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Potential and Impedance Imaging of Polycrystalline BiFeO$_3$ Ceramics

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Abstract
Electrostatic-force-sensitive scanning probe microscopy (SPM) is used to investigate grain boundary behavior in polycrystalline BiFeO₃ ceramics. Scanning surface potential microscopy (SSPM) of a laterally biased sample exhibits potential drops due to resistive barriers at the grain boundaries. In this technique, the tips acts as a moving voltage probe detecting local variations of potential associated with the ohmic losses within the grains and at the grain boundaries. An approach for the quantification of grain boundary, grain interior, and contact resistivity from SSPM data is developed. Scanning impedance microscopy (SIM) is used to visualize capacitive barriers at the grain boundaries. In SIM, a dc-biased tip detects the variations of local potential induced by the lateral ac voltage applied to the sample. Unlike the traditional dc and ac transport measurement, both of these techniques are sensitive to the variation of local potential (SSPM) or local voltage oscillation amplitude and phase (SIM), rather than to current. Therefore, special attention is paid to the relationship between SSPM and SIM images and data obtained from traditional impedance spectroscopy and dc transport measurements. For BiFeO₃ ceramics excellent agreement between the local SIM measurements and impedance spectroscopy data are demonstrated.

Comments
### Introduction

Applications of semiconducting oxides as chemical sensors, solar and fuel cells, and electronic ceramic devices attract significant interest to these materials.\(^1\) in many cases, the macroscopic properties of ceramics are determined by the microstructure, particularly by grain boundary structure and topology. The most versatile tools for the characterization of oxide ceramics are impedance spectroscopy and dc transport measurement.\(^1\)–\(^8\) Through analysis of the frequency dependence of the amplitude and phase of a bias-induced current the major relaxation processes within the solid can be associated with individual microstructural elements. The typical applications of impedance spectroscopy differentiate grain boundary, grain interior, and electrode impedances by fitting the impedance data to corresponding equivalent circuit models. This approach addresses the average properties of a polycrystalline material and little or no information is obtained about the properties of the individual elements. Moreover, for complex (e.g., multiphase) systems the equivalent circuits rapidly become complex and nonunique. Additional complications arise in the impedance spectroscopy of ferroelectric materials in which domain walls can participate in the relaxation processes.\(^9\) Therefore, interpretation of impedance spectra of a polycrystalline material in terms of the microstructure represents a complex problem. Finally, the correlation between atomic structure of grain boundaries and transport properties requires spatially resolved transport data. A number of approaches have been suggested to separate the impedance response of individual structural elements, such as microimpedance spectroscopy using patterned contact arrays\(^10\)–\(^12\) or studies of bicrystal samples.\(^13\)–\(^14\) Using these techniques, Fleig and Maier\(^15\) have been able to perform impedance spectroscopy over a single grain boundary. However, this approach relies heavily on the preset contact pattern, and the maximum resolution achieved by this technique (~20 μm) is well below the resolution of microscopic techniques. Nonuniform current distribution between contacts hinders the studies of voltage-dependent properties of individual interface.\(^16\) The small contact area inevitably leads to high contact resistance that contributes heavily to both ac and dc transport data. Specifically, as shown by Mason et al., high contact resistance precludes quantitative four-probe impedance spectroscopy due to the voltage divider effect.\(^17\)–\(^18\) For dc transport measurements, contact resistance higher than the input impedance of the voltmeter precludes reliable conductivity measurements. Increasing contact resistance for small contact areas imposes a fundamental limit on local characterization of materials properties by current-based techniques.

Alternatively, spatially resolved electrostatic properties of surfaces can be addressed by variants of the scanning probe microscopy (SPM) techniques. SPM has been successfully applied to semiconductor,\(^19\) organic,\(^20\) and ferroelectric\(^21\)–\(^22\) surfaces, as well as to defects,\(^23\)–\(^24\) and photoinduced\(^25\)–\(^26\) and thermal phenomena\(^27\)–\(^28\) in these materials. A number of SPM studies on grain boundary related phenomena have also been reported.\(^29\)–\(^30\) However, despite a few notable exceptions, the information provided by SPM has been limited to static properties of the surfaces.\(^31\)–\(^33\) The primary limitation of all SPM techniques as applied to materials characterization stems from the fact that they are ultimately based on tip–surface interactions; therefore, SPM analysis of the lateral transport properties of material requires an additional effort.

In the present paper, a general framework for application of scanning probe microscopy to characterization of ac and dc transport properties of individual interfaces is demonstrated through an analysis of polycrystalline bismuth ferrite. BiFeO\(_3\) simultaneously exhibits both ferroelectric (\(T_C = 830^\circ\)C) and long-range antiferromagnetic G-type ordering (\(T_N = 370^\circ\)C).\(^34\) Because of this magnetoelectric coupling, it has been proposed that BiFeO\(_3\) ceramics systems could be used to develop novel memory device applications. Extensive structural, magnetic, and electric studies of various BiFeO\(_3\) solid solutions systems have been reported.\(^35\)–\(^37\) However, perhaps because of the difficulty of obtaining a single-phase material, there have been fewer reported studies of pure BiFeO\(_3\). The majority of the published studies of pure BiFeO\(_3\) have focused on understanding the atomic structure and complex magnetic ordering. Most of these studies have reported the existence of small impurity phases in their samples, but the impurity levels were typically deemed too low to affect the structural and magnetic studies. In contrast, the electric and dielectric properties of BiFeO\(_3\), which could be strongly affected by small amounts of impurities and ferroelectric behavior, have been inadequately investigated. Our preliminary work on BiFeO\(_3\) suggests that the segregation of these impurities creates resistive grain boundaries, leading to complex impedance behavior and

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Electrostatic-force-sensitive scanning probe microscopy (SPM) is used to investigate grain boundary behavior in polycrystalline BiFeO\(_3\) ceramics. Scanning surface potential microscopy (SSPM) of a laterally biased sample exhibits potential drops due to resistive barriers at the grain boundaries. In this technique, the tips acts as a moving voltage probe detecting local variations of potential associated with the ohmic losses within the grains and at the grain boundaries. An approach for the quantification of grain boundary, grain interior, and contact resistivity from SSPM data is developed. Scanning impedance microscopy (SIM) is used to visualize capacitive barriers at the grain boundaries. In SIM, a dc-biased tip detects the variations of local potential induced by the lateral ac voltage applied to the sample. Unlike the traditional dc and ac transport measurement, both of these techniques are sensitive to the variation of local potential (SSPM) or local voltage oscillation amplitude and phase (SIM), rather than to current. Therefore, special attention is paid to the relationship between SSPM and SIM images and data obtained from traditional impedance spectroscopy and dc transport measurements. For BiFeO\(_3\) ceramics excellent agreement between the local variations of potential associated with the ohmic losses below the resolution of microscopic techniques. Nonuniform current distribution between contacts hinders the studies of voltage-dependent properties of individual interface. The small contact area inevitably leads to high contact resistance that contributes heavily to both ac and dc transport data. Specifically, as shown by Mason et al., high contact resistance precludes quantitative four-probe impedance spectroscopy due to the voltage divider effect. For dc transport measurements, contact resistance higher than the input impedance of the voltmeter precludes reliable conductivity measurements. Increasing contact resistance for small contact areas imposes a fundamental limit on local characterization of materials properties by current-based techniques.

Alternatively, spatially resolved electrostatic properties of surfaces can be addressed by variants of the scanning probe microscopy (SPM) techniques. SPM has been successfully applied to semiconductor, organic, and ferroelectric surfaces, as well as to defects, and photoinduced and thermal phenomena in these materials. A number of SPM studies on grain boundary related phenomena have also been reported. However, despite a few notable exceptions, the information provided by SPM has been limited to static properties of the surfaces. The primary limitation of all SPM techniques as applied to materials characterization stems from the fact that they are ultimately based on tip–surface interactions; therefore, SPM analysis of the lateral transport properties of material requires an additional effort.

In the present paper, a general framework for application of scanning probe microscopy to characterization of ac and dc transport properties of individual interfaces is demonstrated through an analysis of polycrystalline bismuth ferrite. BiFeO\(_3\) simultaneously exhibits both ferroelectric (\(T_C = 830^\circ\)C) and long-range antiferromagnetic G-type ordering (\(T_N = 370^\circ\)C). Because of this magnetoelectric coupling, it has been proposed that BiFeO\(_3\) ceramics systems could be used to develop novel memory device applications. Extensive structural, magnetic, and electric studies of various BiFeO\(_3\) solid solutions systems have been reported. However, perhaps because of the difficulty of obtaining a single-phase material, there have been fewer reported studies of pure BiFeO\(_3\). The majority of the published studies of pure BiFeO\(_3\) have focused on understanding the atomic structure and complex magnetic ordering. Most of these studies have reported the existence of small impurity phases in their samples, but the impurity levels were typically deemed too low to affect the structural and magnetic studies. In contrast, the electric and dielectric properties of BiFeO\(_3\), which could be strongly affected by small amounts of impurities and ferroelectric behavior, have been inadequately investigated. Our preliminary work on BiFeO\(_3\) suggests that the segregation of these impurities creates resistive grain boundaries, leading to complex impedance behavior and...
grain boundary barrier layer (GBBL) dielectric effects. In the present study, it is shown that SPM can be used to facilitate the understanding of the macroscopic impedance and dielectric properties by clarifying the local ac and dc transport properties of polycrystalline BiFeO₃ samples. Scanning surface potential microscopy (SSPM) is applied to a laterally dc-biased sample and the tip acts as a moving voltage probe detecting local potential variations associated with the ohmic losses within the grains and at the grain boundaries. A recently proposed scanning impedance microscopy (SIM) technique is used to address the ac transport properties.

II. Theoretical Development

SSPM is a well-established SPM technique that allows the local potential to be determined with submicrometer resolution. SIM is an improved scanning probe technique that allows local impedance imaging. The information provided by SSPM and SIM on laterally biased devices is summarized in Fig. 1. Quantification of dc and ac transport properties of multiple interface systems from SSPM and SIM data are considered below.

1) dc Transport Properties by SSPM

SSPM has been successfully used to detect stray fields over Schottky double barriers in electroceramics and semiconductors and to image potential drops at laterally biased grain boundaries. Reconstruction of current–voltage properties of a single grain boundary in a bicrystal was recently illustrated. The more general case of a polycrystalline sample is developed here. Assuming the series arrangement of the grains, total resistance of sample, \( R_s \), can be written as

\[
R_s = R_{lt} + N R_{gi} + (N - 1) R_{gb} + R_e \tag{1}
\]

where \( R_e \) is the resistance of the left contact, \( R_{gb} \) the grain boundary resistance, \( R_{gi} \) is the resistance of the grain interior, and \( N = n + m + 1 \) is the number of the grains, \( n \) and \( m \) being the number of grains to the right and left of the investigated grain. Equation (1) can be interpreted in terms of the brick-layer model, where \( R_s \) is \( R_{sample} S_{sample}/S_{grains} \), where \( R_{sample} \) is sample resistance, \( S_{grains} \) average grain size, and \( S_{sample} \) is sample cross-section area. The potential drop at the individual grain boundary, \( \Delta V_{gb} = V_1 - V_2 \), is

\[
\Delta V_{gb} = \left( \frac{R_{gb}}{R_s} \right) V \tag{2}
\]

where \( V \) is the lateral dc bias. The potential drop within the grain, \( \Delta V_{gi} = V_3 - V_4 \), can be determined as

\[
\Delta V_{gi} = \left( \frac{R_{gi}}{R_s} \right) V = \left( \frac{1}{N} \right) \left( \frac{\alpha}{\alpha + 1} \right) R_s \tag{3}
\]

where \( \alpha = \frac{R_{gb}}{R_{gi}} \).

Provided that the electrode resistance is small, \( R_e + R_{gb} << N(R_{gb} + R_{gi}) \), the total resistance can be measured directly and the grain boundary and grain interior resistances are

\[
R_{gb} = \left( \frac{1}{N} \right) \left( \frac{\alpha}{\alpha + 1} \right) R_s \tag{5a}
\]

\[
R_{gi} = \left( \frac{1}{N} \right) \left( \frac{1}{\alpha + 1} \right) R_s \tag{5b}
\]

This approach can also be extended to high electrode resistance. In this case, direct measurement of the surface potential close to the right electrode and close to the left electrode allows potential drops at the electrodes to be distinguished from the potential drop in the bulk and all three components of dc resistivity can be determined.

2) ac Transport Properties by SIM

The direct application of SIM allows quantitative measurements of phase changes within the grain and grain boundaries as well as delineation of the resistive versus capacitive behavior of individual microstructural elements.

![Fig. 1](image-url)

Fig. 1. Schematic diagram comparing (a) scanning surface potential microscopy (SSPM) and (b) scanning impedance microscopy (SIM). SSPM yields information on potential drops within the grains and at the grain boundaries (c), thus allowing the analysis of dc transport properties of the sample similar to 4-probe resistance measurements. SIM yields information on the local voltage amplitude and phase angle (d) and ac transport properties.
Assuming the series arrangement of the grains (Fig. 2(b)), the total impedance of the sample, $Z_s$, is

$$Z_s = Z_n + N(Z_{gb} + Z_g) + Z_i$$

where $Z_n$ is the impedance of the left contact, $Z_i$ is the impedance of the right contact, $Z_{gb}$ is the grain boundary impedance, $Z_g$ is the impedance of the grain interior, and $N = n + m + 1$ is the number of grains. Grain boundary and grain interior impedances are modeled by capacitive and resistive elements in parallel,

$$Z_{gb} = \frac{1}{1/R_{gb} + i2\pi fC_{gb}}$$

$$Z_g = \frac{1}{1/R_i + i2\pi fC_i}$$

where $f$ is frequency, $R_{gb}$ and $C_{gb}$ are the grain boundary resistance and capacitance, and $R_i$ and $C_i$ are the grain interior resistance and capacitance. As for the dc transport, Eq. (6) can be interpreted in terms of the brick-layer model, where measured grain boundary and bulk resistances and capacitances for the sample are scaled linearly and reciprocally by the number of grains in the cross section of the sample.

The phase change at the grain boundary is calculated from the ratio of impedances between the region to the left and to the right of the grain boundary and the ground:

$$\beta = \frac{nZ_{gb} + (n + 1)Z_g + Z_i}{(n + 1)(Z_{gb} + Z_g) + Z_i}$$

as (impedance divider effect)

$$\tan (\varphi_{gb}) = \frac{\text{Im}(\beta)}{\text{Re}(\beta)}$$

The ratio of voltage oscillation amplitudes on the left and on the right is

$$\frac{A_2}{A_1} = |\beta|$$

For high tip biases during SIM measurement this ratio is equal to the ratio of the tip oscillation signal (lock-in output) and is independent of the properties of the tip. Similar analysis for the grain interior and electrodes is straightforward.

It should be noted that Eqs. (1) and (6) are directly interpretable in terms of the brick-layer model. Indeed, the grain boundary and bulk impedances scale reciprocally with cross-section area; therefore, impedance ratios defined in Eqs. (4) and (8) do not depend on sample area.

It is illustrative to model the typical behavior of these values for a realistic material. Figure 3 shows impedance spectra and the SIM phase and amplitude characteristics of the grain boundary and grain interior calculated for a circuit in Fig. 2(b) with $C_{gb} = 10 \text{ nF}$, $R_{gb} = 1 \text{ k\Omega}$, $C_i = 1 \mu\text{F}$, $R_i = 3 \text{ k\Omega}$, $C_{cl} = 3 \mu\text{F}$, and $R_{cl} = 10 \text{ k\Omega}$. Calculated responses without a contact impedance contribution (generic termination) (1), including contact impedance (2), assuming only contact resistance (3), and for contact resistance $R_{cl} = 100 \text{ M\Omega}$ (4) are shown. The impedance spectra exhibit two well-defined half arcs corresponding to grain boundaries and grain interior and partially overlapping electrode half arc. Modeling the SIM grain boundary phase shift shows that the phase shift is a maximum for the frequency between characteristic relaxation frequencies for the bulk and grain boundary. This frequency is further referred to as the voltage resonant frequency of the interface. The grain interior phase shift is equal to the grain boundary phase shift in magnitude and opposite in sign. The only exception is for a purely resistive circuit termination. In this case, there is an asymmetry between the grain boundary and grain interior phase shifts. It should be noted that the typical setup for SIM imaging includes current limiting resistors in the circuit and, therefore, resistive termination is usual. The grain boundary amplitude ratio is small below the resonant frequency and goes to unity above the resonant frequency. Therefore, amplitude changes are expected on the grain boundaries below the resonant frequency (dc limit), while for high frequencies grain boundaries are not associated with amplitude changes. In contrast, the grain interior amplitude ratio (i.e., local slope) in the dc limit is equal to $R_{gb}/(R_{gb} + R_{cl})$ and decreases for higher frequencies, but never achieves unity. Therefore, in the high-frequency limit the SIM amplitude is expected to exhibit uniform decay along the sample surface and grain boundary barriers are not visible in the SIM amplitude image.

This observation implies that the SIM imaging of polycrystalline ceramics will exhibit phase shifts on the interface and phase shifts of the opposite sign in the grain interior. The presence of the resistive circuit termination suppresses the latter for frequencies above the resonant frequency. At the same time, below the resonant frequency the amplitude drops at the interfaces and exhibits uniform behavior within the grains similarly to the dc potential behavior. Above the resonant frequency there is no amplitude change at the interfaces, while there is an amplitude drop within the grain that can be determined as a uniform slope.

### III. Experimental Procedure

The AFM and SSPM measurements were performed with a commercial instrument (Digital Instruments Dimension 3000 NS-III) using metal-coated tips ($l \approx 225 \mu\text{m}$, resonant frequency = 60 kHz, $k = 1-5 \text{ N/m}$). To perform SIM, the AFM was additionally...
equipped with a function generator and lock-in amplifier (DS340, SRS 830, Stanford Research Systems) as described elsewhere. The lift height for the interleave scans in the SSPM and SIM was usually 100 nm; the scan rate varied from 0.5 Hz for large scans to 1 Hz for smaller scans. The driving voltage was 5 V for SSPM and 10 V for SIM. To reduce the effect of drift the images were acquired with the grain boundaries preferentially oriented along the slow scan axis. Topographical images were processed by line flattening. SSPM and SIM images were processed only by constant background subtraction. Phase, amplitude, and potential profiles were obtained by averaging the SIM and SSPM images along the slow scan axis. The BiFeO₃ sample was prepared using a modified version of the procedure first described by Achenbach et al. The dried oxide reagents, Bi₂O₃ (99.999% pure, Cerac Incorporated) and Fe₂O₃ (99.99% pure, Fisher Scientific), were mixed together in a 5% Bi₂O₃-rich molar ratio and ball-milled for 12 h. This excess of Bi₂O₃ was sufficient to suppress the formation of the often-reported Bi₂Fe₄O₉ impurity. The sample was heated twice at 815°C for 4 h with ball milling in between. Excess Bi₂O₃ was removed via a two-step leaching process using first 3.25M then 1.75M HNO₃, followed by several deionized water rinses and drying. The resultant powder was further ball-milled and isostatically pressed into a pellet at 500 MPa. Sintering was conducted at 830°C for 3 h, followed by annealing for 10 h at 500°C. X-ray diffraction analysis of both powder and pellet showed single-phase BiFeO₃. The pellet was cut into a rectangular shape, and silver paint (ST1601-14, Heraeus Inc.) was used to create parallel electrodes on the sample. Macroscopic impedance analysis was performed with an HP 4284A LCR meter over the range of 20 Hz to 1 MHz.

IV. Results and Discussion

(1) SSPM under Lateral Bias

The surface topography and surface potential at a BiFeO₃ surface under different bias conditions are shown in Fig. 4. The
A topographic image exhibits a number of spots due to contaminants and depressions due to inter- and intragranular pores. Grain boundaries can be seen due to selective polishing of grains with different orientations. The surface potential of the grounded BiFeO$_3$ surface exhibits large-scale potential variations due to ferroelectric domains and surface contaminants. On application of a 10 V lateral bias the potential drops at the grain boundaries become evident (Fig. 4(c)). The contrast inverts on application of a bias of opposite polarity (Fig. 4(d)). Note that the potential features related to ferroelectric polarization are independent of the applied bias. Ramping the dc bias across the sample has shown that the potential drop at the interface is linear in external bias and the grain boundaries exhibit ohmic behavior for small biases (∆$V_{gb} < 50$ mV).

(2) ac Transport by SIM

The surface topography, SIM phase images at 20 and 70 kHz and the SIM amplitude image at 70 kHz of the same region are shown in Fig. 5. Note that the phase images exhibit well-defined phase shifts at the grain boundaries, while the amplitude image shows a uniform decrease of amplitude across the surface. Positive phase shifts at the grain boundary and a negative phase shift in the bulk are clearly observed in agreement with theoretical arguments. For higher frequencies phase shifts in the grain interior are not observed because of the resistive component in the experimental circuit. At the same time, the amplitude decreases linearly in the direction of current flow, indicating that the experimental frequency range (10–100 kHz) is above the resonant frequency of the interface. To quantify the frequency dependence of the grain boundary phase shift, the latter was determined for a series of images collected at 10 kHz steps. The analysis in the vicinity of the resonant frequency of the cantilever (60 kHz) is complex because of a force-gradient induced resonant frequency shift and associated nonlinear phase behavior. Therefore, tip-surface phase lag is not constant in the vicinity of cantilever resonance. To relate the SIM phase shift to the material properties, the latter were independently determined by impedance spectroscopy and the corresponding spectra are shown in Fig. 6. From the impedance spectroscopy data, the average grain boundary resistivity and capacitance are estimated as $R_{gb} = 116$ kΩ·cm and $C_{gb} = 7.6$ nF/cm, while the grain interior resistivity and capacitance are $R_{gi} = 812$ Ω·cm and $C_{gi} = 7$ pF/cm. It should be noted that two RC elements provide a relatively poor description of the high-frequency region of the experimental impedance spectra.
the properties of the grain boundary component are well-defined, whereas bulk properties can be determined only approximately. Figure 7 shows the calculated grain boundary phase shift versus frequency dependence as compared with experimental SIM data. The only free parameter in the calculations is the effective grain number. The best fit is obtained for \( n = 210 \) grains, which is comparable with grain number \( N \sim 70 \) estimated from the grain size (\( \sim 20-30 \) \( \mu \)m) and the distance between the measurement point and the left contact (\( \sim 1-2 \) mm). The discrepancy between the two is due to the uncertainty in the bulk resistance and variation in grain boundary properties and orientation. Note the excellent agreement between phase angle frequency dependencies obtained from local measurements and impedance spectroscopy.

V. Conclusions

Scanning probe imaging of electroactive interfaces in ceramic materials and their relationship with conventional 4-probe resistance and impedance spectroscopy measurements have been discussed. Both scanning surface potential microscopy (SSPM) of laterally biased devices and scanning impedance microscopy (SIM) are based on the local detection of surface potential or voltage oscillation amplitude and phase angle by the SPM tip. These techniques permit the local properties to be determined with a resolution of \( \sim 100 \) nm. A noncontact detection mechanism implies that the probe impedance does not contribute to the measured potential, voltage phase, and amplitude. The utility of these techniques for material characterization was illustrated on a sample of polycrystalline BiFeO\(_3\). SSPM of the grounded surface revealed significant potential variations due to ferroelectric polarization. Application of a lateral bias to the electroded sample demonstrated potential drops due to resistive barriers at the grain boundaries; however, quantitative analysis of the SSPM data was precluded by a ferroelectric contribution to the measured potential. SIM phase images of the same region clearly exhibited phase shifts at the interfaces. SIM amplitude images indicated a uniform decrease of the voltage oscillation amplitude across the sample, in agreement with theoretical arguments. At the same time, ferroelectric domain boundaries did not contribute to the SIM image, thus allowing unambiguous correlation of impedance spectra with electroactive grain boundaries. A theoretical model for the quantification of SIM measurements based on the voltage divider effect was developed and used to simulate the SIM phase behavior. For BiFeO\(_3\) ceramics excellent agreement between local SIM measurements and impedance spectroscopy data was found.
Fig. 6. (a) Cole–Cole plots of as-prepared BiFeO₃ pellets and the rectangular sample used for scanning probe microscopy studies. (b) Frequency dependence of the phase angle for the same samples.

Fig. 7. Experimental SIM phase shift across the interface and theoretical curve calculated from the impedance spectra of the sample.

References
