



9-18-2008

D-Instanton Generated Dirac Neutrino Masses

Mirjam Cvetič

University of Pennsylvania, cvetic@cvetic.hep.upenn.edu

Paul Langacker

Princeton University

Follow this and additional works at: http://repository.upenn.edu/physics_papers

 Part of the [Physics Commons](#)

Recommended Citation

Cvetič, M., & Langacker, P. (2008). *D*-Instanton Generated Dirac Neutrino Masses. Retrieved from http://repository.upenn.edu/physics_papers/93

Suggested Citation:

M. Cvetič and P. Langacker. (2008). "D-instanton generated Dirac neutrino masses." *Physical Review D*. 78, 066012.

© 2008 The American Physical Society

<http://dx.doi.org/10.1103/PhysRevD.78.066012>

This paper is posted at Scholarly Commons. http://repository.upenn.edu/physics_papers/93

For more information, please contact repository@pobox.upenn.edu.

D-Instanton Generated Dirac Neutrino Masses

Abstract

We present a stringy mechanism to generate Dirac neutrino masses by *D*-instantons in an experimentally relevant mass scale without fine-tuning. Within type IIA string theory with intersecting *D*6-branes, we spell out specific conditions for the emergence of such couplings and provide a class of supersymmetric local $SU(5)$ grand unified models, based on the $Z_2 \times Z'_2$ orientifold compactification, where perturbatively absent Dirac neutrino masses can be generated by *D*2-brane instantons in the experimentally observed mass regime, while Majorana masses remain absent, thus providing an intriguing mechanism for the origin of small neutrino masses due to nonperturbative stringy effects.

Disciplines

Physical Sciences and Mathematics | Physics

Comments

Suggested Citation:

M. Cvetič and P. Langacker. (2008). "*D*-instanton generated Dirac neutrino masses." *Physical Review D*. **78**, 066012.

© 2008 The American Physical Society

<http://dx.doi.org/10.1103/PhysRevD.78.066012>

***D*-instanton generated Dirac neutrino masses**Mirjam Cvetič^{1,*} and Paul Langacker^{2,+}¹*Department of Physics and Astronomy, University of Pennsylvania, Philadelphia, Pennsylvania, USA*²*Institute for Advanced Study, Princeton, New Jersey, USA*

(Received 2 April 2008; published 18 September 2008)

We present a stringy mechanism to generate Dirac neutrino masses by *D*-instantons in an experimentally relevant mass scale without fine-tuning. Within type IIA string theory with intersecting *D6*-branes, we spell out specific conditions for the emergence of such couplings and provide a class of supersymmetric local SU(5) grand unified models, based on the $Z_2 \times Z'_2$ orientifold compactification, where perturbatively absent Dirac neutrino masses can be generated by *D2*-brane instantons in the experimentally observed mass regime, while Majorana masses remain absent, thus providing an intriguing mechanism for the origin of small neutrino masses due to nonperturbative stringy effects.

DOI: [10.1103/PhysRevD.78.066012](https://doi.org/10.1103/PhysRevD.78.066012)

PACS numbers: 11.25.Wx, 14.60.Pq

I. INTRODUCTION

Until recently, no satisfactory mechanism was known for generating either Majorana neutrino masses (for a see-saw mechanism) or small Dirac masses within the type IIA string theory context. Recent work [1,2] has shown that Majorana masses can be generated nonperturbatively by *D*-brane instantons. In this paper we show that, as an equally plausible alternative, *D*-brane instantons may instead generate small Dirac neutrino masses at the observed scale without fine-tuning.

In the past year there have been intriguing insights into *D*-brane instantons [1–4] which can generate perturbatively absent couplings of genuinely string theoretic origin with apparently no field theory analogs. (For reviews on the subject, see [5,6].) In type II string compactifications with *D*-branes the specific superpotential couplings are typically forbidden due to perturbatively conserved “anomalous” $U(1)$ factors. However, under specific conditions, that ensure the correct number of *D*-instanton fermionic zero modes, these couplings can be generated with a strength that is exponentially suppressed by the *D*-instanton action. The mechanism was originally proposed for generating Majorana neutrino masses, the μ -parameter and *R*-parity violating terms [1,2], as well as the study of supersymmetry breaking effects [4]. Further efforts in these directions focused on rational conformal field theory searches for global models with nonperturbatively realized Majorana masses [7], an explicit calculation of nonperturbative Majorana neutrino couplings within local orbifold constructions [8] and further studies of phenomenological implications for neutrino physics [9], as well as spelling out conditions for nonperturbatively induced Yukawa couplings $10 10 5_H$ within SU(5) grand unified models (GUT’s) [10]. There have also been further analyses of nonperturbative supersymmetry breaking effects [11,12].

While local realizations of models where this *D*-instanton mechanism were found [8], an important challenge was in the construction of globally consistent semirealistic string vacua which realize such nonperturbative effects (for efforts within semirealistic Gepner models, see [7]). The main difficulty seems to have been due to the specific type IIA frameworks, where conformal field theory techniques are applicable. On the other hand, the *T*-dual type I framework with magnetized *D*-branes, described by stable holomorphic bundles on compact Calabi-Yau spaces, is amenable to algebraic geometry techniques. There, the first classes of semirealistic globally consistent string vacua, where hierarchical couplings are realized by *D1*-brane instantons, were constructed [13].

The purpose of this paper is to present a new mechanism for small neutrino masses. Specifically, we present *D*-brane vacua with a standard model sector where perturbatively absent Dirac neutrino masses are generated nonperturbatively by *D*-instantons at a desired mass scale without fine-tuning, while at the same time ensuring the absence of nonperturbatively generated Majorana neutrino masses. This string mechanism should be contrasted with that for Majorana masses [1,2]. Both types of masses can be generated by *D*-instantons that satisfy specific conditions and are thus restricted to specific string vacuum solutions. However, unlike *D*-instanton generated Dirac neutrino masses, the desired mass scale for Majorana neutrino masses can be achieved only after some fine-tuning of the volumes of the cycles wrapped by *D*-instantons.

For the sake of concreteness we focus on the type IIA framework with intersecting *D6*-branes, though the *T*-dual formulation of conditions in the type I framework with magnetized *D9*-branes on Calabi-Yau spaces can also be described employing techniques developed in [13]. In these cases the *D*-instantons can generate exponentially suppressed Dirac neutrino masses at experimentally relevant mass scales, while the Majorana masses are not generated. Thus the proposal provides a nonperturbative string

*cvetic@cvtic.hep.upenn.edu

+pjl@ias.edu

realization of the origin of small Dirac neutrino masses in the absence of a seesaw mechanism [14].

As a concrete application we construct a class of local models, based on the $Z_2 \times Z'_2$ toroidal orientifold, which explicitly realize this scenario. Within this local construction we do not address the moduli stabilization issue, a difficult problem in string theory. The backreaction of supergravity fluxes and/or strong gauge dynamics, responsible for moduli stabilization, can also affect quantitative results for the proposed nonperturbative couplings (as well as global consistency constraints); however, this is beyond the scope of this paper.

The proposal is attractive since the classical instanton action enters the coupling at the exponentially suppressed level, proportional to the inverse string coupling and the volume of the cycles wrapped by the D -brane instanton. These couplings are thus generically extremely small, and thus generate tiny Dirac neutrino masses without any additional tuning of the volume of the cycles. This mechanism should be contrasted with the case of D -instanton generated Majorana neutrino masses [1,2] and some other nonperturbatively generated couplings, such as the $10\ 10\ 5_H$ Yukawa coupling of the $SU(5)$ GUT [10], where some fine-tuning of the volumes of the cycles wrapped by D -instantons is needed in order to obtain the couplings in the desired regime, e.g. for Majorana masses in the 10^{12-14} GeV range.

The specific focus is “semirealistic” constructions within the type IIA string theory framework with intersecting $D6$ -branes wrapping three-cycles in the internal space (for reviews, see [15,16]). Concrete realizations will be based on grand unified $SU(5)$ models [17–19], with chiral families of quarks and leptons. However, again, we do not address the moduli stabilization. Specifically, the string vacuum constructions should have the property that the Yukawa couplings responsible for Dirac neutrino masses are absent perturbatively due to global $U(1)$ selection rules. Focusing on type IIA theory, under suitable circumstances Euclidean $D2$ -branes ($E2$ -instantons) wrapping three-cycles in the internal space can break these global $U(1)$ symmetries to certain discrete subgroups and generate $U(1)$ violating interactions, as spelled out in [1,2,4].

The type IIA framework allows for a geometric formulation of the zero mode conditions in the presence of $E2$ -instantons wrapping rigid three-cycles and thus an explicit geometric interpretation of these nonperturbative string effects. Namely, the intersection numbers of the instanton and D -brane cycles, which specify the number of charged fermionic zero modes, are topological numbers. However, in order to illustrate the effects explicitly, we write expressions for these intersection numbers for a concrete local construction, based on the $Z_2 \times Z'_2$ toroidal orientifold, with Hodge numbers $(h_{11}, h_{12}) = (3, 51)$. We employ the notation of [20] (see also [21]), to which we refer for details of the geometry and the construction of

rigid cycles. The orbifold group is generated by θ and θ' acting as reflections in the first and last two tori, respectively. The $O6$ -plane parallel to the instanton is an $O6^+$ plane, whereas the three others are $O6^-$ planes.

The proposed framework requires three stacks a , b , and c of $D6$ -branes giving rise to a $U(5)_a \times U(1)_b \times U(1)_c$ gauge symmetry. The $U(5)_a$ splits into $SU(5)_a \times U(1)_a$, where the anomalous $U(1)_a$ gauge boson gets massive via the generalized Green-Schwarz mechanism and $U(1)_a$ appears as a global symmetry in the effective action. The matter transforming as $\mathbf{10}$ under $SU(5)_a$ arises at intersections of stack a with its image a' ; the matter fields transforming as $\bar{\mathbf{5}}$ as well as Higgs fields $\mathbf{5}_H$ and $\bar{\mathbf{5}}_H$ are located at intersections of stack a with b and b' or c and c' . The Abelian gauge group factors $U(1)_b$ and $U(1)_c$ also acquires massive gauge bosons due to the generalized Green-Schwarz mechanism.

The key input in the construction of the local model is summarized in Tables I and II. Table I lists the wrapping numbers of the $D6$ -branes wrapping bulk three-cycles Π_a^B , the building blocks of the local GUT models, and the wrapping numbers of the rigid three-cycle Π_Ξ of the $E2$ -instanton with the required zero mode structure.

We build a local model on the $Z_2 \times Z'_2$ orientifold by wrapping $D6$ branes on the bulk cycles specified by wrapping numbers (n_i^a, m_i^a) (for further details see [20]).

The intersection numbers in the respective (a, b) and (a, b') sectors are

$$\begin{aligned} I_{ab} &= 4 \prod_i (n_i^a m_i^b - n_i^b m_i^a), \\ I_{ab'} &= -4 \prod_i (n_i^a m_i^b + n_i^b m_i^a), \end{aligned} \quad (1)$$

where we choose a convention that the chiral superfields in the a, \bar{b} representation correspond to $I_{ab} < 0$. The symmetric and antisymmetric representations arise from the (a, a') sector:

TABLE I. Wrapping numbers of $D6$ -branes wrapping bulk three-cycles and the wrapping numbers of the $E2$ -instanton wrapping a rigid, orientifold action invariant, three-cycle on the $Z_2 \times Z'_2$ toroidal orientifold. The wrapping numbers n_2 and ν_2 are positive integers, co-prime with 2 and $2\nu_2/n_2$ integer, respectively. The simplest choice is $n_2 = \nu_2 = 1$. Another interesting (non-Abelian anomaly free) case is $n_2 = \nu_2 = 3$. The model is supersymmetric for the choice $\chi_1 = \chi_2 = 1/\sqrt{5}$, $\chi_3 = n_2\sqrt{5}/2$ of the complex structure toroidal moduli $\chi_i \equiv (R_2/R_1)_i$ of the i th two-torus.

Nos.	(n_a^1, m_a^1)	(n_a^2, m_a^2)	(n_a^3, m_a^3)
5_a	$(\nu_2, 2\nu_2/n_2)$	(1, 1)	(0, -1)
1_b	$(n_2, 2)$	(-1, 2)	(-1, 1)
1_c	(-1, 0)	(1, 1)	(-1, 1)
1_E	(1, 0)	(0, 1)	(0, -1)

$$I^{\text{antisymm}} = \frac{1}{2}(I_{aa'} + I_{aO6}), \quad I^{\text{symm}} = \frac{1}{2}(I_{aa'} - I_{aO6}), \quad (2)$$

where

$$I_{aa'} = -32n_1^a m_1^a n_2^a m_2^a n_3^a m_3^a, \\ I_{aO6} = -8m_1^a m_2^a m_3^a + 8n_1^a n_2^a m_3^a - 8m_1^a n_2^a n_3^a + 8n_1^a m_2^a n_3^a. \quad (3)$$

As shown in [8], the background of this model exhibits one class of so-called rigid $O(1)$ instantons. For completeness, in the conventions of [20], we give the full expression for the rigid three-cycle wrapped by the $E2$ -instanton

$$\begin{aligned} \Pi_{\Xi} = & \frac{1}{4} \Pi_{\Xi}^B - \frac{1}{4} \sum_{i,j \in (13) \times (12)} \alpha_{ij,m}^{\theta} + \frac{1}{4} \sum_{j,k \in (12) \times (12)} \alpha_{jk,n}^{\theta'} \\ & + \frac{1}{4} \sum_{i,k \in (13) \times (12)} \alpha_{ik,m'}^{\theta\theta'} \end{aligned} \quad (4)$$

where Π_{Ξ}^B wraps the cycle $[(1,0)(0,1)(0,-1)]$. The twisted three-cycles $\alpha_{jk,n}^{\theta}$ [$\alpha_{jk,m}^{\theta}$] can be understood as a product one-cycle $[a]^{I^{\theta}}$ [$[b]^{I^{\theta}}$] on the I^{θ} th two-torus and a two-cycle S^2 —a blow-up of $(i,j) \in (1,2,3,4) \times (1,2,3,4)$ orbifold fixed points. (For further details see [20].) The intersection number in the (a,E) specifies the number of chiral fermionic modes and is of the form

$$I_{aE} = \prod_i (n_i^a m_i^E - n_i^E m_i^a). \quad (5)$$

Again the convention $I_{aE} < 0$ corresponds to chiral fermionic zero modes in the $(a, -1_E)$ representation. Note that since $D6$ -branes wrap (nonrigid) bulk three-cycles, the intersection number in the (a,E) sector does not depend on fractional twisted three-cycles of the instanton.

The supersymmetry conditions are ensured by requiring that the three-cycles are special Lagrangians with respect to the same holomorphic three-form. In the case of toroidal compactification these take the form

$$m_1^a m_2^a m_3^a - \sum_{i \neq j \neq k \neq i} \frac{n_i^a n_j^a n_k^a}{\chi_i \chi_j \chi_k} = 0, \\ n_1^a n_2^a n_3^a - \sum_{i \neq j \neq k \neq i} m_i^a m_j^a m_k^a \chi_i \chi_j \chi_k > 0, \quad (6)$$

where $\chi_i \equiv \left(\frac{R_2}{R_1}\right)_i$ is the complex structure modulus for the i th two-torus.

At the intersection of the $U(1)_b$ and $U(1)_c$ $D6$ -branes the chiral matter corresponds to the right-handed neutrinos N_R . We insist that there only exist chiral states with such $U(1)_b$ and $U(1)_c$ charges that they cannot couple perturbatively in Yukawa couplings $55N_R$, i.e., $U(1)$ charges are perturbatively violated for such couplings, and thus Dirac masses corresponding to them are not present at this stage. In addition we want to ensure that the D -instanton zero modes induce the Dirac neutrino masses, while the Majorana

neutrino masses are absent. These constraints can be ensured by the following specific signs for the intersection numbers:

$$I_{ab} = 0, \quad I_{ab'} < 0, \quad I_{bc} = 0, \\ I_{bc'} < 0, \quad I_{ac} = 0, \quad I_{ac'} > 0, \quad (7)$$

resulting in the following left-handed chiral superfield representations: $(5_a, 1_b)$, $(1_b, 1_c)$, and $(\bar{5}_a, -1_c)$. Therefore, $N_R = (1_b, 1_c)$ [or any singlets in (b, b') and (c, c') sectors with respective charges $\pm 2_b$ and $\pm 2_c$] cannot couple perturbatively via Yukawa couplings to 5_a and $\bar{5}_b$. We also assume that the states in the $N = 2$ sector of (a, b) and (b, c) system are massive by wrapping the respective D -branes on parallel one-cycles that do not coincide. The wrapping numbers presented in the Table I comply with the above intersection number conditions and have the following specific values:

$$I_{ab} = 0, \quad I_{ab'} = -16\nu_2, \quad I_{bc} = 0, \\ I_{bc'} = -16, \quad I_{ac} = 0, \quad I_{ac'} = 16\frac{\nu_2}{n_2}, \quad (8)$$

as are also listed in terms of the multiplicity of the states in the spectrum in Table II.

To generate the desired Yukawa couplings at the non-perturbative level the instanton has to have a spectrum of zero modes ensured by the intersection numbers:

$$I_{aE} = 0, \quad I_{bE} = 2, \quad I_{cE}^{N=2} = 1. \quad (9)$$

Note that for the nonchiral intersection with $I_{cE} = 0$, however, the $N = 2$ (c, E) sector has one vector pair of massless modes. To ensure that the $N = 2$ (a, E) sector does not have massless modes, the parallel one-cycles on the third two-torus for the $D6_a$ -brane and the $E2$ -instanton do not coincide. We therefore ensure the correct structure of the zero modes, i.e., two zero modes $\bar{\lambda}_b$ in the representation $(-1_b, 1_E)$ and one vector pair $\lambda_c + \bar{\lambda}_c$, $(-1_c, 1_E) + (1_c, -1_E)$.

Importantly, D -instanton zero modes (9) cannot generate Majorana masses for $N_R = (1_b, 1_c)$. We have also

TABLE II. Chiral matter spectrum for the local $SU(5)$ GUT models with intersecting $D6$ -branes on the $Z_2 \times Z_2'$ orientifold. The wrapping numbers of the $D6$ -branes are depicted in Table I. A special case $\nu_2 = n_2 = 3$ corresponds to the four family example and is free of non-Abelian anomalies. Another four family example corresponds to $\nu_2 = n_2 = 1$; however, in this case additional ‘‘filler’’ branes would have to be added to cancel non-Abelian anomalies.

Sector	Number	$U(5)_a \times U(1)_b \times U(1)_c$
(a, a')	$4(\nu_2 - 2\frac{\nu_2}{n_2})$	$\mathbf{10}_{(2,0,0)} + \mathbf{\bar{15}}_{(-2,0,0)}$
(a, b')	$16\nu_2$	$\mathbf{5}_{(1,1,0)}$
(a, c')	$16\frac{\nu_2}{n_2}$	$\mathbf{\bar{5}}_{(-1,0,-1)}$
(b, c')	16	$\mathbf{1}_{(0,1,1)}$

checked that in the concrete setup there is no other \tilde{E} -instanton that could induce Majorana masses. Such an instanton would have to wrap a rigid three-cycle with the intersection numbers:

$$\begin{aligned} I_{\tilde{E}\tilde{E}'} &= 0, & I_{E\tilde{E}} &= 0, & I_{a\tilde{E}} &= 0, \\ I_{b\tilde{E}} &= 2, & I_{c\tilde{E}} &= 2. \end{aligned} \quad (10)$$

The first three constraints require $(n_3^{\tilde{E}}, m_3^{\tilde{E}}) = (0, -1)$; however, the last two constraints cannot be satisfied for any wrapping numbers $(n_{1,2}^{\tilde{E}}, m_{1,2}^{\tilde{E}})$, corresponding to a rigid, supersymmetric three-cycle.

Note that specific conditions on the intersection numbers between D -branes (7) and the intersection numbers of the D -instanton with D -branes (9) apply to a general type IIA setup and ensure a mechanism that generates perturbatively absent Dirac neutrino masses due to $E2$ -instantons, which cannot generate Majorana masses for N_R 's.

The contribution to the superpotential arises from the string amplitudes as shown in Fig. 1. These four fermionic zero modes λ can be saturated via the two disk diagrams, thereby generating superpotential contributions to the Yukawa couplings $\tilde{5}5N_R$ of the type

$$Y = \exp(-S_{\text{inst}}) = x \exp\left(-\frac{2\pi}{\alpha_{\text{GUT}}} \frac{\text{Vol}_{E2}}{\text{Vol}_{D6a}}\right), \quad (11)$$

where $\frac{\text{Vol}_{E2}}{\text{Vol}_{D6a}} = (6\nu_a)^{-1}$ for the specific local construction. The numerical factor, x , is expected to be of order 1. A more detailed conformal field theory calculation of the three-point and four-point disc amplitudes [8,22] emerging from the geometric local setup in Fig. 1 could in principle generate additional world-sheet instanton suppression terms, as were explicitly calculated for the D -instanton induced Majorana masses in [8]. In addition, further summation over $Z_2 \times Z_2$ images of the E -instanton can quantitatively affect x , as again was addressed in [8].

Taking $\nu_2 = 1$, $\alpha_{\text{GUT}} \sim \{25^{-1}, 30^{-1}\}$ and a VEV of the Higgs doublet ~ 100 GeV yields neutrino Dirac masses in the range

$$m_{\text{Dirac}} \sim \{2 \times 10^{-3}, 0.4\} \text{ eV}, \quad (12)$$

which is a reasonable regime for the allowed range for the neutrino masses. Note, however, that the case $\nu_2 = n_2 = 3$

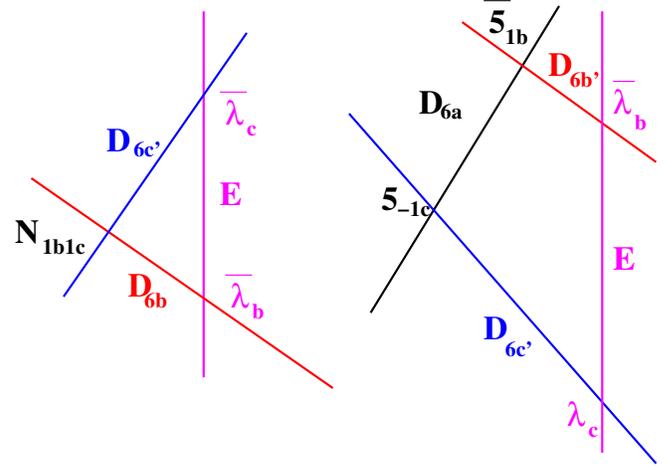


FIG. 1 (color online). String disc diagrams that ensure the absorption of the fermionic zero modes $2 \times \bar{\lambda}_b$ and $\lambda_c + \bar{\lambda}_c$.

would require too small a value $\alpha_{\text{GUT}} \sim 10^{-2}$ to bring m_{Dirac} to the 10^{-3} eV regime.

In conclusion, we have presented specific conditions for a concrete proposal, explicitly implemented within a local supersymmetric $SU(5)$ construction with intersecting $D6$ -branes, where string D -instantons ($E2$ -instantons) can generate perturbatively absent Dirac neutrino masses while Majorana masses remain absent. The exponentially suppressed coupling can be engineered (without fine-tuning) to yield Dirac neutrino masses in the observed regime $\geq 10^{-3}$ eV. While the concrete setup was in the context of type IIA string theory, realizations in the T -dual picture, namely, the type I framework, may be amenable to constructions of global models on compact Calabi-Yau spaces where string D -instanton couplings are realized within globally consistent models, *à la* [13].

ACKNOWLEDGMENTS

We would like to thank Timo Weigand for discussions. We are especially grateful to Robert Richter for discussions and comments on the manuscript. This research was supported in part by the National Science Foundation under Grant No. PHY-0503584 (P.L.), the Department of Energy Grant No. DOE-EY-76-02-3071 (M.C.), the Fay R. and Eugene L. Langberg Endowed Chair (M.C.) and by the Friends of the IAS (P.L.).

- [1] R. Blumenhagen, M. Cvetič, and T. Weigand, Nucl. Phys. **B771**, 113 (2007).
 [2] L. E. Ibáñez and A. M. Uranga, J. High Energy Phys. **03** (2007) 052.
 [3] M. Haack, D. Krefl, D. Lüst, A. Van Proeyen, and M. Zagermann, J. High Energy Phys. **01** (2007) 078.

- [4] B. Florea, S. Kachru, J. McGreevy, and N. Saulina, J. High Energy Phys. **05** (2007) 024.
 [5] N. Akerblom, R. Blumenhagen, D. Lüst, and M. Schmidt-Sommerfeld, Fortsch. Phys. **56**, 313 (2008).
 [6] M. Cvetič, R. Richter, and T. Weigand, arXiv:0712.2845.
 [7] L. E. Ibáñez, A. N. Schellekens, and A. M. Uranga, J. High

- Energy Phys. 06 (2007) 011.
- [8] M. Cvetič, R. Richter, and T. Weigand, Phys. Rev. D **76**, 086002 (2007).
- [9] S. Antusch, L. E. Ibáñez, and T. Macri, J. High Energy Phys. 09 (2007) 087.
- [10] R. Blumenhagen, M. Cvetič, D. Lüst, R. Richter, and T. Weigand, Phys. Rev. Lett. **100**, 061602 (2008).
- [11] O. Aharony, S. Kachru, and E. Silverstein, Phys. Rev. D **76**, 126009 (2007).
- [12] O. Aharony and S. Kachru, J. High Energy Phys. 09 (2007) 060.
- [13] M. Cvetič and T. Weigand, Phys. Rev. Lett. **100**, 251601 (2008).
- [14] Small Dirac masses in supersymmetric field theory may also be generated by higher dimensional operators in the superpotential [23,24] or Kähler potential [25], though this has not yet been implemented in a string construction. For a review, see [26]. If such terms were present in the proposed D -brane constructions they would merely be additive. Such higher dimensional operators have not been studied systematically in these classes of constructions.
- [15] R. Blumenhagen, M. Cvetič, P. Langacker, and G. Shiu, Annu. Rev. Nucl. Part. Sci. **55**, 71 (2005).
- [16] R. Blumenhagen, B. Körs, D. Lüst, and S. Stieberger, Phys. Rep. **445**, 1 (2007).
- [17] R. Blumenhagen, B. Körs, D. Lüst, and T. Ott, Nucl. Phys. **B616**, 3 (2001).
- [18] M. Cvetič, G. Shiu, and A. M. Uranga, Nucl. Phys. **B615**, 3 (2001).
- [19] M. Cvetič, I. Papadimitriou, and G. Shiu, Nucl. Phys. **B659**, 193 (2003); **696**, 298(E) (2004).
- [20] R. Blumenhagen, M. Cvetič, F. Marchesano, and G. Shiu, J. High Energy Phys. 03 (2005) 050.
- [21] E. Dudas and C. Timirgaziu, Nucl. Phys. **B716**, 65 (2005).
- [22] M. Cvetič and I. Papadimitriou, Phys. Rev. D **68**, 046001 (2003); **70**, 029903(E) (2004).
- [23] G. Cleaver, M. Cvetič, J. R. Espinosa, L. L. Everett, and P. Langacker, Phys. Rev. D **57**, 2701 (1998).
- [24] P. Langacker, Phys. Rev. D **58**, 093017 (1998).
- [25] D. A. Demir, L. L. Everett, and P. Langacker, Phys. Rev. Lett. **100**, 091804 (2008).
- [26] P. Langacker, arXiv:0801.1345.