this is an NP-complete problem.

Although this discussion has assumed that the complete state of the network is known to all partitions, this assumption is not required in applying class conflict analysis. [SKWR84] discusses some modifications to the basic algorithm that work with incomplete knowledge of the network status. In addition, the paper discusses refinements that afford more availability than the analysis presented here.

3.3. Discussion

Optimistic versus Pessimistic

One basis for comparing the two types of approaches is in terms of an appropriate cost model. The model should include overhead, the cost of repairing inconsistencies, and the cost of lost opportunities. In the following, costs common to all approaches, such as the propagation of updated values, are omitted.

Optimistic policies have two sources of overhead. The first is the log, which must be maintained while the system is partitioned, recording the readset and writest of each transaction in order to construct the precedence graph and recording sufficient information to rollback transactions. Many database systems already maintain a log, called an undo log, for rolling back transactions in case of site failures or transaction failures (e.g., deadlocks) [GMBLL81]. This same log can be used to roll back conflicting transactions in a partitioned system. However, in order to construct the graph, undo logs must be augmented with records of transactions' readsets (which are normally not recorded since they are not needed to roll back a transaction). This increases the complexity of the logging algorithms, but it does not significantly increase the cost of logging in most systems.

The second and most significant source of overhead is the conflict detection algorithm, which constructs the graph, checks the graph for cycles, and then selects transactions to rollback. Graph construction requires a single pass over the entire log, which can be quite
expensive for a partition of long duration. The selection algorithm can be made arbitrarily expensive, depending on the quality of heuristics used. The best heuristics require time $O(N^{2.5})$ where $N$ is the number of transactions ([DAVIS2], minimally breaking all two-cycles). However, linear time heuristics often yield acceptable solutions.

The cost of repair in an optimistic approach is simply the rollback rate times the cost of rolling back a transaction. We have already discussed rollback rate. The rollback cost is often a significant fraction of the transaction’s execution cost, and may, in fact, exceed the execution cost if the transaction has external side-effects (e.g., a customer may be entitled to compensation if her reservation is cancelled, or a series of transactions may need to be executed to compensate for a single rolled back transaction). Consequently, the rollback rate must be kept reasonable small (certainly less than 20%) if optimistic approaches are to be cost-effective.

The goal of optimistic approaches is to minimize lost opportunity, the cost associated with needlessly delaying a transaction. These costs can be substantial when user satisfaction is important as, for example, in a banking application. Lost opportunities still occur in these approaches because of the allocation of resources to transactions that are destined to be rolled back. Such transactions may displace valid transactions during the partitioning, and rolling them back may cause further delays after the partitions are reconnected. Still, for most applications, we speculate that other costs dominate.

Pessimistic approaches have no repair costs and, except for conflict class analysis, almost no overhead. Even in class conflict analysis, the overhead is likely to be substantially less than in an optimistic strategy, because although conflict analysis and conflict detection are procedurally similar, the number of predeclared classes in conflict analysis is likely to be substantially less than the number of transactions in conflict detection.

The major cost of a pessimistic approach is, of course, the cost of lost opportunities. Included in this cost are not only opportunities lost to real partitioning but also opportunities lost to “apparent” partitionings, for example, site failures that are indistinguishable from real
partitionings. In many systems, apparent partitionings occur more frequently than real partitionings; therefore they must be included in any cost analysis.

In summary, the cost of an optimistic strategy is the overhead of conflict detection plus the repair cost, whereas the cost of a pessimistic strategy is the cost of opportunities lost to real and apparent partitionings. Unfortunately, except for repair costs, informed estimates for these costs are not easily obtained. No one has measured the overhead associated with any of the strategies, and the cost of lost opportunities is hard to quantify (although one component in a pessimistic strategy is the cost of underutilization of processing resources).

Combining Strategies.

Instead of using one strategy during a partitioning, strategies can be combined vertically over time; the system could start out using one strategy and switch to another as circumstances dictate. For example, the number of transactions rolled back in the optimistic protocol has been observed to increase roughly quadratically with time. In fact, the expected number of transactions backed out can be estimated with a formula involving the number of transactions processed within the partition, the number of data-items in the database and certain other parameters modelling the type of transactions being executed (see [DAVI82]). Since it is usually impossible to predict how long a partitioning will last, the database administrator could then set a ceiling on the rollback rate (say 10%) and request that the optimistic protocol be used only until this ceiling was reached. If this ceiling was reached, the system could switch to a more pessimistic approach, such as primary site, for the remainder of the failure. Of course, there is no guarantee that these future transactions would not also be backed out since they could be connected to transactions that had already executed by dependency edges; these transactions would still have to be included in the construction of the precedence graph and hence considered for possible backout in order to guarantee serializability. However, the backout rate would be held at a more acceptable level.

Strategies can also be combined horizontally over time [SKEE82c]. One approach is to assign items different levels of consistency. Items in level 0 (the highest level) are immutable
during a partitioning; items in level 1 are updated according to a pessimistic strategy; and items in level 2 are updated according to an optimistic strategy. Updates to level 1 items are globally consistent and guaranteed to persist, while updates to level 2 items are consistent within the partition but may not be globally consistent and, hence, are subject to rollback. Although a transaction may update items in only one level, it may read items of the same level and higher.

Another way to combine approaches horizontally is to divide transactions, instead of items, into groups. For each partition, transactions are divided into two groups: high priority transactions that can not be rolled back, and low priority transactions that can. Class conflict analysis is used to determine a group of high priority transactions for each partition. The low priority group for a partition consists of all transactions not writing an item read by a high priority transaction in the same partition. (A low priority transaction, though, can write an item read by a high priority transaction in a different partition.) When partitions are reconnected, the optimistic protocol is used to construct a precedence graph containing all transactions executed; however, only low priority transactions are liable to rollback. (An approach similar to this is used in [APWI84].)

4. SEMANTIC APPROACHES

The first three approaches presented in this section illustrate three different ways of using semantics to increase availability. The first approach, log transformations, uses the standard notion of correctness, namely serializability, but uses the semantics of transactions in checking serializability. The second approach relaxes slightly the standard notion of serializability in order to enrich the set of transactions allowed in a partitioned system. The semantics of the application determine when serializability can be relaxed. The third approach, Data-Patch, abandons serializability as a correctness criterion altogether, using instead an application-specific definition of correctness. All three approaches are optimistic. As a matter of fact, to our knowledge, no one has suggested a pessimistic, semantic strategy, probably because semantics are usually introduced to increase availability, not to ensure correctness.
This section ends with a brief discussion of some other proposed ideas for increasing availability.

Log Transformations [BGRCK83]

This approach is similar to the optimistic protocol. During the partitioning, logs are kept of which transactions were executed and in what order. After reconnection, a rerun log is constructed which indicates what should be reflected as having happened during the failure. To achieve this, transactions in each group may have to be backed out and rerun. It differs in that transactions are pre-defined, and semantic properties of pairs of transactions are declared to avoid needlessly backing out and re-executing transactions. These properties can include commutativity ($T_i T_j = T_j T_i$) and overwriting ($T_i T_j = T_j$). There is also a notion of “absolute time” in each group during the failure so that transactions can be merged based on the time at which they were executed.

EXAMPLE: Suppose that during a partition, $P_1$ has executed $T_2, T_4, T_6$ and that $P_2$ has executed $T_1, T_3, T_5$, where the subscripts indicate the absolute timing of the transactions. The rerun log would be $T_1, T_2, T_3, T_4, T_5, T_6$. If we ignored any semantic properties of transactions, merging the database at $P_1$ would involve backing out transactions $T_2, T_4, T_6$ and reexecuting the rerun log. If we assume that backing out transaction $T$ can be achieved by running an inverse transaction $T^{-1}$, then the entire merging operation at $P_1$ can be represented by the backout (or rollback) log $T_6^{-1}, T_4^{-1}, T_2^{-1}$ followed by the redo log. Similarly, the merge operation at $P_2$ involves executing the backout log $T_3^{-1}, T_5^{-1}, T_1^{-1}$ followed by the redo log. Let us call the combined backout, redo log the merge log.

If we know that $T_1$ commutes with $T_2$, then the merge log at $P_1$ can be reduced to

$$T_6^{-1}, T_4^{-1}, T_2, T_3, T_4, T_5, T_6$$

To see that the result of executing $P_1$'s merge log is equivalent to the result of executing $T_1, T_2, T_3, T_4, T_5, T_6$ in order, consider the entire sequence of transactions executed by $P_1$ (that is, the original execution followed by the merge log):

$$T_2, T_4, T_6, T_6^{-1}, T_4^{-1}, T_1, T_3, T_4, T_5, T_6.$$  

Since $T_6, T_6^{-1}$ and $T_4, T_4^{-1}$ are equivalent to the null transaction, the above is equivalent to

$$T_2, T_1, T_3, T_4, T_5, T_6.$$  

And, by the commutativity of $T_1$ and $T_2$, this is equivalent to the desired sequence.

If in addition we know that $T_1$ and $T_3$ commute with $T_4$ and $T_6$, and that $T_6$ overwrites $T_5$, then the $P_1$ merge log can be further reduced to

$$T_1, T_3.$$
(that is, after the partition we only have to run $T_1, T_3$ without backing out any transactions). At $P_2$, this same semantic information only reduces the merge log to
\[ T_5^{-1}, T_3^{-1}, T_2, T_3, T_4, T_6. \]

The process of reducing in size the merge log is called log transformation. The process can be automated with the aid of a graph formalism presented in [BGRCK85]. With it, merge logs are represented as graphs, and each log transformation is represented as a graph transformation.

One advantage of the log transformation approach is that the merge processes at the sites are independent of each other. That is, as each site finds out about transactions that executed elsewhere, it can proceed to integrate them locally, regardless of what the other sites are doing. Thus, this approach may be useful in an environment where failures are common and communications unreliable.

**Weak Consistency** [GAWE82]

Garcia and Weiderhold argue in [GAWE82] that conventional correctness criteria—in particular, serializability—may be stronger than needed for many readonly transactions. Since such transactions do not change the database state, their execution under a weaker correctness criterion can not generate an inconsistent state. Relaxing the serializability constraint is especially attractive for partitioned systems since it would allow a richer mix of readonly transactions. (The original motivation for a weaker correctness criterion was to speed up the processing of readonly transactions in a distributed system.) Since readonly transactions occur frequently in most systems, allowing a richer mix of them often substantially increases the number of transactions executed while partitioned.

In [GAWE82], readonly transactions are divided into two classes: those requiring strong consistency and those requiring weak consistency. A strongly consistent transaction is processed in the normal fashion: its execution must be serializable with respect to update transactions and other strongly consistent transactions. A weakly consistent transaction must see a consistent database state (the result of a serializable execution of update transactions), but its
execution need not be serializable with respect to other readonly transactions. (Weak serializability is stronger than degree 2 or 1 consistency as defined in [GLPT76]. Specifically, with degree 2 or 1 consistency, a readonly transaction can obtain an inconsistent view of the database.) The following example illustrates.

EXAMPLE: Consider again the banking database of the first section with Sites A and B partitioned. The following sequence of transactions occur:

SITE A
C: checking deposit of $50
A: read checking and savings accounts

SITE B
D: savings deposit of $100
B: read checking and savings accounts

Notice that the two update transactions, considered alone, are serializable. In fact, since they access different items, both C:D and D:C are valid serialization orders. However, when the accounting transactions A and B are included, the execution is not serializable. The database state read by A is possible only if C executes before D, while the state read by B is possible only if D executes before C. (Both A and B see a valid serialization order of the updates; the problem is that they see different orders.)

If A and B required only weak consistency, the above execution would be “correct”: the update transactions alone are serializable and each weakly consistent transaction sees the result of a serializable execution of update transactions.

The use of different consistency levels can be integrated with any of the syntactic approaches discussed in the previous section. In a pessimistic strategy a transaction requiring only weak consistency can be executed at any time in any partition, as long as the partition contains copies of items read by the transaction. The transaction will always see a consistent database state since all update transactions are guaranteed to be (globally) consistent. In an optimistic strategy, such a transaction sees a consistent state only if it does not read the result of an update transaction that is eventually rolled back.

The choice of a consistency level for a readonly transaction depends on how the information returned by the transaction is used. An accounting transaction reporting cash flow within a bank probably requires strong consistency. Inventory reporting and transactions computing summary statistics often need only weak consistency.

Fischer and Michael give an important application of weak serializability in their algorithms for directory systems[FIMI82]. A directory supports only three types of transactions:
insert a unique item, list all items, and delete an item. Mail systems, calendar systems, and other familiar applications can be cast as directories. Exploiting the property that the list operation requires only weak consistency, they give an algorithm allowing unrestricted transaction processing in the presence of communication failures, including but not limited to failures partitioning the system.

Data-Patch [GABCR82]

Data-Patch is a tool which aids the database administrator in the development of a program to automatically integrate divergent databases. As in the previous optimistic strategies, transactions are executed "normally" during the failure. At reconnection, the final database state is constructed according to an integration program. Serializability is no longer the correctness criterion; rather, the integration program defines the "correct" final database. This is based on the premise that users may already have observed the effects of a non-serializable execution, thus restoring the database to a serializable state may not be the most sensible thing to do. For example, in an Airline Reservation System, if a flight becomes overbooked it may not be desirable to cancel reservations since a promise has been made to customers and normal passenger cancellations could take care of the problem.

The major design principle involved is identifying image and plan relations. Image relations are observable entities or relationships, and must reflect that in the final database. For example, in a database for Girard bank, the relation GIRARD(BRANCH, CASH, ...) might be used to record the amount of cash at each branch. The value of CASH in each tuple at recovery should reflect the actual amount of cash at that branch. This might be obtained as the latest value for CASH in each partition group. Plan relations do not represent observable entities and the DBA can therefore have more freedom in selecting the final values. In the next example, ACCOUNT is a plan relation.
EXAMPLE:

ACCOUNT (CUSTOMER, BALANCE, ...)
DEPOSIT (CUSTOMER, AMOUNT, DATE, ...)
WITHDRAWAL (CUSTOMER, AMOUNT, DATE, ...)

DEPOSIT and WITHDRAWAL are records of account activity. If during a partition a customer overdraws his account according to the records from each group, he may be assessed a penalty charge. Thus BALANCE would reflect the sum of withdrawals and deposits to the account, plus the penalty charge. If, on the other hand, a customer is mistakenly assessed a penalty charge because a DEPOSIT did not appear during a failure, the penalty charge may be dropped.

The above example shows that not only must a final database state be chosen, but corrective actions must be specified. That is, if integrity constraints are violated after the image and plan relations have been constructed, some sort of compensating or corrective action must be issued (e.g., penalty for overdraft, as above).

The Dispatcher integration program is defined through a set of rules that specify how the integrated database can be obtained from two databases that exist after a partition. Some rules specify how differing facts are to be combined. For example, consider a field that represents the location of a ship. In this case, the DBA can select a “latest value” rule: if the field has a different value in each partition, in the integrated database use the value with the latest timestamp. If the field represents the number of reservations for a flight, the “arithmetic rule” can be used: the integrated value is the sum of the two partitioned values minus the value that existed when the partition started. Other rules specify the corrective actions to be taken. For instance, a rule might specify that if the withdrawals exceed the deposits to an account (after the integrated database has been obtained), then a dunning letter should be sent to the customer.

Other Ideas.

Numerous ad-hoc techniques for exploiting the semantics of an application to increase availability have been proposed. Many of these can best be illustrated by examples.

The first example illustrates the idea of splitting a data item. In an Airline Reservation
System [HASH80], let $SEATS$ represent the number of seats available on a particular flight. When a partition occurs, $P_1$ creates $SEATS_1$ containing 40% of the value of $SEATS$, and $P_2$ creates $SEATS_2$ containing 60% of the value of $SEATS$ (or other percentages reflecting the relative booking rates for that flight). At recovery,

$$SEATS = SEATS_1 + SEATS_2$$

would restore $SEATS$ to its correct value. Splitting can be used whenever the value of the data item represents a partial summation and each term in the summation is not dependent on the current value of the data item.

The second example comes from Incomplete Information Systems ([DAVI82], [LIPS79]). Suppose we have a tuple representing John Doe's age as less than 30. During a partition, $P_1$ gathers more information and concludes that his age is between 20 and 30, while $P_2$ concludes it to be between 15 and 25. At recovery, the intersection of these ranges, 20 to 25, may be taken as John Doe's age.

The last example illustrates the use of failure-mode integrity constraints. Recall the banking example of Figure 2, where overdrafts on the checking account were allowed as long as $\text{checking balance} + \text{saving balance} \geq 0$. That example described a scenario where the this constraint was violated during a partitioning. This anomaly could have been avoided by enforcing a failure-mode integrity constraint disallowing checking account overdrafts when the system is partitioned.

These ideas can be used with a pessimistic approach such as primary copy to allow more transactions to be executed: a portion of $SEATS$ would be available in each group, although the actual or current value for $SEATS$ could not be obtained due to possible bookings in the other group. However, the flight would never be overbooked if neither group sold more than their allotment of seats. It can also be used with more liberal approaches such as the Optimistic Protocol and Data-Patch to avoid conflict and possible transaction backouts. In the Optimistic Protocol, conflicts are mainly caused by updates to the same data-item. By splitting data-items and recombinining at recovery, this can be avoided. In Data-Patch, integration
becomes easier since the value for *SEATS* can simply be computed without canceling reservations.

5. ATOMIC COMMITMENT

A transaction on a distributed database typically executes at several sites. In order to ensure the "all or nothing" property of the transaction, the executing sites must unanimously agree to commit or to abort the transaction. Until now we have assumed that this agreement, known as atomic commitment, can be achieved in a partitioned system. Let us now examine how reasonable this assumption is.

Viewed abstractly, in a commitment protocol each participant first votes to "accept" or "reject" the transaction based on its ability to process the transaction and then decides whether to commit or abort based on the voting. Commitment normally requires unanimous acceptance. Of course, all decisions must agree.

The two-phase commit protocol [GRAY78] is a straightforward implementation of the above. In the first phase, a designated participant, the coordinator, solicits the votes from its cohorts. In the second phase, it decides based on the votes and then sends the decision to all participants. In the course of the protocol, each participant voting "accept" goes through three distinct states: an *uncommitted* state where it has not voted, an *in-doubt* state where it has voted but does not know the result of the voting, and a *decision* state where it knows the commit/abort decision. (A participant voting "reject" does not occupy the in-doubt state since it knows the eventual outcome.)

Consider the consequences of a partitioning occurring during the execution of the two-phase commit protocol. In each partition the participants, acting together, will attempt to decide the outcome based on their states. If the partition contains the coordinator, a decided participant, or an uncommitted participant, a consistent decision can be reached (in the case of an uncommitted participant, abort will be chosen). However, a partition containing only

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7Some protocols for fully replicated databases require only acceptance by a majority.
in-doubt participants and lacking the coordinator can not safely decide: the participants can not commit since they do not know the outcome of the voting, and they can not abort since they may contradict the decision of the coordinator. Hence, these sites must wait until reconnection before deciding, and the protocol (and associated transaction) is said to be blocked at those sites.

Given that the two-phase commit protocol occasionally blocks, the interesting question then is: are there any nonblocking protocols for partitionings? The answer is no: even under the most favorable, realistic partitioning assumptions, there exists no nonblocking protocols [SKEE82b]. The situation is even worse if sites can fail during a partitioning; in this case there is no protocol that guarantees that even a single site will be able to decide.

Since it is impossible to eliminate blocking, it is desirable to minimize it. Several protocols have been proposed that, under appropriate partitioning assumptions, block less than the two-phase commit protocol. One protocol, the decentralized two-phase commit protocol, reduces the likelihood of blocking by decreasing the time a site spends in the in-doubt state [SKEE82c]. This is accomplished by having the participants send their votes directly to each other, bypassing the coordinator. Another protocol, the quorum commit protocol, reduces the probability that a large partition (one consisting of many participants) will be blocked in the event of a partitioning, by introducing extra phases ([SKEE82a], [SKEE82b]). Its principal advantage is that it is also resilient to site failures and (nonpartitioning) communication failures. However, both protocols have drawbacks. Although the decentralized protocol decreases the probability that a partitioning will occur while sites are in the in-doubt state, it increases the expected number of blocked sites if a partitioning should occur. The quorum protocol actually increases the chance that some site will be blocked in the event of a partitioning (although the expected number of blocked sites decreases).

How the partition strategies of the previous two sections treat blocked transactions depends on whether the strategy is pessimistic or optimistic. In a pessimistic strategy, the data items at undecided sites must be rendered inaccessible until reconnection. In an optimistic
strategy more flexibility is possible. A partition can tentatively commit or abort a blocked transaction. If its decision is inconsistent with other decisions, it can resolve in the same way that it resolves other inconsistencies, by rolling back the offending transaction and all dependent transactions. Since rolling back is fairly expensive, a tentative decision should be made only if it has a high probability of being correct.

6. DISCUSSION


Given an application, how should one choose a partition strategy? Caution should be used in answering this question. A criticism that has been levied at research in the distributed database area in general [MOHA80] is that solutions are commonly viewed in isolation from other problems. In fact, different mechanisms may be so highly intertwined that changes proposed in one area affect many other parts of the system. In particular, with partition strategies one must pay attention to the concurrency control mechanism being used. For example, the use of a voting or token-passing concurrency control algorithm may dictate a corresponding partition algorithm unless one worries about restructuring the vote or reassigning tokens (see also [DAVI82] for a discussion of the relationship between the optimistic protocol and common forms of concurrency control). In addition, very little attention has been given to the performance of proposed mechanisms. In some cases this is because it is difficult to construct an appropriate model; in others it is because the mechanism is highly application dependent.

With these cautions in mind, we group the factors that influence the choice of a strategy into three areas:

Environment. Included here are the properties of the network and the nature of the partitionings. An important consideration is whether partitionings are caused by failures or are the result of anticipated events. In the latter case, complete information about the characteristics of the partitioning, including duration and network topology, may be known, and this can be exploited in some strategies (in particular, class conflict analysis).
However, most systems partition because of failures, and in this case the robustness of the strategy may be an important factor. For example, a primary site strategy would be a poor choice if sites failures cannot be distinguished from communication failures. Also, class conflict analysis (as presented) cannot be used if communication failures do not always result in clearly delineated partitions.

The duration of the partitioning is also important. Long failures tend to generate many conflicts between transactions in different partitions; in this case, a pessimistic strategy is a better choice than an optimistic one.

*Workload*. Two important workload characteristics are average transaction length and transaction variance. Optimistic policies work better when transactions are short and variance small.

Another important workload factor is locality of reference: Do updates to given data-items tend to occur at a certain site? If so, a primary site strategy will not prohibit many transactions and availability will still be good. The backout rate in the optimistic protocol will also be reduced, but the transactions will still have to be tested for conflict.

*Application Specific*. These factors fall into two groups. The first are requirements placed by the application on transaction processing. Two important questions are:

1. Can transaction processing be temporarily halted for recovery purposes? If not, a pessimistic approach should be adopted which merely requires the forwarding of updates to merge the databases.

2. Can transaction processing be limited in parts of the database, or is availability a premium? If the latter, a more optimistic approach should be used.

The second group include semantic considerations. Relevant questions here are:

1. Can transactions be backed out? That is, do they have an inverse? If the latter, either conflict should be avoided totally, or the divergent databases should be patched up using compensating actions if necessary to achieve correctness.
(2) Is serializability a concern, or is a more procedural definition of "correctness" in the final database state acceptable? If not, a Data-Patch approach can be used.

(3) Should a partitioned system be expected to behave exactly as an unpartitioned system? For example, even if serializability is the "normal" correctness criterion, under extenuating circumstances (such as partition failures) a more lenient definition could be used.

6.2. Future Directions

Partitioned operation is still very much an active research area. We comment briefly on several interesting research directions.

One obvious deficiency in our current knowledge of partition strategies is the lack of any performance data on how well they work. Few strategies have been implemented and none tested on a representative application. Clearly, more experience with the proposed strategies is needed before we can understand the performance tradeoffs between them.

Another important area of research is the adaptation of these strategies to accommodate more general processing models, in particular, nested transactions (and the related concept of multilevel atomicity [LYNCH83]). Nested transactions arise in general purpose distributed programming environments such as ARGUS [LISK83].

Algorithms for detecting and analyzing network partitions have also not been developed. Since several of the strategies require that the failure be initially recognized, this is an important area to address.

Finally, the use of semantics in partitioned strategies has been only scantily explored. One interesting direction is to assume that data items are instances of abstract data types and transactions are instances of operations on those types. Type-specific partition strategies can be derived from the formal properties of the types. (This is an extension of the notion of type-specific concurrency control proposed in [SCSP83].)
References


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