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Abstract

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Disciplines

Engineering | Materials Science and Engineering

Comments

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Lattice dynamics of metal-organic frameworks: Neutron inelastic scattering and first-principles calculations

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By combining neutron inelastic scattering (NIS) and first-principles calculations, we have investigated the lattice dynamics of metal-organic framework-5 (MOF5). The structural stability of MOF5 was evaluated by calculating the three cubic elastic constants. We find that the shear modulus, $c_{44}=1.16$ GPa, is unusually small, while two other moduli are relatively large (i.e., $c_{11}=29.42$ GPa and $c_{12}=12.56$ GPa). We predict that MOF5 is very close to structural instability and may yield interesting phases under high pressure and strain. The phonon dispersion curves and phonon density of states were directly calculated and our simulated NIS spectrum agrees very well with our experimental data. Several interesting phonon modes are discussed, including the softest twisting modes of the organic linker.

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Metal-organic framework (MOF) compounds,¹⁻⁵ which consist of metal-oxide clusters connected by organic linkers (see Fig. 1), are a class of nanoporous materials with very promising potential applications such as energy storage, gas separation, and template synthesis of nanoclusters and catalysts. There are an almost exponentially growing number of studies on MOF materials, mostly focusing on the optimization of the metal-oxide clusters and/or the organic linkers to improve the gas adsorption properties. Much less attention is paid to the fundamental properties of this interesting class of materials such as their structural stability and lattice dynamics. Understanding the stability and dynamical properties is clearly needed in order to optimize these materials for desired properties. For example, it was recently proposed that the MOF structure can encapsulate C_{60} molecules and result in superconductivity upon doping.⁶ In such hybrid structures, it is important to know the phonon spectrum of the MOF lattice and its coupling to the electronic structure. Furthermore, a lack of knowledge concerning MOFs lattice dynamics presents a significant obstacle in the quantum dynamics study of gas molecules (H_2 , CH_4 , etc.) adsorbed on MOFs.^{7,8}

Here we report a detailed study of the structural stability and lattice dynamics of MOF5 (the most widely studied MOF material) from combined neutron inelastic scattering (NIS) and first-principles calculations. The structure of MOF5 (Fig. 1) is highly symmetric (space group $Fm-3m$) and consists of ZnO_4 clusters at the tetrahedral site of an fcc lattice, linked by 1,4-benzenedicarboxylate (BDC) to form the three-dimensional framework.

Our first-principles calculations were performed within the plane-wave implementation of the local density approximation to density functional theory in the PWscf package.⁹ We used Vanderbilt-type ultrasoft potentials with Perdew-Zunger exchange correlation. A cutoff energy of 408 eV and a $1 \times 1 \times 1$ k -point mesh were found to be enough for the total energy to converge within 0.5 meV/atom.

We first describe the dependence of the structure on the cell volume (i.e., external pressure). Figure 2 shows how the lattice parameter and the total energy of the cell changes with external pressure and the total volume, respectively. We optimized the atomic positions for each volume and did not

find any structural instability over the pressure range studied. From -0.5 to 0.5 GPa, we find a linear pressure dependence of the lattice constant with a slope of 0.46 \AA/GPa . Fitting the energy vs volume curve to the Murnaghan equation of state¹⁰ yields a bulk modulus of 18.2 GPa. The minimum energy corresponds to lattice constant $a_C=25.58 \text{ \AA}$, which is in excellent agreement with the experimental value^{11,1} of $a=25.91 \text{ \AA}$. The optimized atomic positions were also found to agree well with the experimental values.

A better insight into the structural stability can be gained from the elastic constants, which we calculated following the standard scheme for a cubic crystal,^{12,13} starting from the fully optimized MOF5 structure. Three types of strains were applied to the conventional fcc cell of MOF5 (see Fig. 3). The first strain is a volume-conserving tetragonal deformation along the z axis, the second one refers to a uniform hydrostatic pressure, and the third one corresponds to a volume-conserving orthorhombic shear. For all three strains,

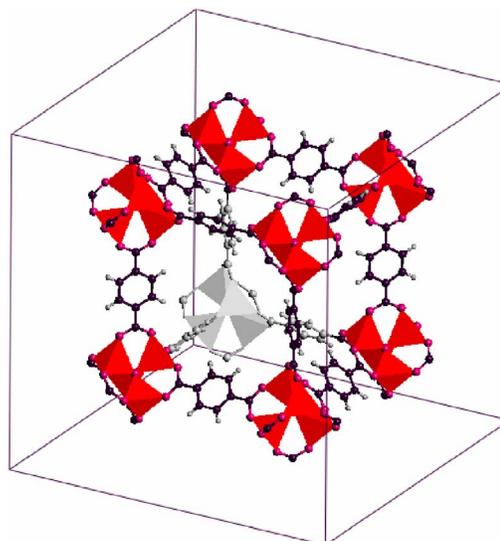


FIG. 1. (Color online) The crystal structure of MOF5, which consists of BDC linkers connecting ZnO_4 clusters located at the tetrahedral site of an fcc lattice. For clarity, some of the atoms were not shown.

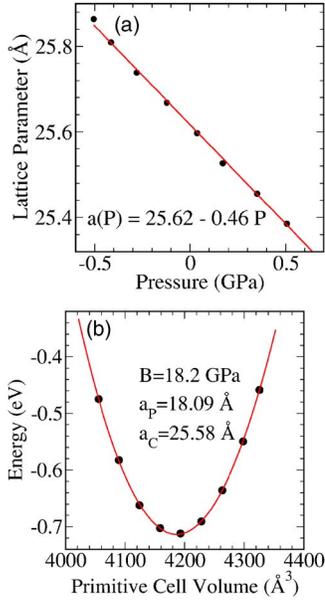


FIG. 2. (Color online) (a) The cubic lattice parameter of MOF5 versus pressure, indicating linear dependence near equilibrium structure. (b) The total energy versus primitive cell volume (dots) and the fit by the Murnaghan equation of state (solid line).

there is only one variable, γ , in the strain tensor, reflecting the magnitude of the strain. All calculations were done on the strained primitive cell, which is structurally equivalent to the strained conventional cell. Atomic positions were fully optimized and E vs γ data were obtained. $E(\gamma)/V$ was then fit to a polynomial in γ , where V is the unit cell volume. The results are summarized in Fig. 3. As expected, the calculated values satisfy the stability criteria (i.e., $c_{11} > c_{12}$, $c_{11} + 2c_{12} > 0$, and $c_{44} > 0$ for a cubic crystal). However, the shear modulus c_{44} is very small (1.16 GPa), indicating that MOF5 is very close to structural instability. Besides, $c_{11} - c_{44}$ is significantly larger than zero and according to the Cauchy relation,¹⁴ this indicates a significant deviation from a central intermolecular potential, consistent with what was found previously.¹⁵ The small c_{44} also suggests that MOF5 could collapse into a potentially useful structure under certain shear stress. For example, the pristine MOF5 structure has a large pore volume but the pores are too open to hold hydrogen molecules at high temperatures; a collapsed MOF5 structure could have finer cavities connected by smaller channels, which are in principle better for H₂ storage.

Notably, the shear modulus c_{44} that we calculated is significantly different from a previously reported result.¹⁵ This is probably due to the very weak dependence of the energy on the shear strain applied, which requires very accurate total energy calculations. We note that we do get about the same value for c_{44} regardless of the magnitude of the strain used (i.e., small or large), as evidenced from the perfect fit shown in Fig. 3.

After having shown that the MOF5 structure is stable with a very small shear modulus, we now discuss the lattice dynamics properties at the zone center and along high-symmetry directions in the Brillouin zone. The phonon density of states (DOS) and dispersion curves were calculated

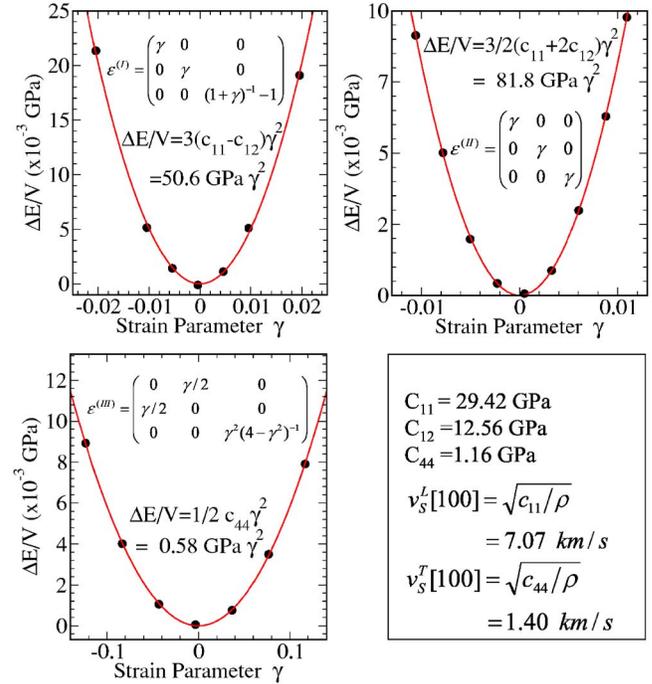


FIG. 3. (Color online) The three cubic elastic constants of MOF5. The dots are the actual calculations and the solid lines are the quadratic fit. The deformation matrices for each distortion are also shown. The right-bottom panel summarizes the calculated elastic moduli and the sound velocities. Here ρ is the mass density of MOF5 (0.59 g/cm³).

using the supercell method with finite difference.¹⁶ The primitive cell was used and the full dynamical matrix was obtained from a total of 26 symmetry-independent atomic displacements (0.03 Å).

The primitive cell of MOF5 contains two formula units [Zn₄O₁₃-(C₈H₄)₃] giving rise to a total of 318 phonon branches. The phonon modes at Γ are classified as

$$\Gamma(q=0) = 9A_{1g}(R) + 3A_{1u} + 3A_{2g} + 9A_{2u} + 12E_u + 12E_g(R) \\ + 17T_{2u} + 24T_{2g}(R) + 24T_{1u}(IR) + 17T_{1g},$$

where R and IR correspond to Raman and infrared active, respectively. The crystal symmetry implies 105 Raman and 72 IR-active modes. In Table I, we list the calculated energies at Γ . We hope that our calculations will initiate more experimental work such as Raman/IR measurements to confirm the gamma phonon energies that we calculated here. In the absent of such high-resolution data, we have performed neutron inelastic scattering measurements of the phonon DOS and compared it with our calculations.

The experimental NIS spectrum shown in Fig. 4 was collected on a powder sample of MOF5 using the Filter Analyzer Neutron Spectrometer¹⁷ under conditions that provide full width at half maximum energy resolutions of 2–4.5 % of the incident energy over the range probed. To compare the NIS data with theory, the NIS spectrum was computed for a $10 \times 10 \times 10$ q -point grid within the incoherent approximation,^{16,18} with instrumental resolution taken into account. As shown in Fig. 4, the agreement between calcu-

TABLE I. List of phonon symmetries and calculated energies (in meV) of MOF5 at the Γ point of the primitive cell.

A_{2g}	2.6	A_{2u}	23.7	$3T_{1g}$	74.3	A_{1u}	121.0	$2E_g$	171.0
$3T_{1g}$	3.1	A_{1g}	28.7	$3T_{2g}$	74.6	$3T_{2u}$	121.0	$3T_{2g}$	171.3
$2E_g$	3.5	$3T_{1u}$	31.7	$3T_{1g}$	75.4	$2E_u$	121.1	A_{1g}	171.9
$3T_{2u}$	3.7	$3T_{2u}$	32.5	$3T_{2g}$	75.8	$2E_u$	124.8	$3T_{1g}$	183.0
$3T_{2u}$	5.3	$3T_{1g}$	33.3	$2E_g$	81.9	$3T_{1u}$	124.9	$2E_u$	183.5
$3T_{1u}$	6.8	A_{2u}	33.7	$3T_{2g}$	82.1	A_{2u}	124.9	$3T_{1u}$	183.5
$2E_u$	8.0	$3T_{1u}$	34.2	$3T_{1g}$	82.1	$3T_{2u}$	131.7	A_{2u}	183.5
$3T_{1g}$	9.5	$3T_{2g}$	34.3	$3T_{2g}$	82.2	$3T_{1u}$	131.7	$3T_{2g}$	183.6
A_{1u}	10.1	$2E_u$	34.6	A_{1g}	82.7	$2E_g$	137.1	$2E_g$	190.6
A_{2g}	10.8	$3T_{2g}$	43.0	$3T_{2u}$	88.8	$3T_{2g}$	137.2	$3T_{2g}$	190.7
$3T_{2g}$	10.9	$3T_{1g}$	43.5	$3T_{1u}$	89.2	A_{1g}	137.2	A_{1g}	191.1
$3T_{1g}$	11.0	A_{1u}	49.0	$2E_u$	95.7	$2E_g$	140.4	$3T_{2u}$	191.6
$3T_{2g}$	13.5	$3T_{2u}$	49.1	$3T_{1u}$	96.3	$2E_u$	140.6	$3T_{1g}$	193.5
$3T_{2u}$	13.6	$2E_u$	49.1	A_{2u}	97.5	$3T_{2g}$	140.6	$3T_{1u}$	196.2
$3T_{1u}$	14.2	$3T_{2g}$	54.5	$3T_{1g}$	98.3	$3T_{1u}$	140.6	$3T_{2g}$	197.5
$2E_g$	15.2	A_{1g}	55.3	$3T_{2g}$	98.5	A_{2u}	140.8	$2E_u$	381.6
$3T_{1g}$	15.7	$2E_g$	55.9	$2E_g$	102.3	A_{1g}	141.2	$3T_{1u}$	381.6
$3T_{1u}$	16.1	$3T_{2u}$	56.1	$3T_{2g}$	102.6	$3T_{1g}$	154.3	A_{2u}	381.6
$3T_{2u}$	17.4	$3T_{1u}$	56.1	A_{2g}	103.0	$3T_{2g}$	154.3	$3T_{1g}$	381.7
$2E_u$	18.5	$3T_{1u}$	57.8	A_{1g}	103.2	$2E_u$	167.9	$3T_{2g}$	381.7
$3T_{2g}$	18.5	$3T_{2g}$	59.0	$3T_{1g}$	103.2	$3T_{1u}$	168.1	$3T_{2u}$	383.0
$3T_{1g}$	18.9	A_{2u}	68.2	$2E_g$	103.3	A_{2u}	169.0	$3T_{1u}$	383.0
$3T_{2u}$	19.7	$2E_u$	68.6	$3T_{2u}$	107.7	$3T_{2u}$	170.1	$2E_g$	383.2
$3T_{2g}$	20.6	$3T_{1u}$	68.6	$3T_{1u}$	107.8	$3T_{1u}$	170.2	$3T_{2g}$	383.2
$2E_g$	21.5	$3T_{2u}$	72.5	$3T_{1g}$	119.5	$3T_{2u}$	171.0	A_{1g}	383.3
$3T_{1u}$	22.0	$3T_{1u}$	73.1	$3T_{2g}$	119.6	$3T_{1u}$	171.0		

lation and experiment is very good. In contrast to Raman and IR spectroscopy, neutron spectroscopy is not subject to any selection rules, thus all modes falling in the energy range covered by our measurement (~ 20 to 170 meV) were detected. Within this E range, the NIS spectrum is dominated by one-phonon processes. The two-phonon contribution coming from the combination of one-phonon processes is not significant. Also note that the NIS spectrum is dominated by hydrogen displacements because of the relatively large H neutron scattering cross section.

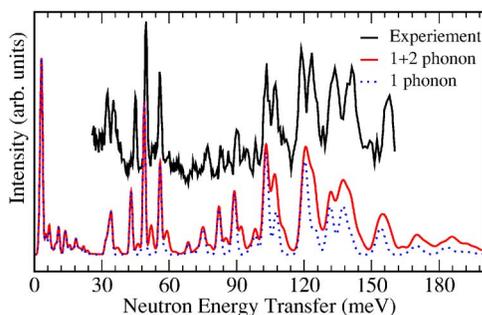


FIG. 4. (Color online) Measured NIS spectrum of MOF5 at 4 K (top curve) along with calculated spectrum (bottom curves). The calculated 1 (dotted line) and 1+2 phonon contributions are shown.

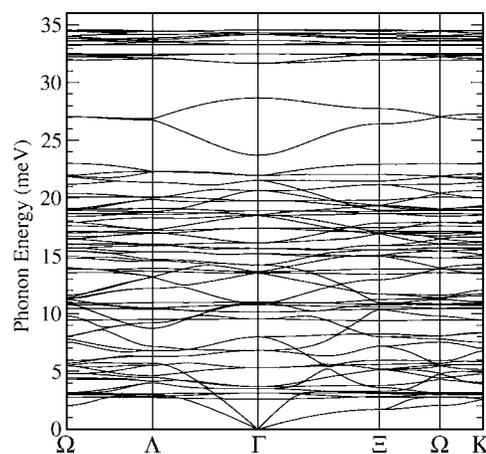


FIG. 5. Calculated phonon dispersion curves along high-symmetry directions in the Brillouin zone for MOF5. For clarity, only the low energy (0–40 meV) portion is shown.

Figure 5 shows the dispersion curves of the low-energy modes along high-symmetry directions in the Brillouin zone. The high energy modes are quite dispersionless and thus are not shown. It is interesting to point out that some of the modes have significant dispersion, such as those between 25 and 30 meV. This is surprising, considering the rigidity of the units (i.e., the ZnO_4 cluster and the BDC linker). We find that the dispersion comes from the points where these two rigid units are connected. This is also the reason for the very low shear modulus c_{44} . Another interesting result is the very low energy modes near 3 meV, which are quite flat. Some of these phonon modes will be discussed in detail below. Up to now, no phonon-dispersion measurement on MOF5 has been reported, partly due to the difficulty of growing a large single crystal needed for the experiment. We hope that in the near future, some of the phonon dispersions that we predict here can be experimentally confirmed.

We next discuss several interesting modes revealed by the phonon calculations. Animations of these phonon modes are available in Ref. 19 for direct visualization. The lowest energy mode (A_{2g} , 2.59 meV) is singly degenerate, with all C_6H_4 linkers twisting around the crystal axis direction. This mode is basically dispersionless (see Fig. 5), which is due to negligible interaction between two adjacent benzene linkers along the crystal axis. The second lowest energy mode (T_{1g} , 3.12 meV, three-fold degenerate) can be described as two of three C_6H_4 linkers twisting around the two corresponding crystal axes. These two softest twisting modes imply that the bonds between the organic linkers and the metal clusters are the most unstable part of the MOF structure. Their interaction with the acoustic modes could provide an explanation for the extraordinary small elastic constant c_{44} . The ~ 0.55 meV energy difference between the two modes suggests a coupling of the twisting motions of the nearest-neighbor benzene linkers.

Since the energy of the twisting mode is very low, one may wonder if the benzene ring is free to rotate at high temperatures. This could have important consequences for the hydrogen absorption dynamics in MOF5. If the linker is rotated 90° , it could block the channels connecting the cubic

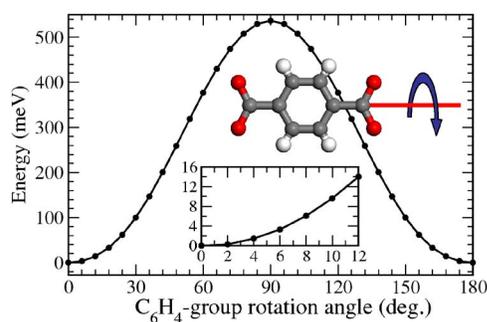


FIG. 6. (Color online) The variation of the total energy as one of the C_6H_4 groups (part of the BDC organic linker of MOF5) is twisted around the crystal axis direction. Note that the initial twisting does not cost much energy (see inset) although the energy barrier for the 180° flipping (two-site jumping) of the C_6H_4 group is rather large (~ 537 meV).

cavities in MOF5 available for hydrogen storage. Motivated by these arguments, we have investigated the dynamics of the linker using quasielastic neutron scattering measurements.²⁰ However, we did not observe any free rotation of the linker at high temperature nor any evidence of the π -rotational jumps of the linker. These findings later became clear when we looked at the potential curve as the C_6H_4 linker is rotated. We performed total energy calculations as a function of the rotational angle of the benzene plane. For simplicity, we only twisted one of the six benzene rings in the primitive cell. The results are shown in Fig. 6. The overall barrier is surprisingly large (~ 537 meV), consistent with the quasielastic neutron scattering results. However, twisting for a few degrees only costs an energy of several meV (see the inset of Fig. 6), in agreement with the phonon modes being very soft. The third lowest energy mode (3.50 meV, T_{2u} , threefold degenerate) involves all C_6H_4 linkers translating along crystal axis a , b , and c . All other modes with $E < 23$ meV are various combinations of the motion of the C_6H_4 linker as a whole and the vibration of the ZnO_4 clus-

ters. Two modes at slightly higher energy (23.69 meV, A_{2u} and 28.67 meV, A_{1g}) are the breathing modes of the ZnO_4 cluster, with the clusters vibrating in the unit cell out of phase and in phase, respectively. Most of other modes falling in the energy range of our NIS measurement are one of the twisting, stretching, breathing, bending, and wagging motions of the benzene rings. They can be roughly divided into two groups. With $E < \sim 70$ meV, the phonon modes are more dominated by the C displacements of the C_6H_4 linkers. The modes in the higher energy region are more dominated by H displacements.

The highest energy modes (390–395 meV, not covered by our NIS data) are totally dominated by the C-H covalent bond and all are associated with various C-H stretching modes of the C_6H_4 group.

In summary, we presented a detailed lattice dynamics study of MOF5 combining first-principles calculations and neutron inelastic scattering measurements. Our results indicated that MOFs are an interesting class of materials in terms of structural stability and dynamical properties. We identified the modes associated with the twisting of the linker to be the softest modes in the structure and therefore expected to be populated first with increasing temperature, eventually leading to structural instability. This is also consistent with the very small shear modulus c_{44} that we have calculated. Despite the very low energy of the linker twisting modes, we found a very large energy barrier for the full rotation of the linker. We hope that our calculations will initiate further experiments to confirm our predictions. In particular, our results suggest that MOF5 is very close to structural instability, possibly leading to an interesting structural transformation under high pressure.

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